

# Elementary Particles II

## 3 – The Higgs Particle at the LHC

Predictions, Strategies, Machines, Detectors, Data,  
Measurements, Tests of SM

# SSB - I

Field theory: Real scalar field

$$L = \frac{1}{2}(\partial_\mu \phi)^2 - V(\phi)$$

$$V(\phi) = \frac{1}{2}\mu^2\phi^2 + \frac{1}{4}\lambda^2\phi^4, \lambda > 0$$

Reflection symmetric:  $V(\phi) = V(-\phi)$

$V$  Minima:

$$\mu^2 > 0: \phi = 0$$

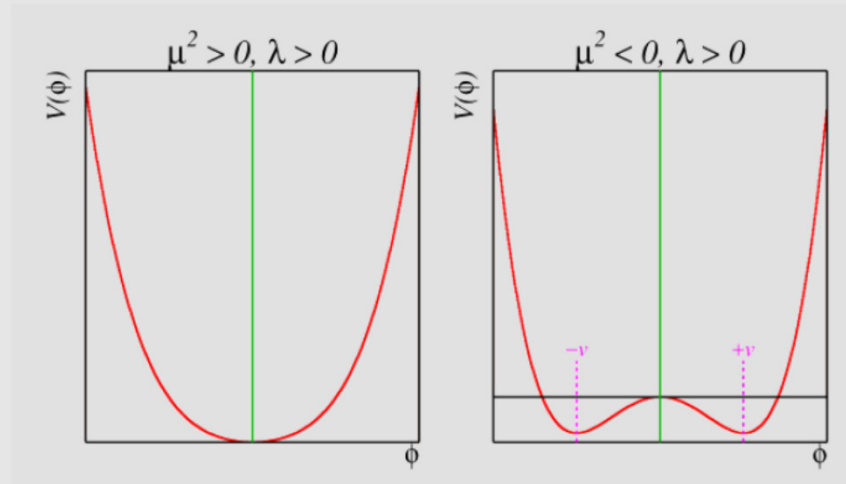
$$\mu^2 < 0: \phi = v = \pm \sqrt{-\frac{\mu^2}{\lambda}}$$

$V$  Minima: Defining *vacuum* state (← Cannot have less energy)

$\mu^2 > 0$ : Vacuum (non degenerate)  $\equiv$  Zero field

$\mu^2 < 0$ : Vacuum (degenerate!) =  $v \neq$  Zero field !!

$v$  = Vacuum Expectation Value (VEV) of  $\phi$



# SSB - II

Choose vacuum state:

$$\langle \phi(x) \rangle_0 = v \quad \text{Spontaneous Symmetry Breaking}$$

Define:  $\phi(x) = v + \eta(x)$

$$\rightarrow L = \frac{1}{2}(\partial_\mu \eta)^2 - \lambda \left( v^2 \eta^2 - v \eta^3 - \frac{1}{4} \eta^4 \right) = \left[ \frac{1}{2}(\partial_\mu \eta)^2 - \lambda v^2 \eta^2 \right] - \lambda v \eta^3 - \frac{1}{4} \lambda \eta^4$$

$$L = \frac{1}{2}(\partial_\mu \eta)^2 - \lambda v^2 \eta^2 \text{ ~~+higher powers of } \eta~~$$

→ Free Klein-Gordon equation

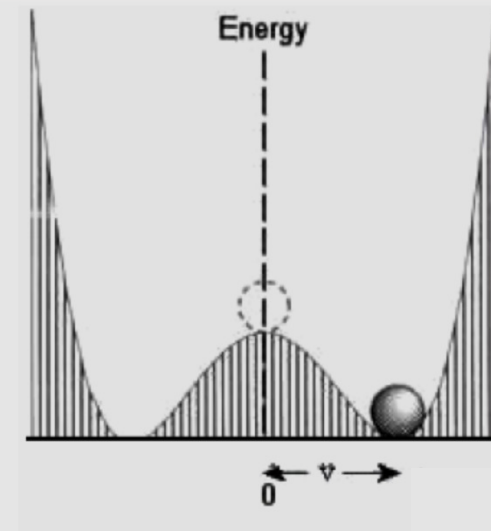
→ Scalar quantum field

$$m^2 = 2\lambda v^2 \rightarrow m = \sqrt{-2\mu^2} > 0$$

[Observe:  $\mu^2 < 0 \rightarrow$  Imaginary mass in original  $L!$ ]

$$\text{KO: } L(\eta) \neq L(-\eta)$$

Reflection symmetry *spontaneously broken*



# SSB - III

Field theory: Complex scalar field

$$\phi = \frac{1}{\sqrt{2}}(\phi_1 + i\phi_2), \phi^* = \frac{1}{\sqrt{2}}(\phi_1 - i\phi_2)$$

$$L = (\partial_\mu \phi)(\partial^\mu \phi)^* - V(\phi)$$

$$V(\phi) = \mu^2 \phi^* \phi + \lambda (\phi^* \phi)^2, \lambda > 0, \mu^2 < 0$$

$U(1)$  symmetric:  $\phi \rightarrow \phi' = e^{i\alpha} \phi$

Observe:  $U(1)$  *continuous* symmetry

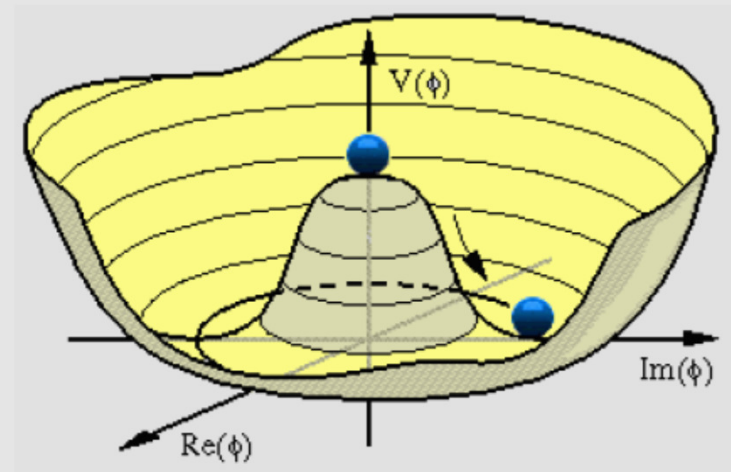
$V$  Minima:

$$\mu^2 < 0: \phi_1^2 + \phi_2^2 = -\frac{\mu^2}{\lambda}$$

→ Vacuum *infinitely* degenerate

Choose vacuum =  $(v, 0)$

→  $U(1)$  symmetry *spontaneously broken*





# SSB - IV

Define:

$$\phi(x) = \frac{1}{\sqrt{2}} [v + \xi(x) + i\eta(x)]$$

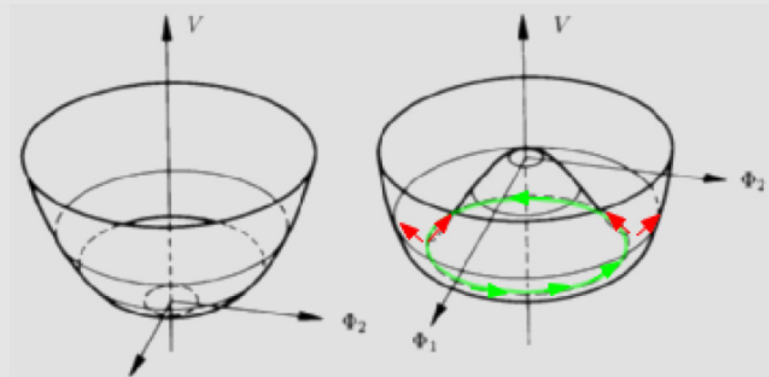
$$L = \frac{1}{2} [(\partial_\mu \xi)^2 + (\partial_\mu \eta)^2] + \mu^2 \eta^2 + \text{higher powers of } \eta$$

Free Klein-Gordon equations for  $(\xi, \eta)$

But: "Kinetic energy" terms for both  $\xi, \eta$ ; Mass term only for  $\eta$

→  $\eta$  field excitations: *massive* scalar particles

→  $\xi$  field excitations: *massless* scalar particles, aka *Goldstone Bosons*



# SSB - V

SSB of a continuous, global ( $\leftarrow$  non local) symmetry

$\rightarrow \infty$  degenerate vacuum states

Symmetry generators transform any vacuum state into another one

Indeed, for a non-degenerate vacuum:

$\langle \phi \rangle_0$  Invariant under  $G$ :

$$\rightarrow e^{i\alpha G} \langle \phi \rangle_0 \simeq (1 + i\alpha G) \langle \phi \rangle_0 = \langle \phi \rangle_0 \leftrightarrow G \langle \phi \rangle_0 = 0$$

$\rightarrow G$  does annihilate a non-degenerate vacuum

For a degenerate vacuum:

$\langle \phi \rangle_0$  Non-invariant under  $G$ :

$\rightarrow$  Goldstone Theorem:

$n$  generators not annihilating the vacuum  $\rightarrow$  Appearance of  $n$  massless scalars

Also called *Goldstone bosons*

# SSB - VI

Example from condensed matter physics: Ferromagnet

Interaction rotationally invariant

But, below Curie temperature

→ Spontaneous magnetization in a random orientation

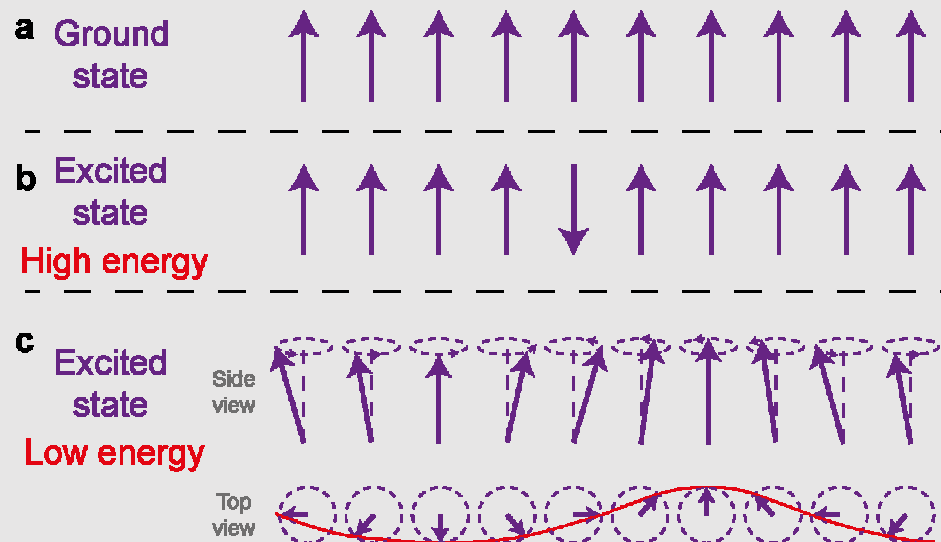
→ Rotational symmetry lost

→ Degenerate vacuum

→ Goldstones

Non-relativistic version of *massless*

Spin waves  $\equiv$  Zero energy-gap *quasi-particles* (i.e. lattice excitation)



# Higgs Mechanism - I

Goldstone theorem would seem to definitely destroy  
our hint of a Standard Model:

3 + 1 massless gauge bosons, only one observed

4 massless scalar bosons, none observed

Local gauge invariance + SSB:

Higgs mechanism

evading Goldstone's theorem

Simple, yet subtle way of giving mass to gauge bosons  
without spoiling gauge invariance (and renormalizability)

# Higgs Mechanism - II

Example by Higgs :

$U(1)$  gauge group, require *local* symmetry:

Gauge vector boson  $A_\mu$  to be introduced, coupling to some current as usual

Now: Add "sombbrero" potential for a complex, scalar field  $\phi = \phi_1 + i\phi_2$

$$L = \underbrace{\left[ \left( \partial_\mu - ieA_\mu \right) \phi^* \right] \left[ \left( \partial^\mu + ieA^\mu \right) \phi \right]}_{EM \text{ interaction of (charged) } \phi} - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \mu^2 \phi^* \phi - \lambda (\phi^* \phi)^2 + \underbrace{\dots}_{\text{Current-field interaction etc}}$$

As found before:

Degenerate vacuum state  $\rightarrow$  SSB picks as vacuum state  $(v, 0)$

# Higgs Mechanism - III

$$\rightarrow \phi = v + \eta_1 + i\eta_2$$

$L$  written in terms of  $\eta_1, \eta_2$ :

Upon quantization, 2 scalar particles  $\rightarrow m_1 = \sqrt{2\lambda v^2}, m_2 = 0$

Plugging  $\phi = v + \eta_1 + i\eta_2$  into  $L$ :

$$L = \frac{1}{2}(\partial_\mu \eta_1)(\partial^\mu \eta_1) - \frac{1}{2} \overbrace{2\lambda v^2}^{m_1^2} \eta_1^2 + \frac{1}{2}(\partial_\mu \eta_2)(\partial^\mu \eta_2) + \frac{1}{2} \overbrace{(ev)^2}^{m_V^2} A^\mu A_\mu - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \underbrace{ev A^\mu \partial_\mu \eta_2}_{??} + \dots$$

*Massive vector!*

Attempting to understand  $L$ :

Massive vector field  $A^\mu$  + Massive scalar field  $\eta_1$  + Massless scalar field  $\eta_2$

Troubling term coupling  $A^\mu$  and  $\eta_2$

# Higgs Mechanism - IV

Use gauge invariance:

$$\begin{cases} \phi \rightarrow \phi' = e^{-ie\theta(x)} \phi \\ A^\mu \rightarrow A'^\mu = A^\mu + \partial_\mu \theta \end{cases}$$

Choose  $\theta$  to make  $\phi$  real: Then  $\eta_2 \equiv 0$  ( $\leftarrow$  Unitary gauge)

$$\rightarrow L = \frac{1}{2} (\partial_\mu \eta_1) (\partial^\mu \eta_1) - \frac{1}{2} 2\lambda v^2 \eta_1^2 + \underbrace{\frac{1}{2} \overbrace{(ev)^2}^{M_V^2} A^\mu A_\mu}_{\text{Massive vector!}} - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \dots$$

Massive vector field  $A^\mu$  + Massive scalar field  $\eta_1$

Counting degrees of freedom:

$$\underbrace{2}_{A_\mu} + \underbrace{1+1}_\phi = \underbrace{3}_{A_\mu} + \underbrace{1}_{\eta_1} \quad \text{OK}$$

Standard picture:

By effect of a smart gauge transformation,  
the massless vector field  $A_\mu$  has eaten the Goldstone boson  $\eta_2$   
to become massive

# Higgs Mechanism - V

Attempting to dissipate some misunderstandings likely to sneak in:  
Mostly related to our naive perception of what is really a 'particle'

1) Where is the mass?

To identify mass terms in  $L$ : Not necessarily a trivial task

Key point: Particle content *only meaningful in perturbative expansion*

Example:  $L = (\partial_\mu \phi)(\partial^\mu \phi)^* - (-\mu^2 \phi^* \phi) - \lambda(\phi^* \phi)^2, \lambda > 0, \mu^2 > 0$

$-\mu^2 \rightarrow$  Imaginary mass  $\rightarrow$  Nonsense  $\rightarrow$  ???

But: To use this form of  $L$  to extract Feynman rules, should expand around  $|\phi| = 0$

Unstable extremum  $\rightarrow$  Can't make it

Rewrite by expanding around  $\eta = 0$ :  $L = \frac{1}{2}(\partial_\mu \eta)^2 - \lambda v^2 \eta^2 + \dots$

Stable extremum  $\rightarrow$  OK

$\rightarrow$  Particle content should be identified in this form



# Higgs Mechanism - VI

2) What's so special in unitary gauge?

Nothing:  $L$  invariant under local gauge transformations, including the one to unitary gauge:

→  $L$  describe the same physics before and after the gauge transformation

But: Particle content much easier to extract in the unitary gauge

3) Disappearing Goldstones !?

Indeed: And re-appearing as extra degrees of freedom for massive gauge bosons

See comment above on the tricky business of defining what is a particle...

4) What decides which vacuum is selected among the many?

Not really relevant: Any choice yields identical results

5) Could we make it with the SM without SSB and all that complicated swapping of degrees of freedom?

Actually no: SSB is an *intrinsic* feature of certain quantum systems

(with an infinite number of degrees of freedom)

# SM Reminder - I

Extend Abelian Higgs model to non-Abelian gauge symmetry:

$$\text{Gauge group} = SU(2)_L \otimes U(1)_Y$$

To add SSB to the Standard Model:

Add a doublet of complex, scalar fields:

$$\phi(x) = \begin{pmatrix} \phi^+(x) \\ \phi^0(x) \end{pmatrix}$$

$$\text{Assuming } y = 1 \rightarrow \begin{cases} Q[\phi^+(x)] = +1 \\ Q[\phi^0(x)] = 0 \end{cases}$$

# SM Reminder - II

$SU(2)_L \otimes U(1)_Y$  Gauge transformation of doublet:

$$\phi \rightarrow \phi' = \exp \left\{ -i \left[ \frac{g}{2} \mathbf{a}(x) \cdot \boldsymbol{\tau} + \frac{g'}{2} y \theta(x) I \right] \right\} \phi$$

$SU(2)_L \otimes U(1)_Y$  Covariant derivative:

$$D^\mu = \partial^\mu + i \left[ \frac{g}{2} \boldsymbol{\tau} \cdot \mathbf{W}^\mu + \frac{g'}{2} y B^\mu \right]$$

→ Additional term to EW lagrangian:

$$L_H = D_\mu \phi^\dagger D^\mu \phi - \mu^2 \phi^\dagger \phi - \lambda (\phi^\dagger \phi)^2$$

Take  $\mu^2 < 0$ ,  $\lambda > 0$ :

$$|\phi|_{\min}^2 = -\frac{\mu^2}{2\lambda} = \frac{v^2}{2} \rightarrow v = \sqrt{-\frac{\mu^2}{\lambda}}$$

Pick ground state (= vacuum) as

$$\langle \phi \rangle_0 = \begin{pmatrix} 0 \\ v \\ \frac{v}{\sqrt{2}} \end{pmatrix} \rightarrow \text{SSB of Electroweak gauge symmetry}$$

$$v = 246 \text{ GeV}$$

# SM Reminder - III

Introduce field deviation from vacuum:

$$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} \sigma_1 + i\sigma_2 \\ v + \eta_1 + i\eta_2 \end{pmatrix} \rightarrow V = -\frac{\mu^4}{4\lambda} + \lambda v^2 \eta_1^2 + \lambda v \eta_1 (\sigma_1^2 + \sigma_2^2 + \eta_1^2 + \eta_2^2) + \frac{\lambda}{4} (\sigma_1^2 + \sigma_2^2 + \eta_1^2 + \eta_2^2)^2$$

After properly 'rotating' to Unitary Gauge:

1 massive scalar:  $\eta_1, m_{\eta_1} \equiv m_H = \sqrt{2\lambda v^2} \leftarrow$  The Higgs

2 massive, charged vectors:  $W^\pm, m_W = \frac{g}{2} \sqrt{-\frac{\mu^2}{\lambda}}$

1 massive, neutral vector:  $Z^0, m_Z = \frac{\sqrt{(g^2 + g'^2)}}{2} \sqrt{-\frac{\mu^2}{\lambda}}$

→ Relating model parameters to independently measured constants  $e, G_F, \sin \theta_W$ :

$$M_W = \sqrt{\frac{\sqrt{2}g^2}{8G_F}} = \sqrt{\frac{\sqrt{2}e^2}{8G_F \sin^2 \theta_W}} \simeq 77.5 \text{ GeV}, \quad M_Z = \frac{M_W}{\cos \theta_W} \simeq 88.4 \text{ GeV}$$

$$M_H = \frac{\sqrt{2}\lambda}{G_F} = ???$$

# SM Reminder - IV

Gauge terms of  $L$  in the unitary gauge, in terms of the physical fields:

$$L_B + L_H$$

$$= -\frac{1}{4} F_{\mu\nu}(x) F^{\mu\nu}(x) \quad \text{Photon}$$

$$-\frac{1}{2} F_{\mu\nu}^W(x) F^{\mu\nu W}(x) + \frac{1}{2} m_W^2 W_\mu^\dagger W^\mu \quad W^\pm \text{ boson}$$

$$-\frac{1}{4} Z_{\mu\nu}(x) Z^{\mu\nu}(x) + \frac{1}{2} m_Z^2 Z_\mu Z^\mu \quad Z^0 \text{ boson}$$

$$+ (\partial_\mu \sigma)(\partial^\mu \sigma) - \frac{1}{2} m_H^2 \sigma^2 \quad H \text{ Higgs boson}$$

$$+ L_{BB}^I + L_{HH}^I + L_{HB}^I \quad \text{Gauge-Higgs, Higgs self-, Gauge self-interactions}$$

# SM Reminder - V

Fermion masses: Yukawa (scalar) coupling

Describing interaction between Dirac and scalar fields:

Example: Single lepton family

$$L_{HL} = -g_l \left[ \bar{\Psi}_l^L \Phi \psi_l^R + \bar{\psi}_l^R \Phi^\dagger \Psi_l^L \right] - \underbrace{g_{\nu_l}}_{=0 \text{ for massless neutrino}} \left[ \bar{\Psi}_l^L \tilde{\Phi} \psi_{\nu_l}^R + \bar{\psi}_{\nu_l}^R \tilde{\Phi}^\dagger \Psi_l^L \right], \quad \tilde{\Phi} = \begin{pmatrix} \phi_b^* \\ -\phi_a^* \end{pmatrix}$$

In the unitary gauge:

$$L_{HL} = -\frac{1}{v} m_l \bar{\psi}_l \psi_l \sigma - \frac{1}{v} m_{\nu_l} \bar{\psi}_{\nu_l} \psi_{\nu_l} \sigma$$

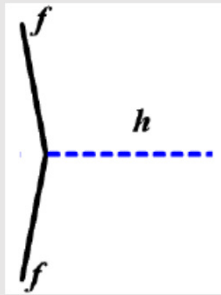
Lepton masses in terms of model parameters:

$$m_l = \frac{v g_l}{\sqrt{2}}, \quad m_{\nu_l} = \frac{v g_{\nu_l}}{\sqrt{2}} (= 0 \text{ in the Minimal Standard Model})$$

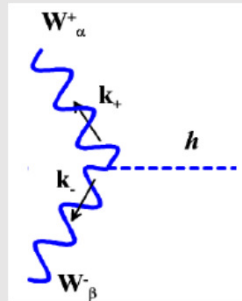
$g_l$  individual constant

# SM Reminder - VI

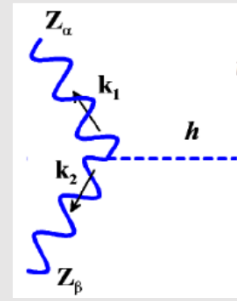
Higgs vertexes:



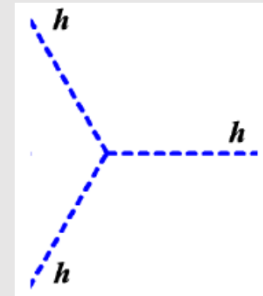
$$-im_f \sqrt{\sqrt{2}G_F} \bar{f} f$$



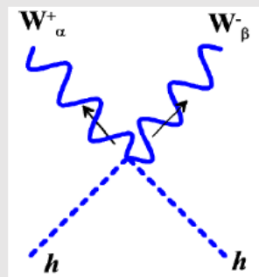
$$2iM_W^2 \sqrt{\sqrt{2}G_F} g^{\alpha\beta} W_\alpha^{+\dagger} W_\beta^{-\dagger} h$$



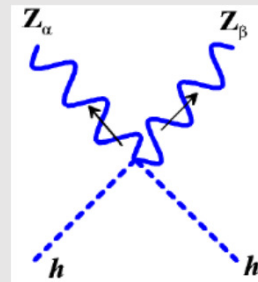
$$2iM_Z^2 \sqrt{\sqrt{2}G_F} g^{\alpha\beta} Z_\alpha^\dagger Z_\beta^\dagger h$$



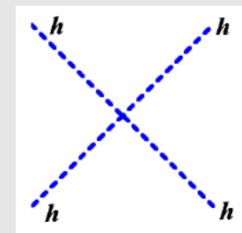
$$-3im_h^2 \sqrt{\sqrt{2}G_F} hhh$$



$$2iM_W^2 \sqrt{2}G_F g^{\alpha\beta} hh W_\alpha^{+\dagger} W_\beta^{-\dagger}$$



$$2iM_Z^2 \sqrt{2}G_F g^{\alpha\beta} hh Z_\alpha^\dagger Z_\beta^\dagger$$



$$-3im_h^2 \sqrt{2}G_F hhhh$$

Observe: Amplitude  $\sim$  mass(fermions),  $\text{mass}^2$ (bosons)

# About the Higgs Field - I

Universal, constant field

Lorentz scalar  $\rightarrow$  Same value in any frame, rotation invariant

Non-standard feature:

Vacuum expectation value  $v \neq 0$

Usual analogy: Spontaneously magnetized ferromagnet:

$\mathbf{M} \neq 0$  below Curie temperature

$\rightarrow$  Pick up a direction

Ground state rotationally not symmetric, in spite of  $H$  being symmetric



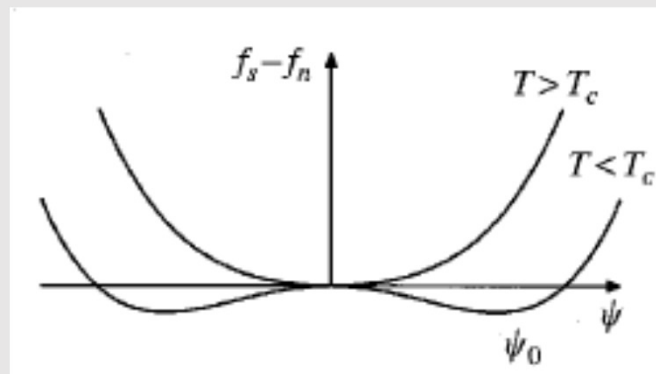
# About the Higgs Field - II

Better analogy: Superconductor

Energy difference between normal and s.c. state at two different temperatures

$$\Delta E = a(T)|\psi|^2 + \frac{1}{2}b(T)|\psi|^4 + \dots \quad \text{Landau theory of phase transitions}$$

$\psi$  is the Cooper pair 'wave function'  $\rightarrow |\psi|^2 \sim$  density of Cooper pairs



Below  $T_c$ , the minimum energy state ('vacuum') occurs for  $\psi = \psi_0 \neq 0$ , phase undefined  
 $\rightarrow U(1)$  QED gauge invariance spontaneously broken

$\rightarrow$  Photon becomes 'massive'  $\rightarrow \mathbf{B} = 0$  inside

# About the Higgs Field - III

$\psi$  'Higgs field' of superconductivity:  $\langle \psi \rangle \neq 0 \leftrightarrow$  Permanent supercurrents

Superconductive state:

'Higgs field' = 'Wave function' of Cooper pairs

→ Not a fundamental field

→ 'Composite' field of fundamental fermions (electrons)

Why there is the composite?

$e$ - $e$  effective interaction: Attractive (!) due to  $e$  - lattice interaction

Is the 'real' Higgs field a genuine, fundamental field or a composite?

Good question..No answer (yet):

Take it as a fundamental field

# About the Higgs Field - IV

A couple of questions:

1) What about the nonzero VEV of the Higgs field?

Higgs: Unique field whose VEV  $\neq 0$

Similar to magnetization  $\mathbf{M} \neq 0$  in a ferromagnet

But:

*In a vacuum*  $\rightarrow$  Not related to many body effects

*Lorentz scalar*  $\rightarrow$  No preferred direction, reference frame

2) Does it involve a new force? 'Giving mass to  $\approx$  all the fundamental constituents' ??

- Part of the standard EW interaction, often as a negligible contribution:

Higgs *particle* exchange diagrams between Fermion lines normally strongly suppressed

by  $m_f/m_W$  factors as compared to  $\gamma, Z^0, W^\pm$  exchange (Not true for  $t$  quark!)

3- & 4-boson diagrams with and without  $H$  similar

- Crucial role as 'Background' interaction:

For most particles Higgs *field* coupling translates into *inertial mass* !

# About the Higgs Field - V

Apparently contributing to vacuum energy density:

Beware: Take *potential energy*  $V(\phi)$

$$\begin{aligned} V_{\min} = V(v) &= \frac{1}{2}\mu^2 v^2 + \frac{1}{4}\lambda v^4 \quad \text{use } \mu^2 = -\lambda v^2 \\ &= -\frac{1}{4}\lambda v^4 \quad \text{use } m_h^2 = 2\lambda v^2 \\ &= -\frac{1}{8}m_h^2 v^2 \end{aligned}$$

Constant term: Usually not considered

Does not enter field equations, where only energy *differences* count

But: Taken into account by gravity

→ Cosmological term ?

*Cosmological constant* : Possibly additional term in Einstein's field equations

May yield long range attraction/repulsion, according to sign

Invented by Einstein in order to guarantee static universes

Rejected by Einstein at the time of discovery of expansion of the Universe

Recently resurrected following the discovery of accelerated expansion

# About the Higgs Field - VI

$$\text{Zero point energy} = -\frac{1}{8}m_h^2v^2 \sim \rho_{\text{Higgs}}$$

$$\text{Indeed: } \left[ -\frac{1}{8}m_h^2v^2 \right] = \underbrace{E^4}_{\text{GeV}^4} = E(E^{-1})^{-3} \rightarrow \frac{E}{L^3} \quad \text{Energy density}$$

$$\rho_{\text{Higgs}} \sim 1.210^8 \text{ GeV}^4$$

By assuming  $\rho$  to be a cosmological term, compare:

$$\rho_{\text{observed}} \sim 10^{-47} \text{ GeV}^4 !$$

$\rightarrow \rho_{\text{Higgs}}$  55 orders of magnitude too big

(and with the wrong sign...)

Quick fix:  $V(v)$  can be set = 0 by adding a constant to  $V(\phi)$

Constant apparently unrelated to  $m_h, v...$

...to be chosen to an accuracy of 1 part out of  $10^{55}$  !

Fine tuning problem, still essentially unsolved

Something missing?

# About the Higgs Field - VII

Higgs boson: Quantum excitation of the field, mass  $m_H$  *not* given by the field

Further issue:

$V(\phi)$  appearing in  $L$ : *Classical* potential

→ Must be quantized

→ Will be used perturbatively

→ Radiative corrections will modify the classical  $V(\phi)$

Similar to vacuum polarization corrections to Coulomb potential in QED

(Uehling potential & Lamb shift)

Standard effect:

Running constants, including  $\lambda$

$$L_H = D_\mu \phi^\dagger D^\mu \phi - \mu^2 \phi^\dagger \phi - \lambda (\phi^\dagger \phi)^2$$

$$\lambda = \lambda(q^2)$$

→  $m_H$  modified by radiative corrections

Upon taking  $\mu^2 < 0$ ,  $\lambda(0) > 0$

→  $\lambda$  evolution depending on  $\beta$  – *functions*

# About the Higgs Field - VIII

Running couplings and  $\beta$  – functions:

$$\frac{dg^2}{d \ln Q^2} \equiv 4\pi\beta(g^2) = \underbrace{bg^4}_{1 \text{ loop}} + \underbrace{O(g^6)}_{2 \text{ loop}} + \dots$$

$$\rightarrow \frac{dg_i^2}{d \ln Q^2} = 4\pi\beta_i(g_i^2) \simeq b_i g_i^4$$

For the EW interaction:

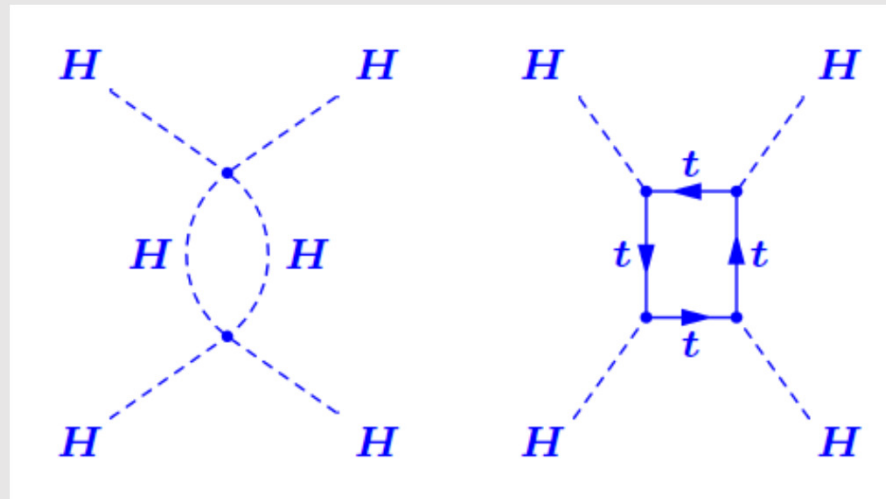
$$b_g = -\frac{19}{6 \cdot 16\pi^2}, \quad b_{g'} = +\frac{41}{6 \cdot 16\pi^2}$$

Higgs couplings:

$$\frac{d\lambda}{d \ln Q^2} = \frac{1}{32\pi^2} \left[ 24(\lambda^2 + h_t^2 - h_t^4) - 3\lambda(3g^2 + g'^2) + \frac{3}{8}(2g^4 + (g^2 + g'^2)^2) \right] \text{ Self}$$

$$\frac{dh_t}{d \ln Q^2} = \frac{1}{32\pi^2} \left[ 9h_t^3 - h_t \left( 8g_s^2 + \frac{9}{4}g^2 + \frac{17}{12}g'^2 \right) \right] \text{ Top (Yukawa)}$$

$$\rightarrow m_H < \left( \frac{2\sqrt{2}\pi^2}{3G_F \ln \frac{\Lambda}{\nu}} \right)^{1/2} \sim \begin{matrix} O(140 \text{ GeV}), \Lambda \sim m_{\text{Planck}} \approx 1.210^{19} \text{ GeV} \\ O(650 \text{ GeV}), \Lambda \sim 1 \text{ TeV} \end{matrix}$$



# About the Higgs Field - IX

$$\frac{d\lambda}{d \ln Q^2} \sim \frac{3\lambda^2}{4\pi^2} \quad \text{Neglect smaller contributions at large } \lambda$$

$$\frac{d\lambda}{\lambda^2} \sim \frac{3}{4\pi^2} d \ln Q^2 \rightarrow -\frac{1}{\lambda(Q^2)} + \frac{1}{\lambda(\nu^2)} \sim \frac{3}{4\pi^2} \ln \frac{Q^2}{\nu^2}$$

$$\rightarrow \frac{1}{\lambda(Q^2)} \sim \frac{1}{\lambda(\nu^2)} - \frac{3}{4\pi^2} \ln \frac{Q^2}{\nu^2}$$

$$\lambda(\nu^2) = \frac{G_F m_H^2}{\sqrt{2}}$$

$$\rightarrow \lambda(Q^2) \sim \frac{\lambda(\nu^2)}{1 - \frac{3}{4\pi^2} \lambda(\nu^2) \ln \frac{Q^2}{\nu^2}}$$

$$\lambda \rightarrow \infty \text{ as } \frac{3}{4\pi^2} \lambda(\nu^2) \ln \frac{Q^2}{\nu^2} \rightarrow 1 \quad \text{Diverging at 'Landau pole'} \quad Q_{LP} = \nu \exp\left(\frac{2\pi^2}{3\lambda(\nu^2)}\right) = \nu \exp\left(\frac{2\sqrt{2}\pi^2}{3G_F m_H^2}\right)$$

$$\rightarrow \text{New physics required at scale } \Lambda < Q_{LP} \rightarrow \ln \frac{\Lambda}{\nu} < \left(\frac{2\sqrt{2}\pi^2}{3G_F m_H^2}\right) \rightarrow m_H < \left(\frac{2\sqrt{2}\pi^2}{3G_F \ln \frac{\Lambda}{\nu}}\right)^{1/2}$$



# About the Higgs Field - X

$$\frac{d\lambda}{d \ln Q^2} \sim -\frac{3h_t^4}{4\pi^2} \text{ Neglect smaller contributions at small } \lambda$$

$$\rightarrow d\lambda \sim -\frac{3h_t^4}{4\pi^2} d \ln Q^2$$

$$\rightarrow \lambda(Q^2) \sim \lambda(\nu^2) - \frac{3h_t^4}{4\pi^2} \ln \frac{Q^2}{\nu^2}$$

$\lambda$  must stay +ve in order to keep vacuum stable (!):

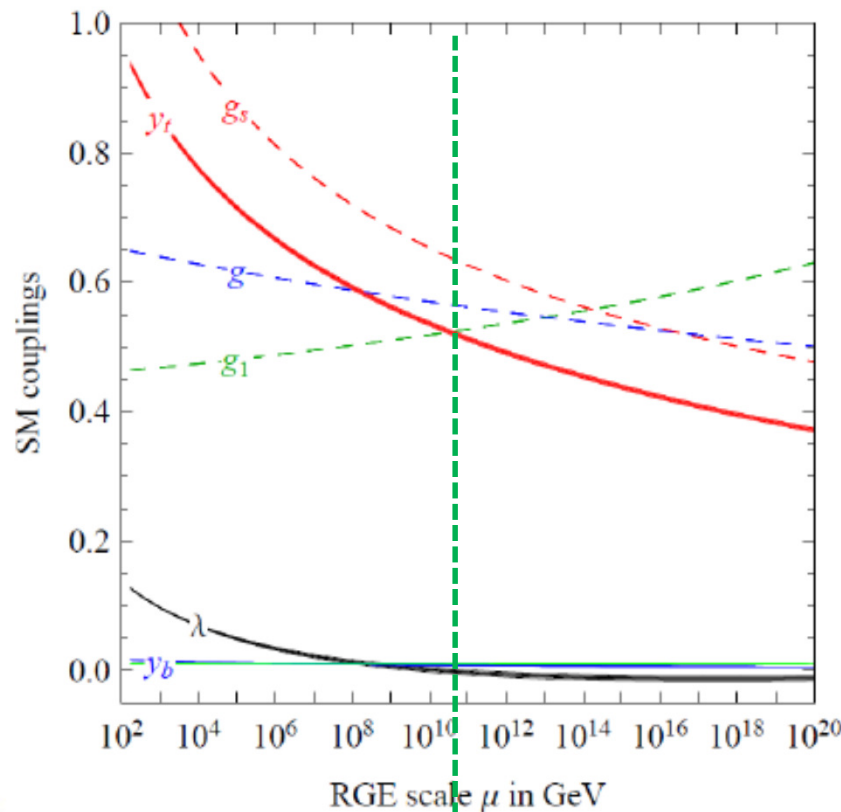
Don't like a too quick End of the World

$$\rightarrow \lambda(\nu^2) > \frac{3h_t^4}{4\pi^2} \ln \frac{Q^2}{\nu^2} \rightarrow \frac{G_F m_H^2}{\sqrt{2}} > \frac{3h_t^4}{4\pi^2} \ln \frac{Q^2}{\nu^2} \text{ for some } Q \sim \Lambda$$

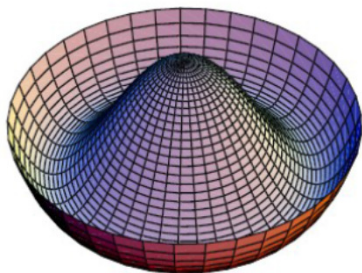
$$\rightarrow m_H > \left( \frac{3h_t^4}{\sqrt{2}\pi^2 G_F} \ln \frac{\Lambda}{\nu} \right)^{1/2}$$

# About the Higgs Field - XI

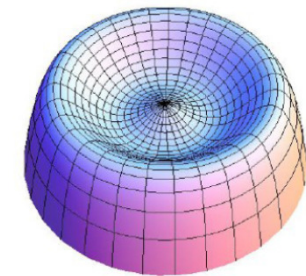
Running couplings:



Sombrero:  $\lambda > 0$   
Relax



Dog Bowl:  $\lambda < 0$   
End of the World  
(sometime)



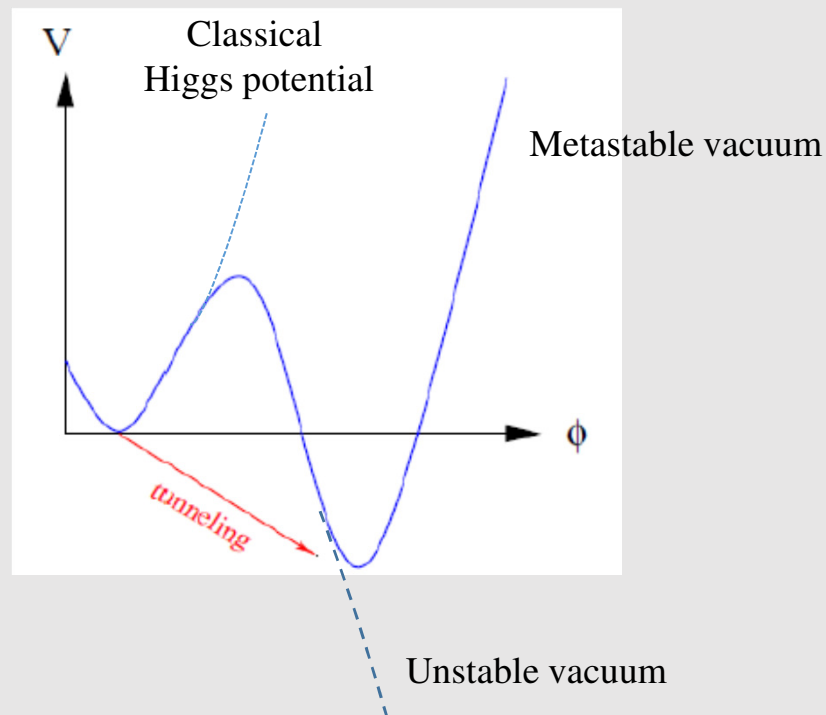
$\Lambda$

# About the Higgs Field - XI

Radiative corrections leading to major changes in the effective Higgs potential at large  $\phi$  values:

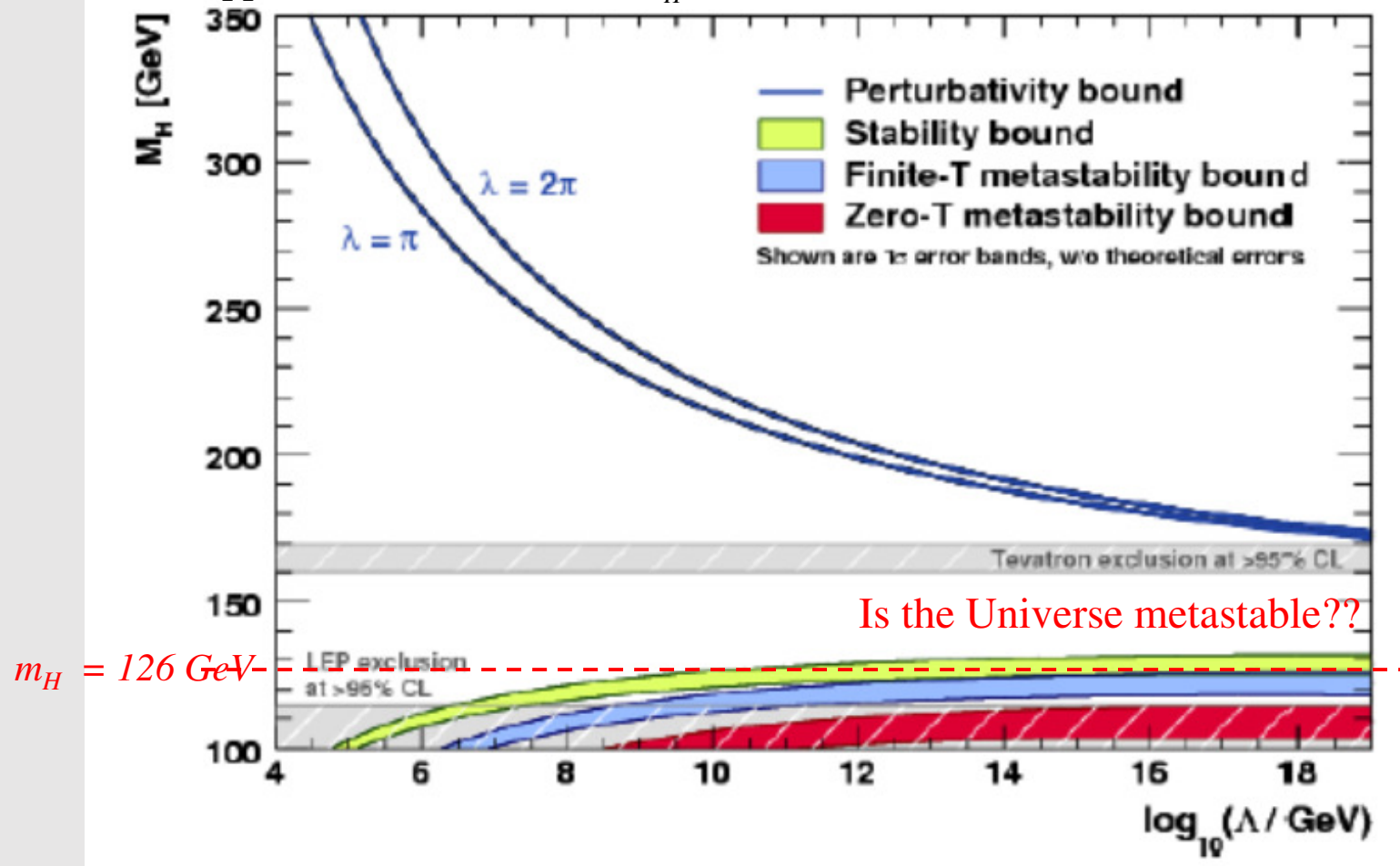
Details tied to  $m_H, m_t$

Might induce vacuum instability/metastability through fast/slow tunneling



# About the Higgs Field - XII

Theoretical upper & lower bounds on  $m_H$  :



# Hunting the Higgs

Try to sketch some guidelines:

(i) Production modes  $\rightarrow$  Machines

(ii) Decay modes  $\rightarrow$  Detectors

Both related to couplings

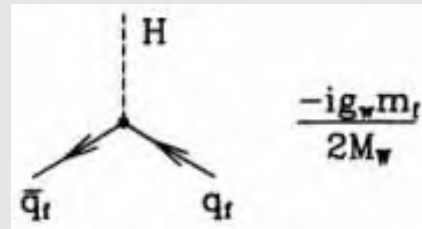
Compare rates, backgrounds

$\rightarrow$  Sensitivity

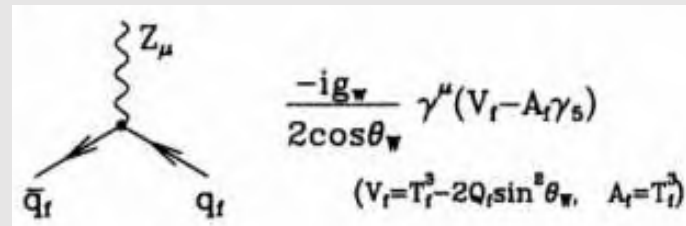
$\rightarrow$  Further observables (Spin/Parity, Width, Branching Ratios,..)

# Higgs Production - I

Start from  $H$  coupling to Fermions:



Compare to coupling to  $Z^0$  :

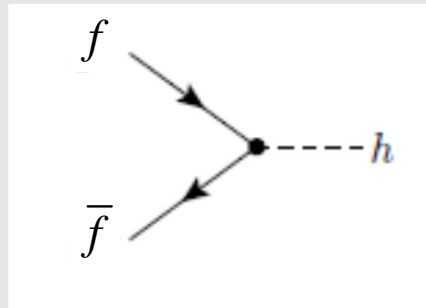


→  $H$  coupling down by a factor  $\sim \frac{m_f}{m_w}$  as compared to  $Z^0$

# Higgs Production - II

First mode:

$s$ -channel formation:



Ideal for lineshape scan, provided cross-section is big enough

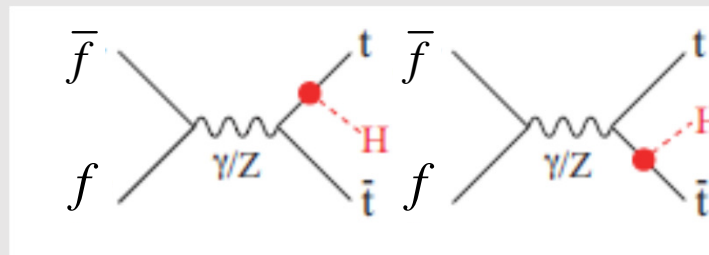
Lepton colliders:

Tough requirements on luminosity, energy resolution

# Higgs Production - III

Second mode:

$H$  radiation from quarks, sizeable contribution from Top:



$t\bar{t}$  signature might be useful to tag



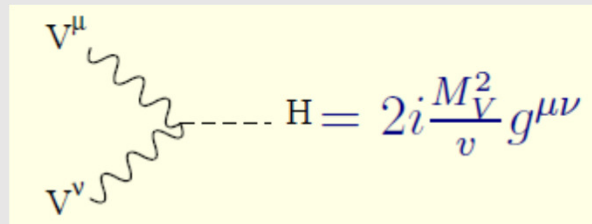
# Higgs Production - IV

Shift to gauge bosons:

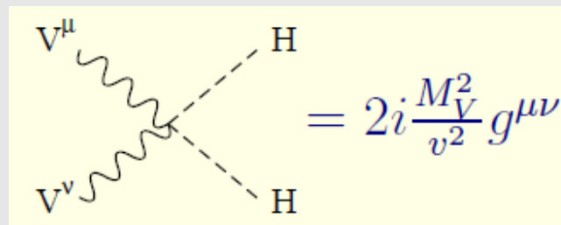
Exclude massless photon, gluon *at tree level*

[Photon, gluon *loop* contribution to be taken into account: See later]

More promising:  $W, Z$  mass very large



A Feynman diagram showing two incoming gluons, labeled  $V^\mu$  and  $V^\nu$ , with wavy lines. They meet at a vertex from which a single dashed line representing a Higgs boson ( $H$ ) emerges. The diagram is associated with the equation  $H = 2i \frac{M_V^2}{v} g^{\mu\nu}$ .

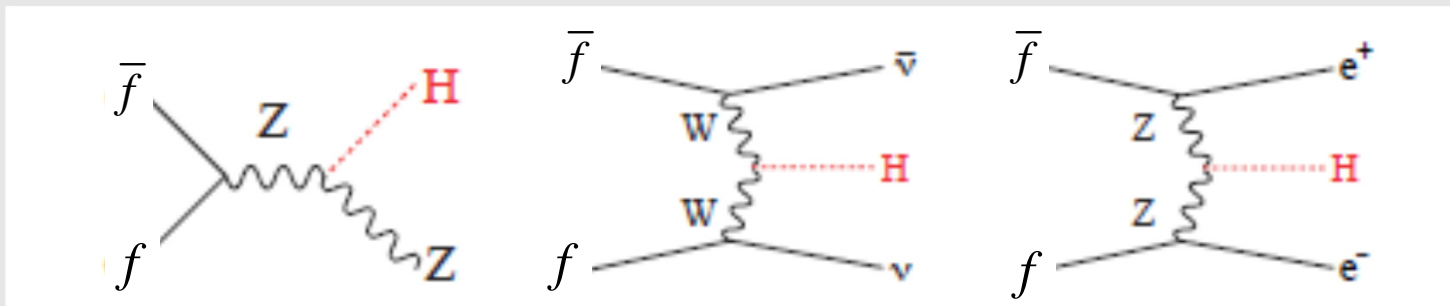


A Feynman diagram showing two incoming quarks, labeled  $V^\mu$  and  $V^\nu$ , with wavy lines. They meet at a vertex from which two dashed lines representing Higgs bosons ( $H$ ) emerge. The diagram is associated with the equation  $= 2i \frac{M_V^2}{v^2} g^{\mu\nu}$ .

# Higgs Production - V

Best modes:

'Higgsstrahlung', 'Gauge boson fusion'

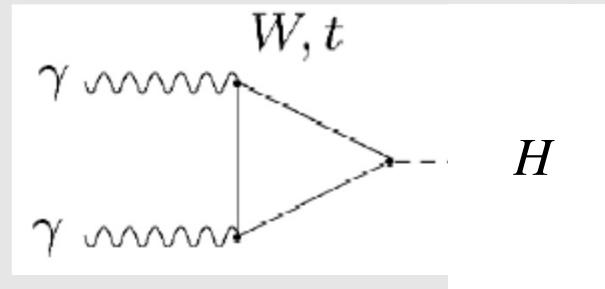


# Higgs Production - VI

Beyond tree level: Very Important Loops

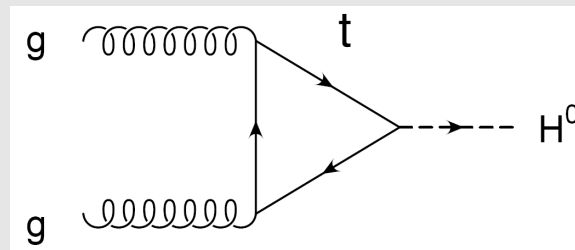
Lepton machines:

Interesting diagrams, also quite relevant to detection

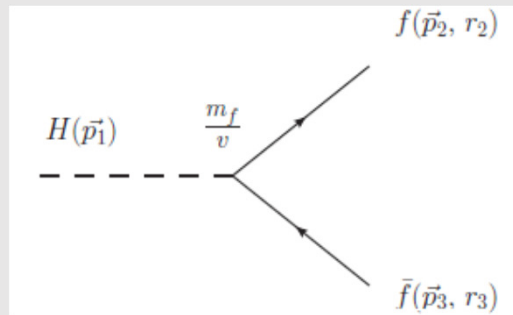


Parton machines:

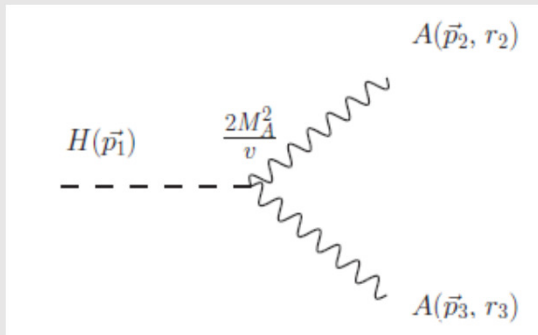
Dominant diagram at LHC



# Higgs Decays - I



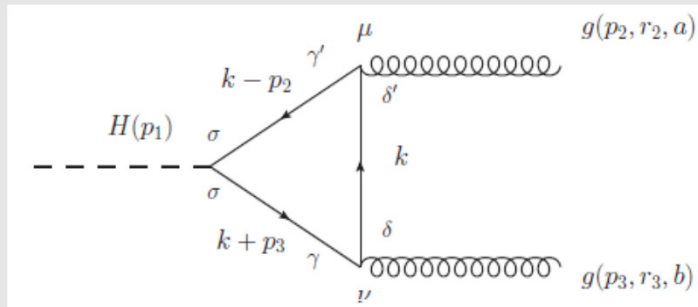
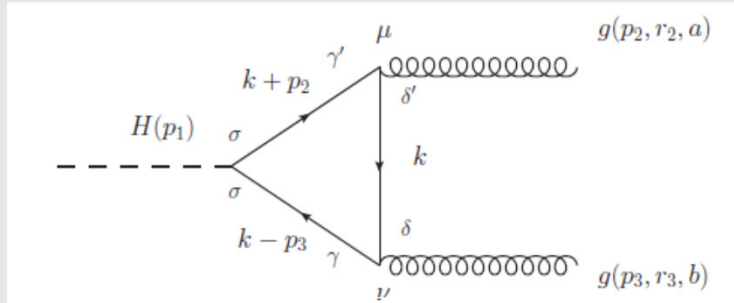
$$\Gamma(H \rightarrow f\bar{f}) = N_C \frac{1}{8\pi} \frac{m_f^2}{v^2} M_H \left(1 - \frac{4m_f^2}{M_H^2}\right)^{3/2}$$



$$\Gamma(H \rightarrow WW) = \frac{1}{4\pi} \frac{M_W^4}{M_H v^2} \left(1 - \frac{4M_W^2}{M_H^2}\right)^{1/2} \left(3 + \frac{1}{4} \frac{M_H^4}{M_W^4} - \frac{M_H^2}{M_W^2}\right)$$

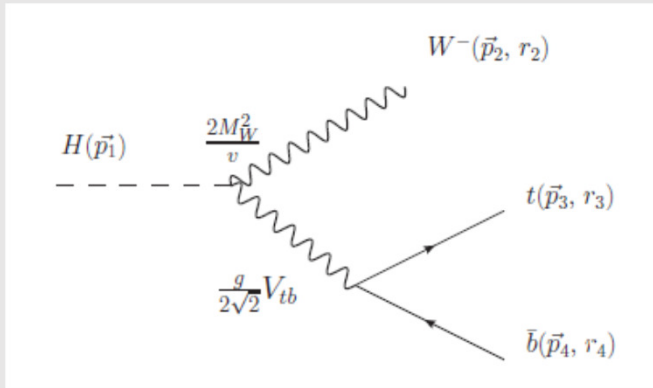
$$\Gamma(H \rightarrow ZZ) = \frac{1}{8\pi} \frac{M_Z^4}{M_H v^2} \left(1 - \frac{4M_Z^2}{M_H^2}\right)^{1/2} \left(3 + \frac{1}{4} \frac{M_H^4}{M_Z^4} - \frac{M_H^2}{M_Z^2}\right)$$

# Higgs Decays - II



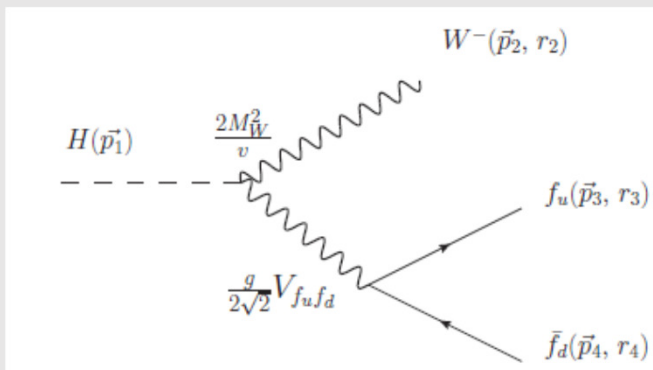
$$\Gamma(H \rightarrow gg) = \frac{M_H^3}{8\pi v^2} \left(\frac{\alpha_s}{\pi}\right)^2 n^2 |D(n)|^2$$

# Higgs Decays - III



$$\Gamma(H \rightarrow Wtb) = N_C \frac{g^2}{2v^2} \frac{M_W^4}{M_H} |V_{tb}|^2 \int dQ_3 \frac{G^{\beta\nu} T_{\beta\nu}}{[s_{34} - M_W^2]^2}$$

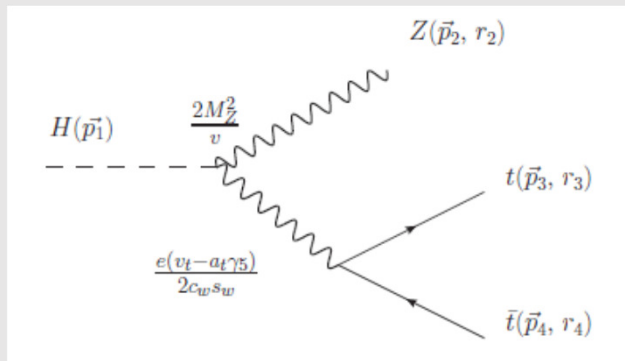
3-body phase space factor



$$\Gamma(H \rightarrow W f_u f_d) = \frac{g^2}{v^2} \frac{3M_W^2}{256\pi^3} M_H S(x)$$

3-body phase space factor

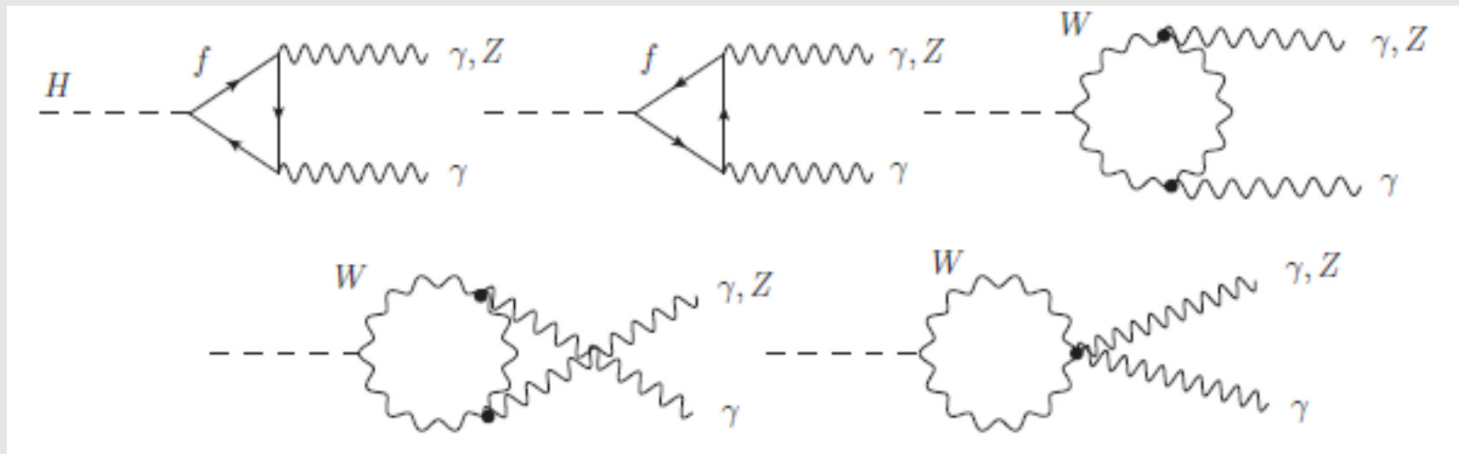
# Higgs Decays - IV



$$\Gamma(H \rightarrow Z f \bar{f}) = \frac{g^2}{v^2} \frac{3M_Z^2}{256 \pi^3} M_H S(x) \frac{R(\theta_w)}{\cos^2 \theta_w} \left( \frac{7}{12} - \frac{10}{9} \sin^2 \theta_w + \frac{40}{27} \sin^4 \theta_w \right)$$

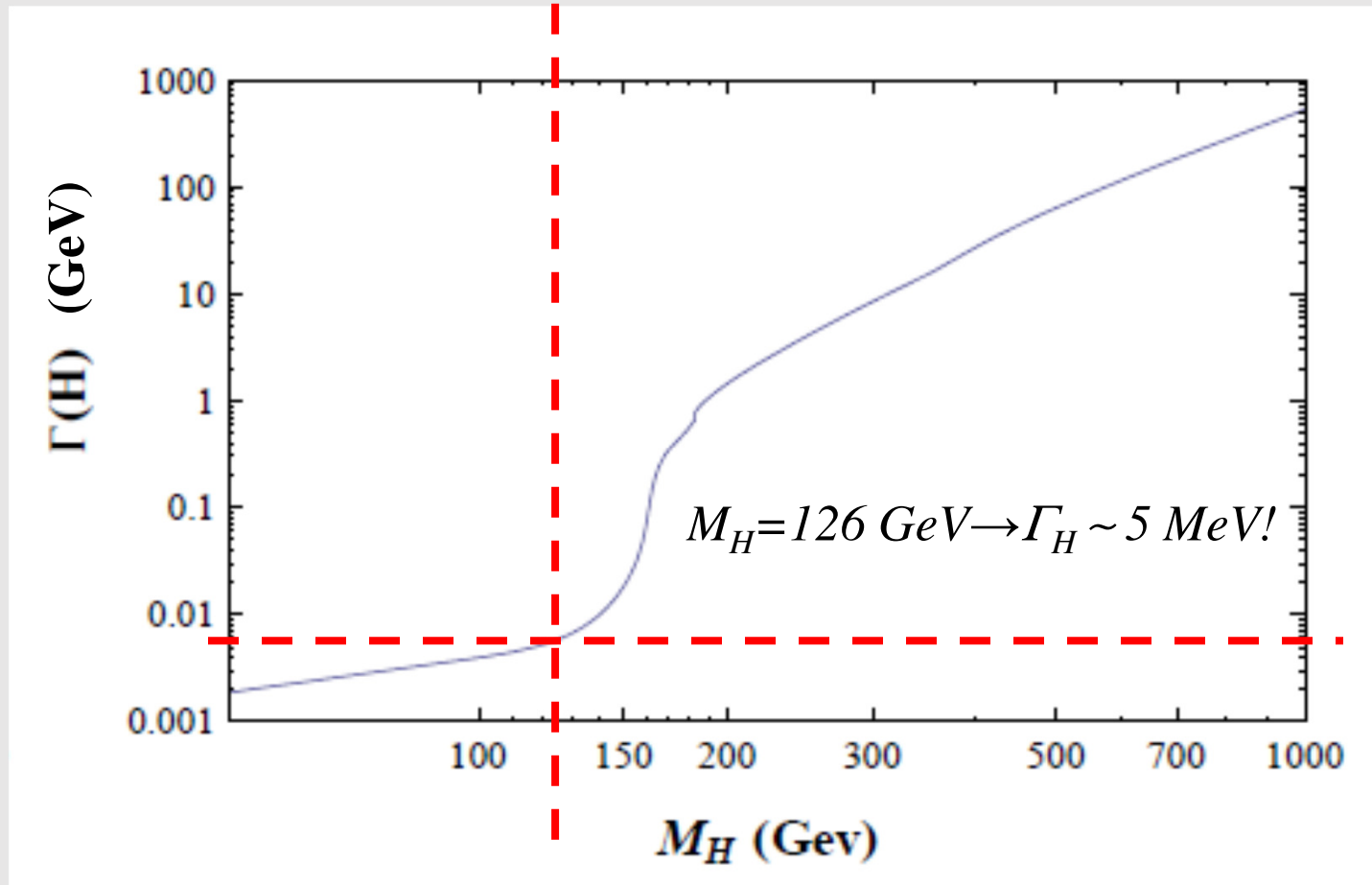
3-body phase space factor

$$\Gamma(H \rightarrow Z / \gamma, \gamma)$$



# Higgs Decays - V

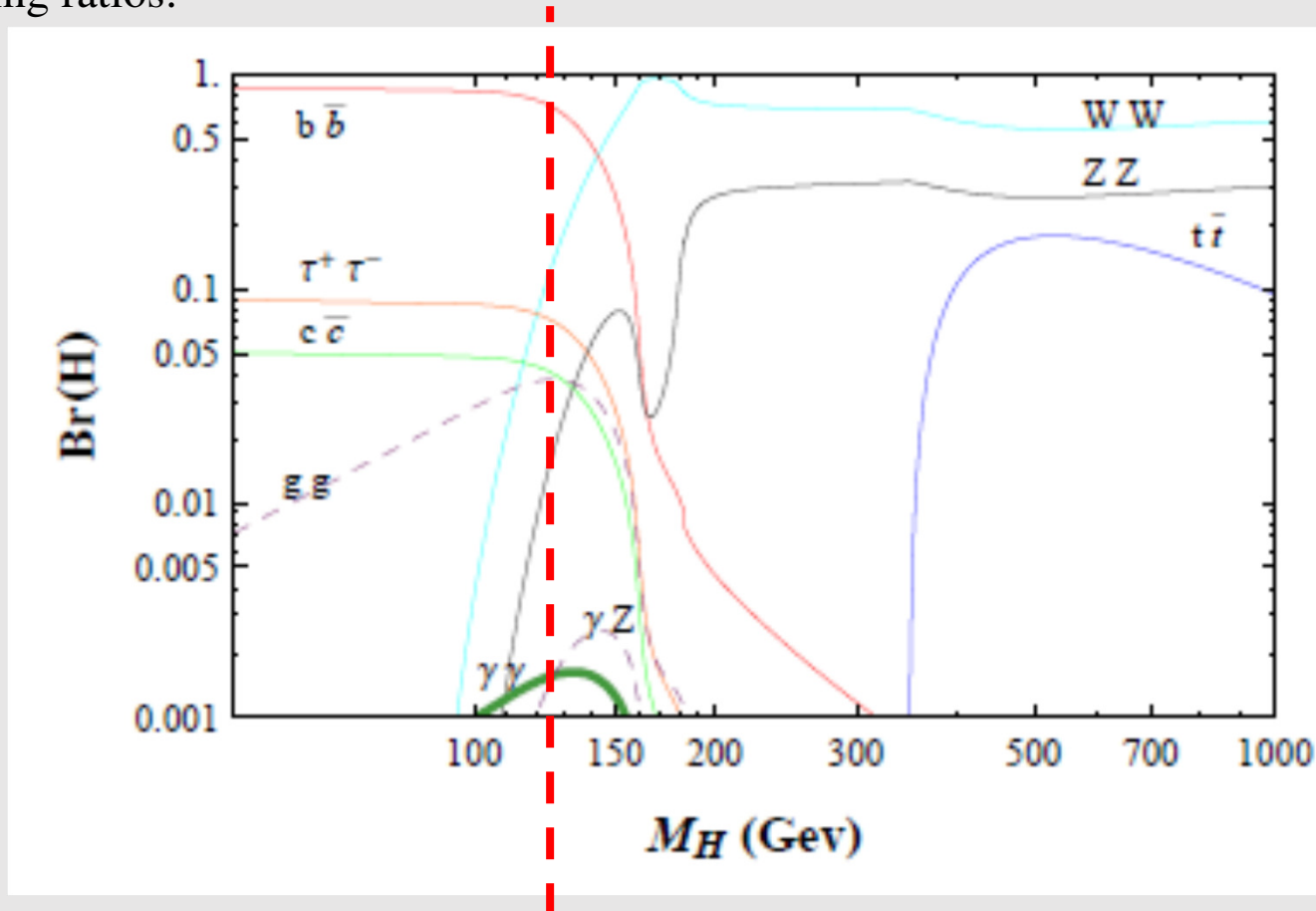
$H$  decays entirely determined by Higgs mass:



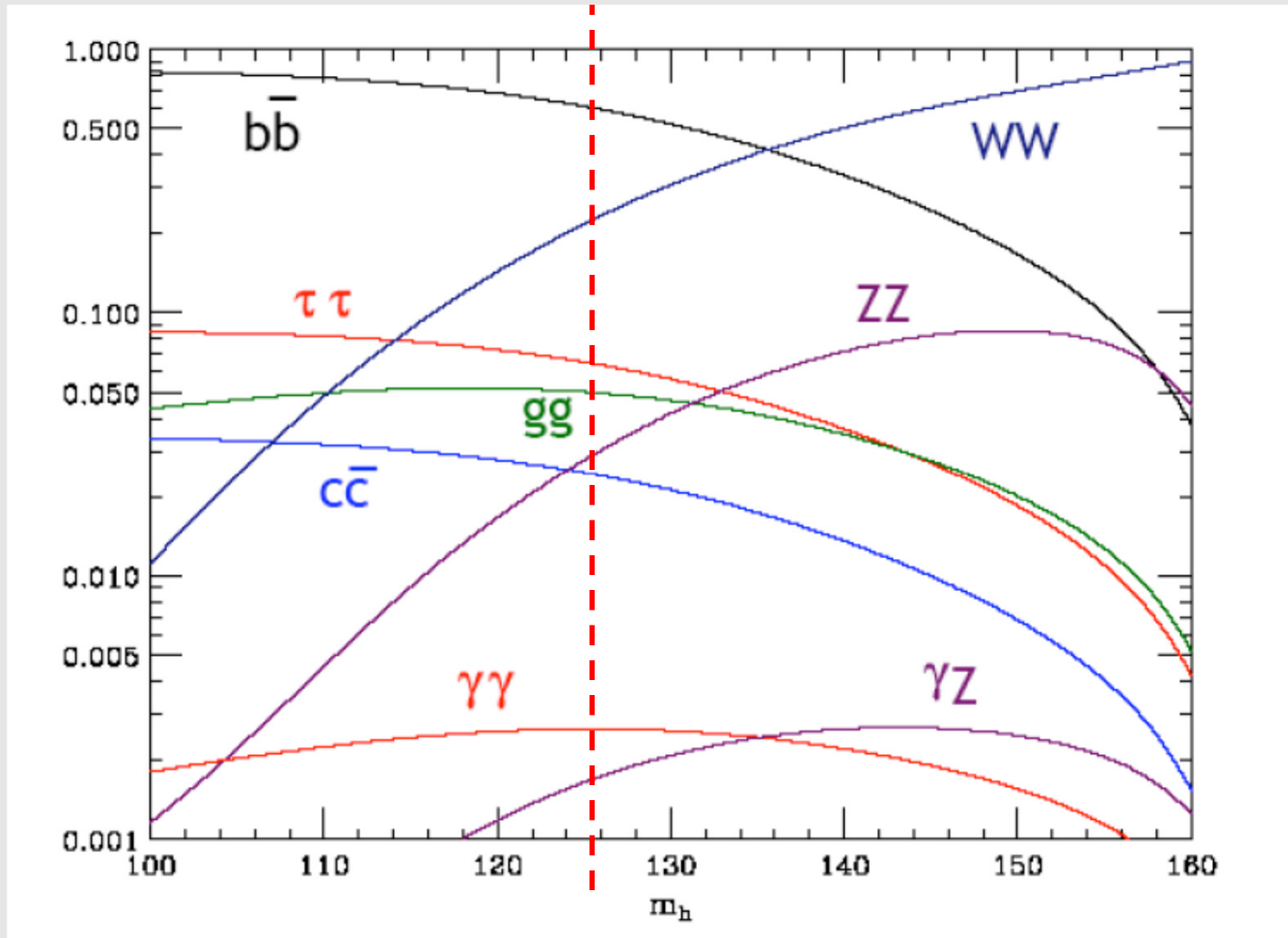


# Higgs Decays - VI

$H$  branching ratios:



# Higgs Decays - VII



# Lepton Collider - I

Leptons: Easier to handle

Taking lifetime into account: Restrict to electron, muon (?)

Linear vs. Circular

$s$  – channel formation:

Not feasible at  $e^-e^+$  colliders:

Factor  $\frac{m_e^2}{M_W^2} \sim 4 \cdot 10^{-11} \rightarrow$  Tiny cross section

Better chance for a  $\mu^-\mu^+$  collider

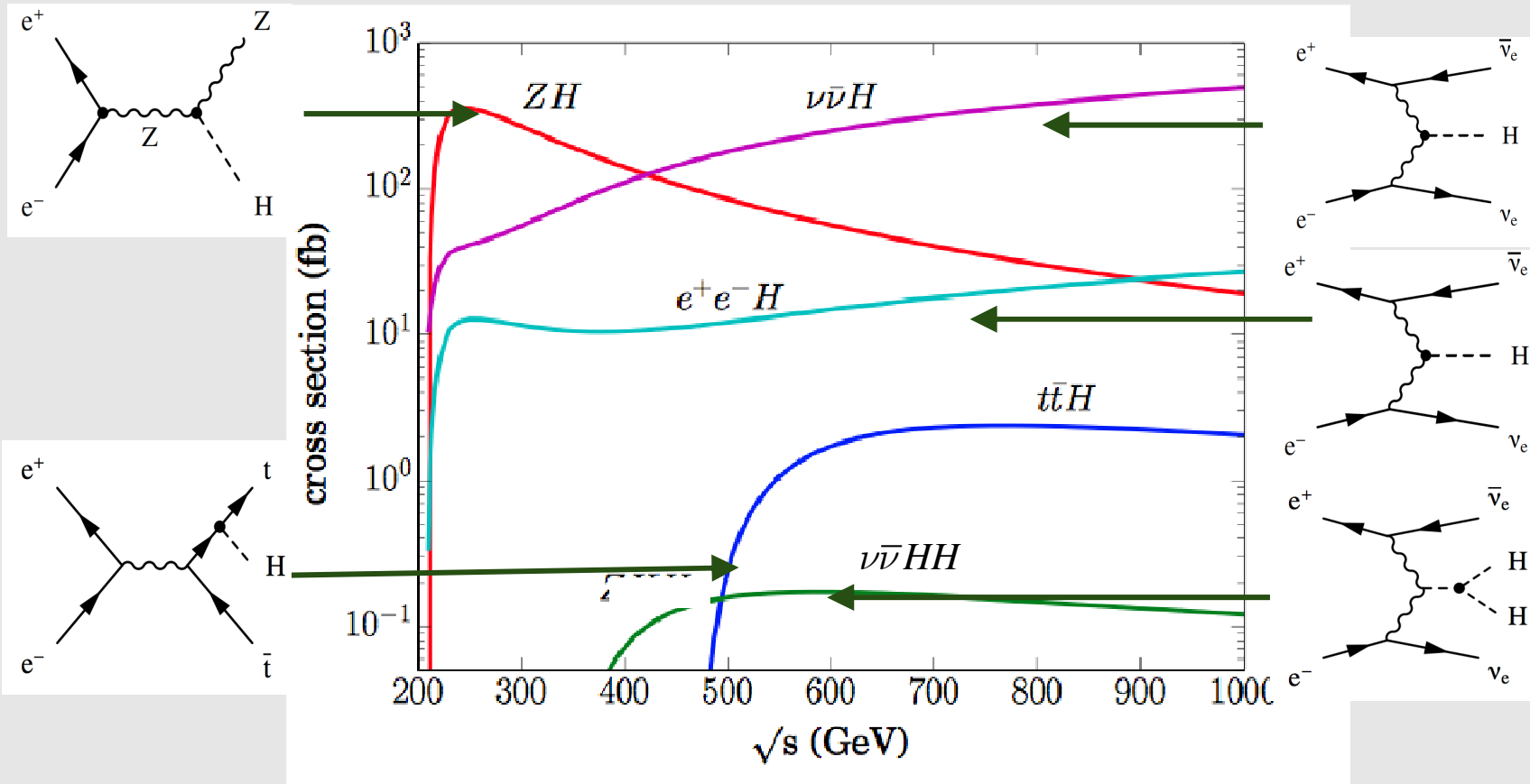
$\frac{m_\mu^2}{M_W^2} \sim 1.6 \cdot 10^{-6}$

Other channels more promising

# Lepton Collider - II

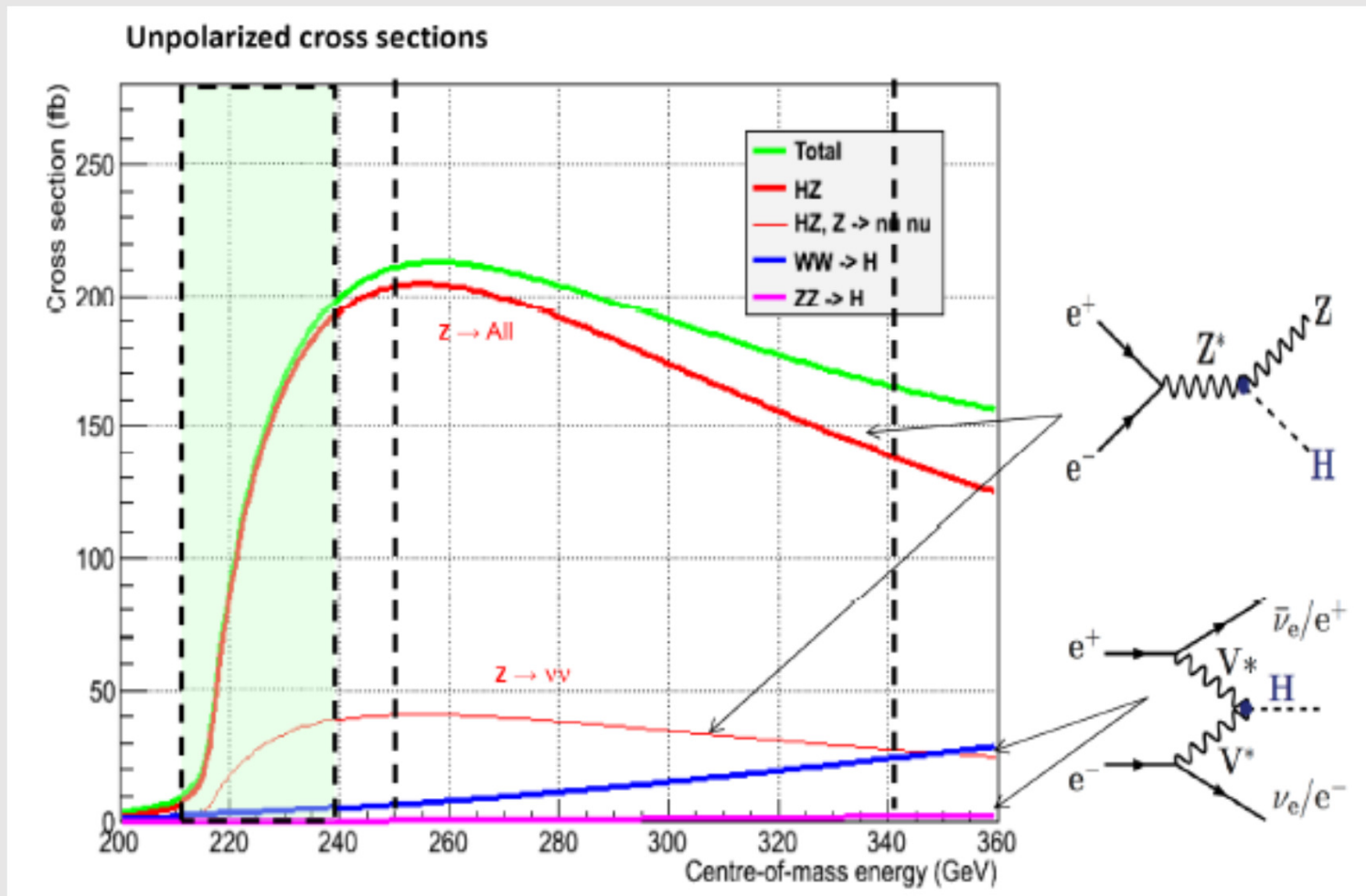
Electron collider: Tree level contributing diagrams

Higgs width



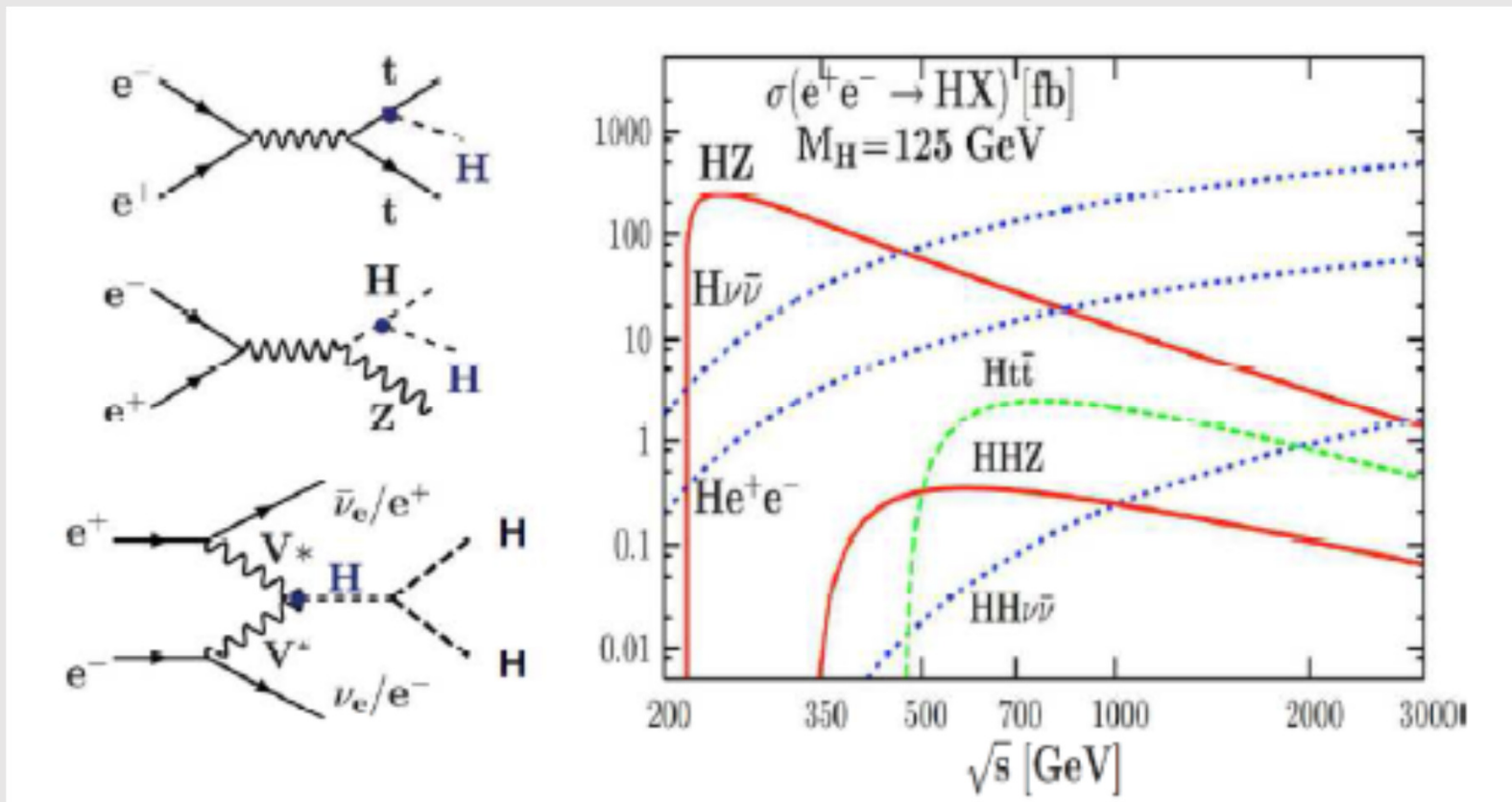
# Lepton Collider - III

Electron collider: 'Low energy' option



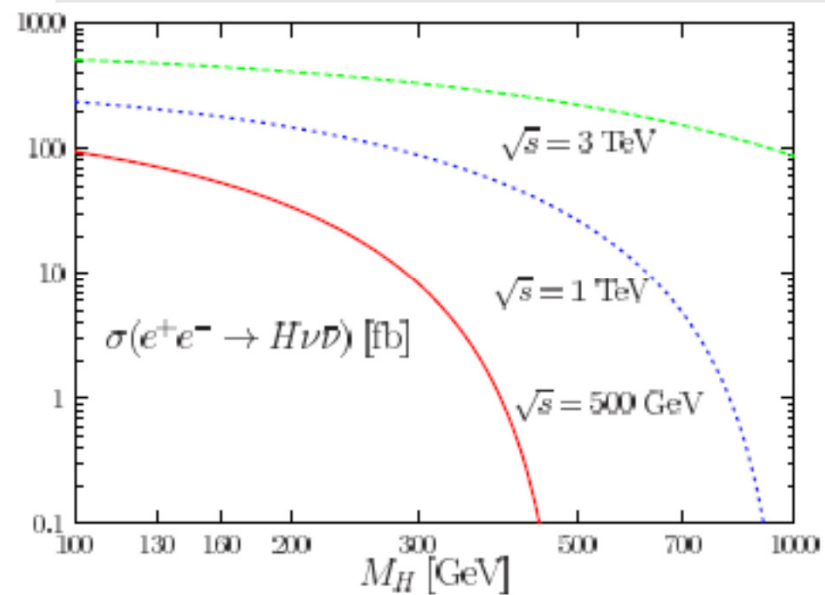
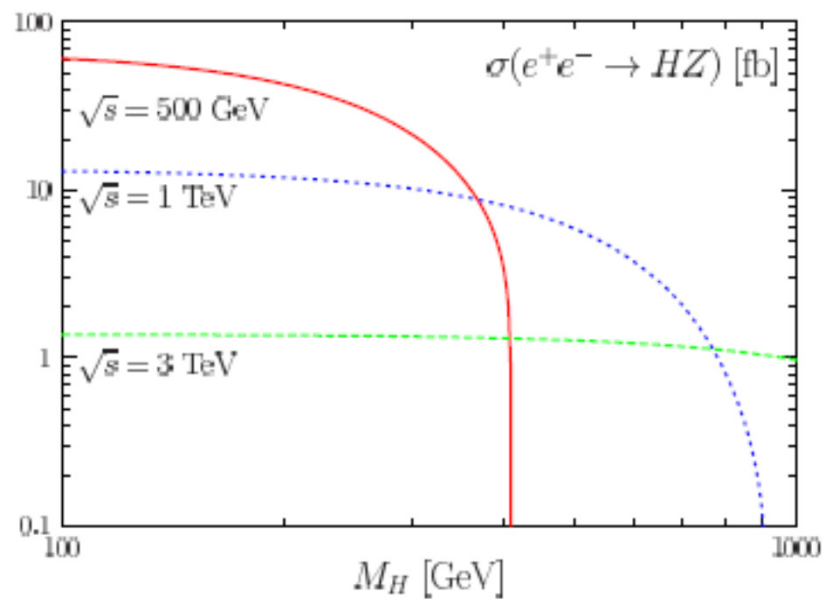
# Lepton Collider - IV

Electron collider: 'High energy' option



# Lepton Collider - V

$m_H$  dependence:



# Lepton Collider - VI

$\sqrt{s}$ (GeV)	$\langle L \rangle (ab^{-1}/\text{year})^*$	Rate (Hz) $ee \rightarrow \text{hadrons}$	Years	Statistics
90	5.6	$2 \cdot 10^4$	1	$2 \cdot 10^{11}$ Z decays
160	1.6	25	1-2	$2 \cdot 10^7$ W pairs
240	0.5	3	5	$5 \cdot 10^5$ HZ events
350	0.13	1	5	$2 \cdot 10^5$ ttbar

\* each interaction point

- Precise measurement (0.1% to 1% ) of the Higgs Couplings
- Improve precision (statistics  $\times 10^5$  ) on the measurements of the Z parameters [  $M_Z, \Gamma_Z, R_\ell, R_b, R_c$ , Asymmetries & weak mixing angle]. Z rare decays.
- Scan W threshold ( aiming at 0.5 MeV precision). W rear decays
- Scan ttbar threshold (aiming at 10 MeV)



# Lepton Collider - VII

Circular collider: Two main issues, among many

**Bending field:** Must keep the beam on orbit

$$\text{Orbit radius: } R = \frac{3.3p}{B} \quad m, GeV, T$$

First look:

Either low  $B$ , large  $R$  or high  $B$ , small  $R$

**RF power:** Must provide energy to beam up to max. energy

(also compensating for synchrotron radiation loss)

Ex: LEP I

$$B = \frac{3.3 \cdot 45}{4300} \approx 0.034 \text{ T}$$

128 2 m cavities

Typical cavity max field:  $1.5 \text{ MV} / \text{m}$

Typical beam current:  $6+6 \text{ mA}$

→ Max. energy gain  $\sim 128 \cdot 3 \sim 375 \text{ MeV} / \text{turn}$ ; RF max power  $\sim 125 \text{ kW} / \text{cavity}$

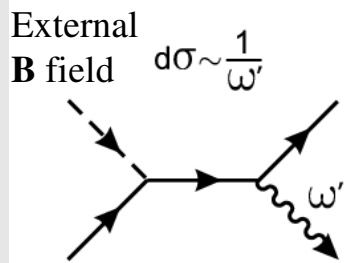
# Lepton Collider - VIII

Another crucial point: Minimize *synchrotron radiation* loss

Process related to EM interaction of ultrarelativistic charged particles moving in a **B** field:

Similar to Bremsstrahlung

Energy loss per particle, per turn:



$$\Delta E (KeV) = \frac{e^2 \gamma^4}{3\epsilon_0 R} = \begin{cases} 88.5 \frac{E (GeV)^4}{R (m)} & \text{Electrons} \\ 6.03 \frac{E (TeV)^4}{R (m)} & \text{Protons} \end{cases}$$

Critical energy:

$$\epsilon_c = 3hc\gamma^3 / (2R)$$

$$\epsilon_c (keV) = 2.218 E^3 (GeV) / R (m)$$

Ex: LEP II

$$E = 104 GeV \rightarrow \epsilon_c \sim 580 keV$$

Power loss by a beam current  $I_b$ , to be restored by RF:

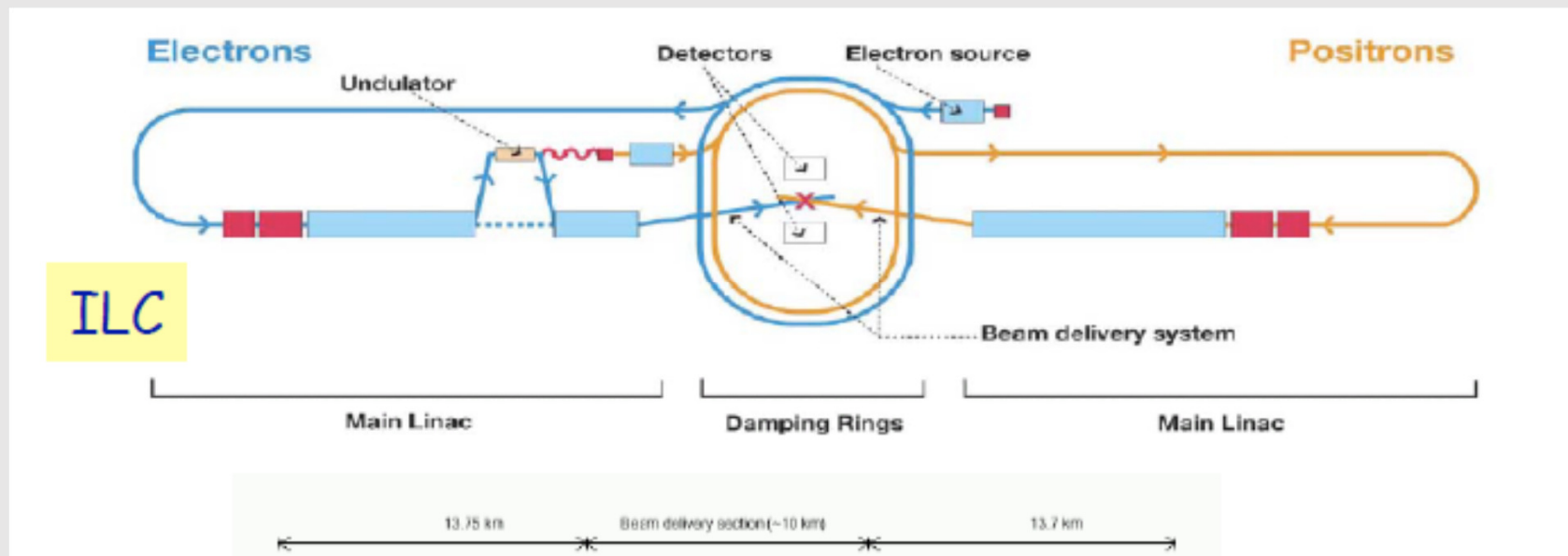
$$P (kW) = \frac{e\gamma^4}{3\epsilon_0 R} I_b = \begin{cases} 88.5 \frac{E (GeV)^4}{R (m)} I_b (A) & \text{Electrons} \\ 6.03 \frac{E (TeV)^4}{R (m)} I_b (A) & \text{Protons} \end{cases}$$

→ Pointing to large  $R$  → low  $B$

# Lepton Collider - IX

Electron collider: Linear

International Linear Collider (Japan?)

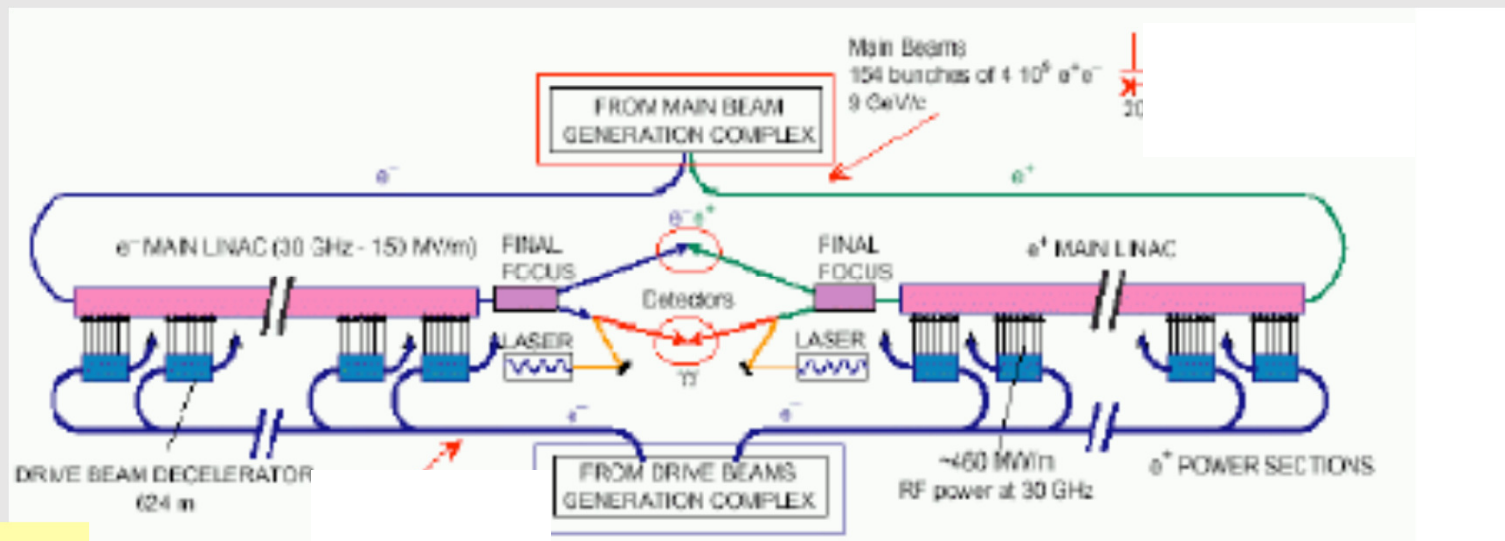


- Superconducting RF cavities
- Gradient 32 MV/m
- $\sqrt{s} \leq 500$  GeV (1 TeV upgrade option)
- $L \sim 2 \cdot 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- Focus on  $\leq 500$  GeV, physics studies also for 1 TeV
- Length  $\sim 31$  km (500 GeV)

# Lepton Collider - X

Electron collider: Linear

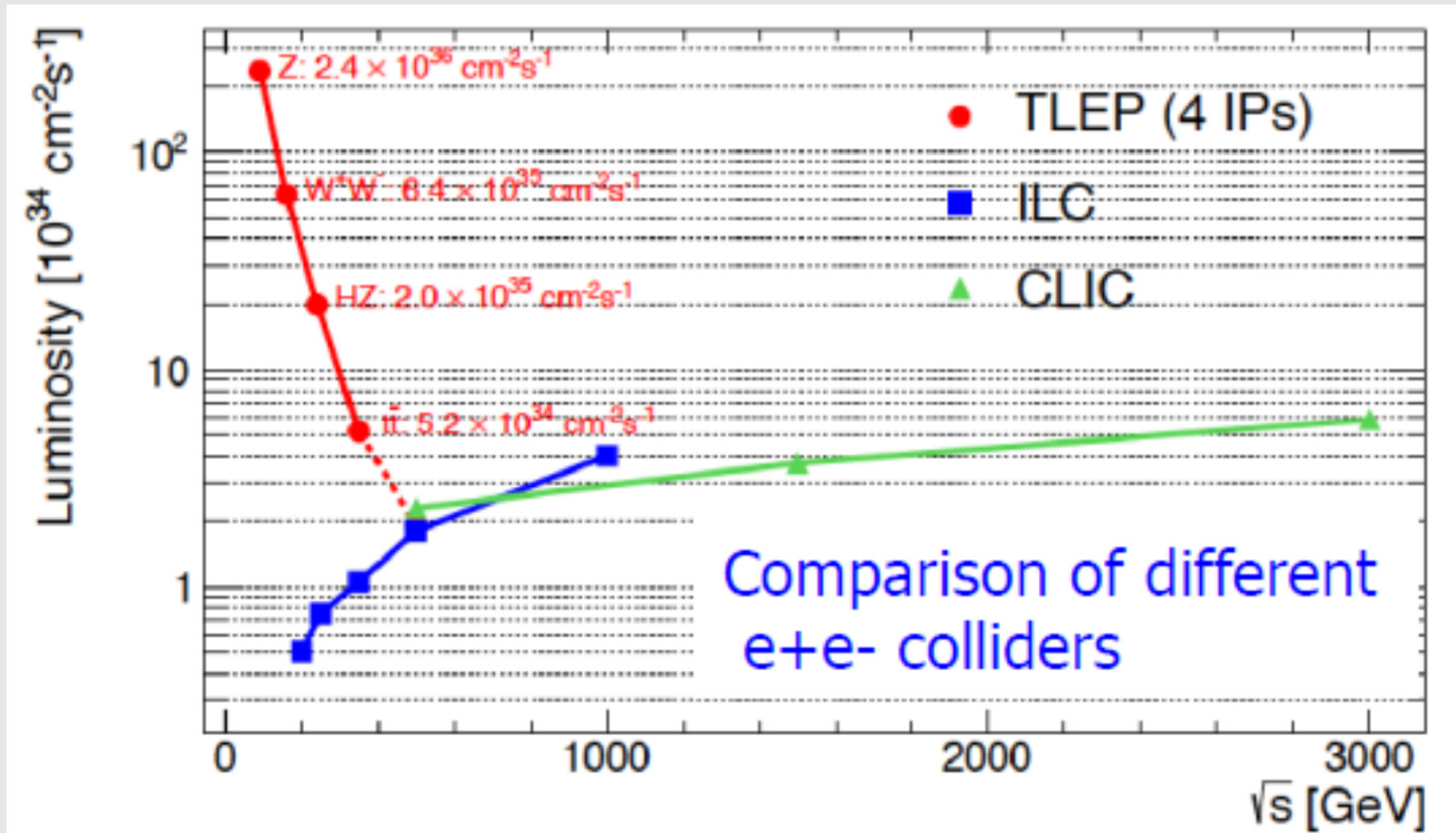
Compact Linear Collider (CERN?)



CLIC

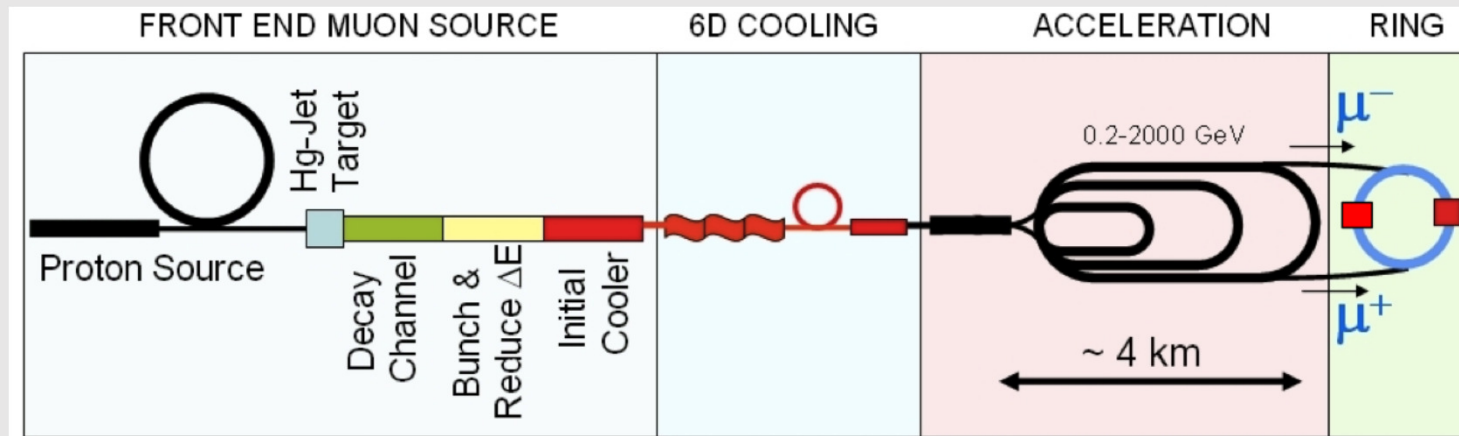
- Copper RF cavities
- Gradient 150 MV/m (!)
- $\sqrt{s} = 3 \text{ TeV}$
- $L \sim 6 \cdot 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- Length  $\sim 41 \text{ km}$  (500 GeV)

# Lepton Collider - XI



# Lepton Collider - XII

Muon collider: Overall layout



Critical points:

– Proton LINAC+Booster (4 MW)

$$16 \text{ GeV} \times 1.5 \cdot 10^{15} \text{ pps} = 16 \text{ GeV} \times 250 \mu\text{A} = 4 \text{ MW} !$$

– Cooling (fast, large)

Ionization:  $dE / dx$  reducing both  $p_{\parallel}$  and  $p_{\perp}$

RF restoring  $p_{\parallel} \rightarrow \frac{p_{\perp}}{p_{\parallel}}$  reduced

# Lepton Collider - XIII

Muon collider

Pros:

Large  $H$  cross section in the  $s$ -channel ( $\sigma_{\mu\mu} \approx 4 \cdot 10^4 \sigma_{ee}$ )  $E$

Best energy resolution ('*Beamstrahlung*' strongly suppressed)

→ Unique feature: Can perform full scan of lineshape

Main requirements:

$$\text{Energy resolution: } \begin{cases} E = \frac{m_H}{2} \simeq 63 \text{ GeV} \\ \sigma_E \leq \Gamma_H = 4.2 \text{ MeV} \end{cases} \rightarrow R = \frac{\sigma_E}{E} \leq 5 \cdot 10^{-5}$$

Feasible, but  $L \sim 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$

→ 1 y data taking  $\sim 10^{38} \text{ cm}^2 = 100 \text{ pb}^{-1}$

→  $N_H \sim 2000 \text{ y}^{-1}$

→  $\sigma_M \sim 100 \text{ keV}, \sigma_\Gamma \sim 200 \text{ keV}, \sigma_{\mu \text{ coupling}}$  to 3% in 1 year

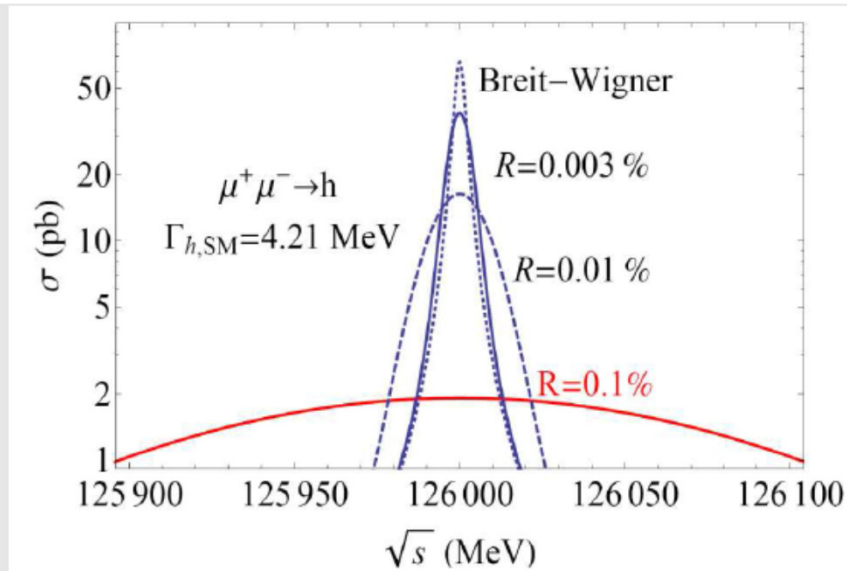
# Lepton Collider - XIV

Breit-Wigner/Gaussian convolution:

$$\sigma(\mu^+\mu^- \rightarrow h \rightarrow X) = \frac{4\pi\Gamma_h^2 \text{Br}(h \rightarrow \mu^+\mu^-) \text{Br}(h \rightarrow X)}{(\hat{s} - m_h^2)^2 + \Gamma_h^2 m_h^2}.$$

$$\sigma_{\text{eff}}(s) = \int d\sqrt{\hat{s}} \frac{dL(\sqrt{\hat{s}})}{d\sqrt{\hat{s}}} \sigma(\mu^+\mu^- \rightarrow h \rightarrow X)$$

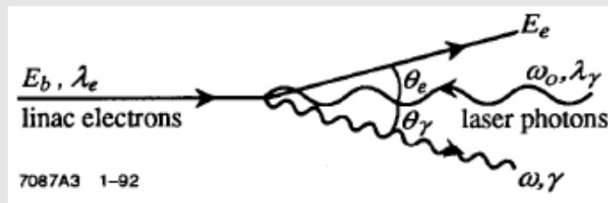
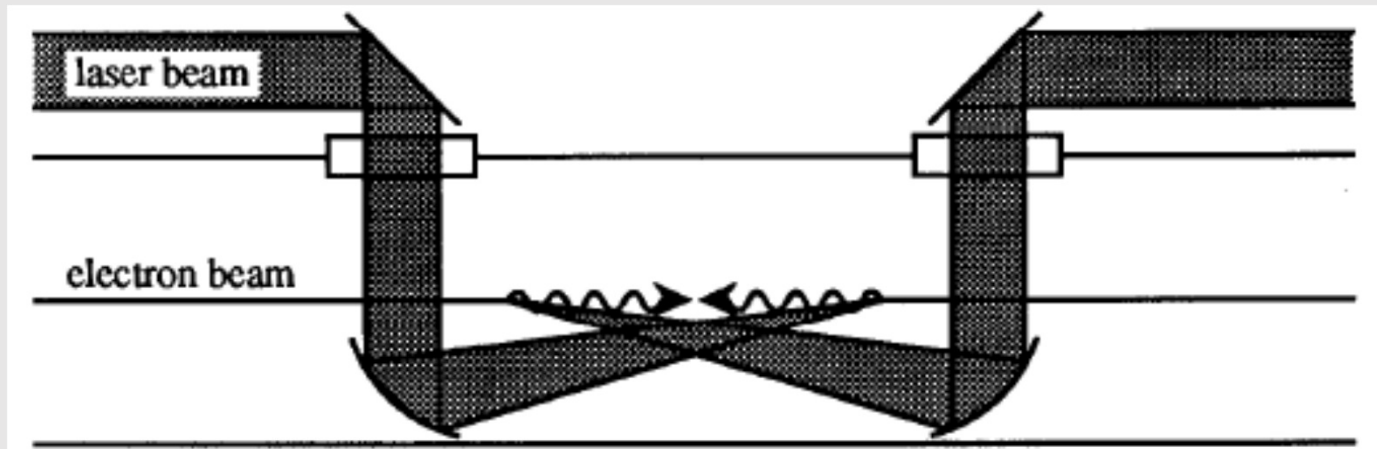
$$\propto \begin{cases} \Gamma_h^2 B / [(s - m_h^2)^2 + \Gamma_h^2 m_h^2] & (\Delta \ll \Gamma_h), \\ B \exp[-\frac{(m_h - \sqrt{s})^2}{2\Delta^2}] (\frac{\Gamma_h}{\Delta}) / m_h^2 & (\Delta \gg \Gamma_h). \end{cases}$$



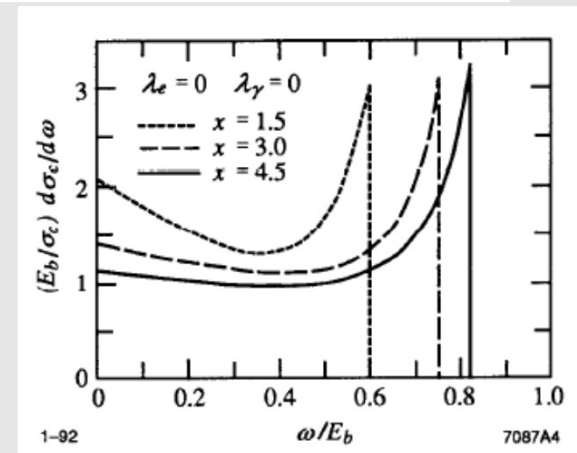


# Photon Collider - I

General idea: Compton back-scattering of intense laser beam by the  $e$  beam

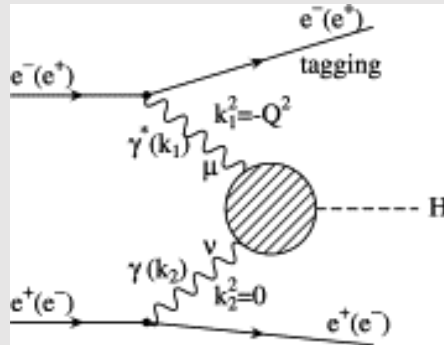


$$x = (4E_b\omega_o/m_e^2)\cos^2(\alpha/2) \approx 15.3\left(\frac{E_b}{\text{TeV}}\right)\left(\frac{\omega_o}{\text{eV}}\right)$$

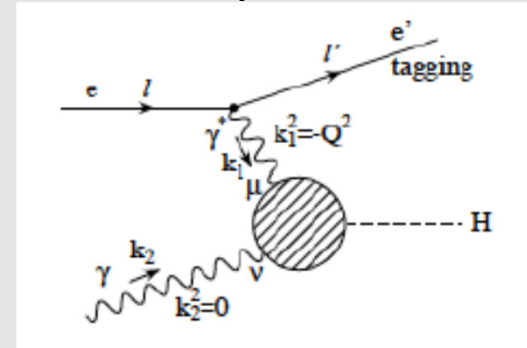


# Photon Collider - II

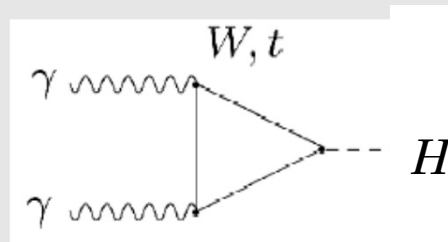
Virtual+Virtual photons



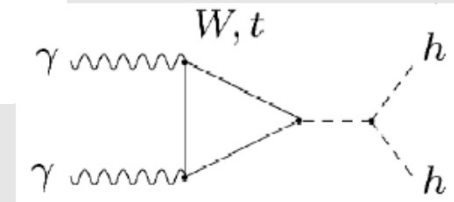
Virtual+Real photons



Most important loop diagrams for the 'blob': Dominated by largest mass fermions, gauge bosons



Making for a particularly clean study of  $H$  self-coupling



# Photon Collider - III

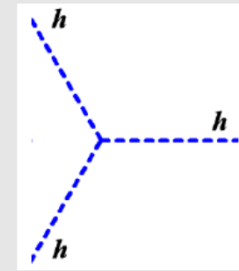
Higgs self-couplings: Very important for  $\left\{ \begin{array}{l} \text{radiative corrections to } m_h \\ \text{signs of new physics} \end{array} \right.$

Origin of 3- and 4-linear self-couplings:

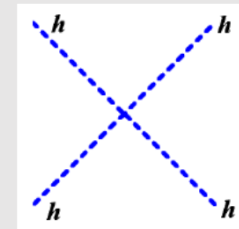
Re-writing  $L$  upon introducing shifted field, 1D example

$$\begin{aligned} \text{Kinetic term: } \mathcal{L}_{\text{kin}}(\eta) &= \frac{1}{2}(\partial_\mu(\eta + v))\partial^\mu(\eta + v) \\ &= \frac{1}{2}(\partial_\mu\eta)(\partial^\mu\eta) \end{aligned}$$

$$\begin{aligned} \text{Potential term: } V(\eta) &= +\frac{1}{2}\mu^2(\eta + v)^2 + \frac{1}{4}\lambda(\eta + v)^4 \\ &= \lambda v^2\eta^2 + \lambda v\eta^3 + \frac{1}{4}\lambda\eta^4 + \frac{1}{4}\lambda v^4 \end{aligned}$$



$$-3im_h^2\sqrt{\sqrt{2}G_F}h h h$$

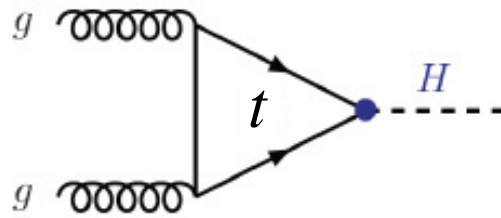


$$-3im_h^2\sqrt{2}G_F h h h h$$

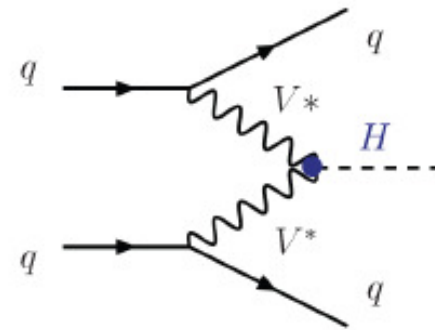
# Parton Collider - I

Dominant diagrams for  $H$  production:

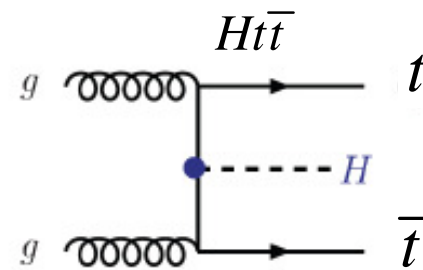
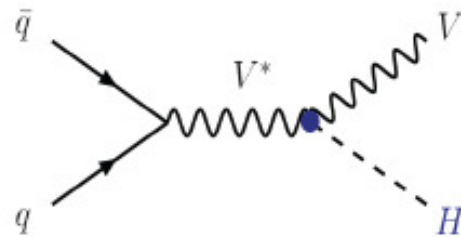
Gluon-Gluon fusion



Vector Boson fusion



Higgsstrahlung



# Parton Collider - II

Basic ingredient: PDFs

Quarks: Look for heavy ones

Tree diagrams: Best bet is with  $b$

Factor  $\frac{m_b^2}{M_W^2} \sim 3 \cdot 10^{-3}$  encouraging

But: No  $b$ -quark beams, must rely on  $b\bar{b}$  sea inside the nucleon

$b$ -quark partonic density small...

Taking  $H$  production at small rapidity  $y \sim 0$ , with a 7 TeV beam  $x \sim 10^{-2}$

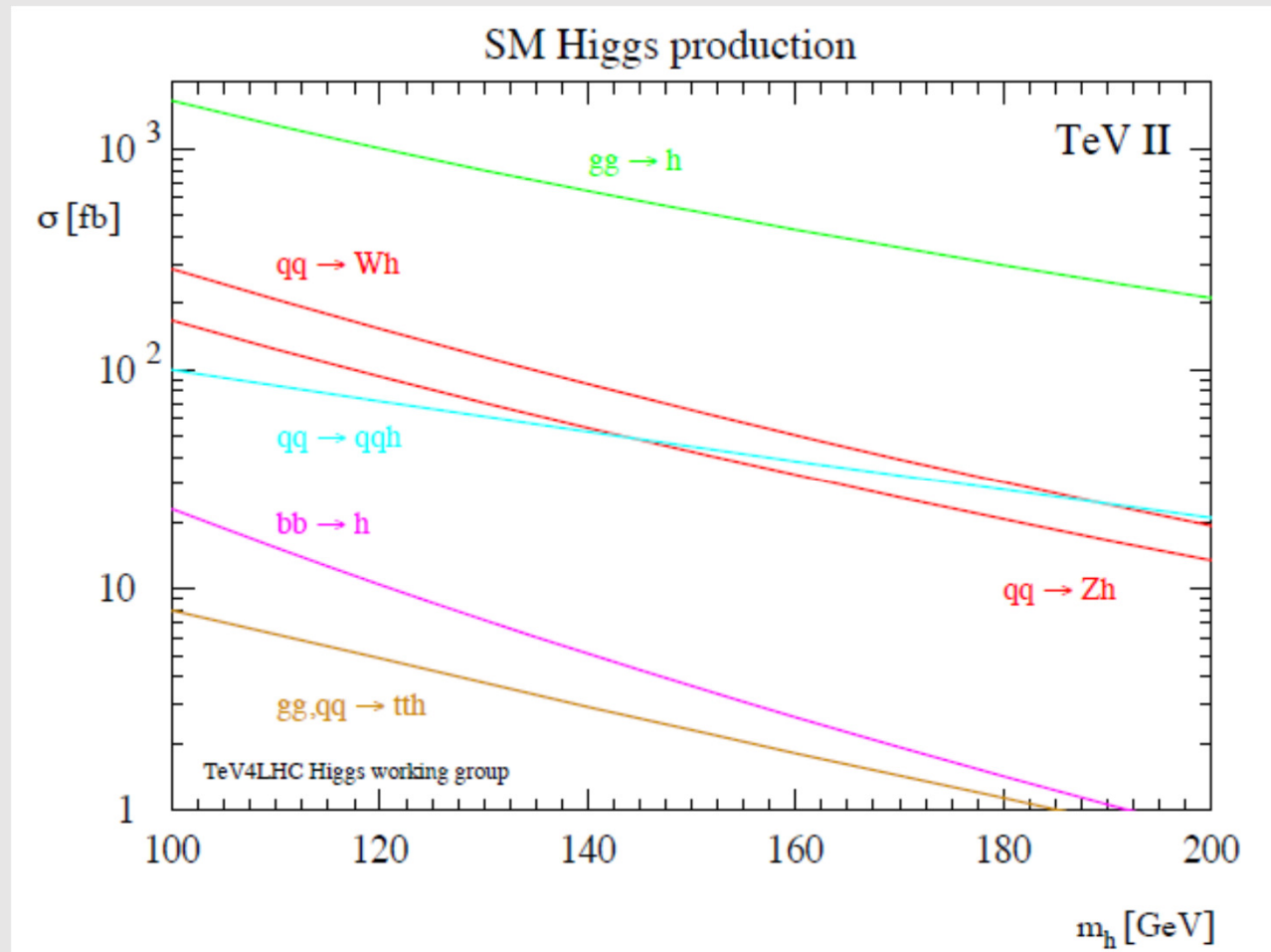
→ Incident flux of sea  $b$ -quarks very small

Gluons: Main contribution

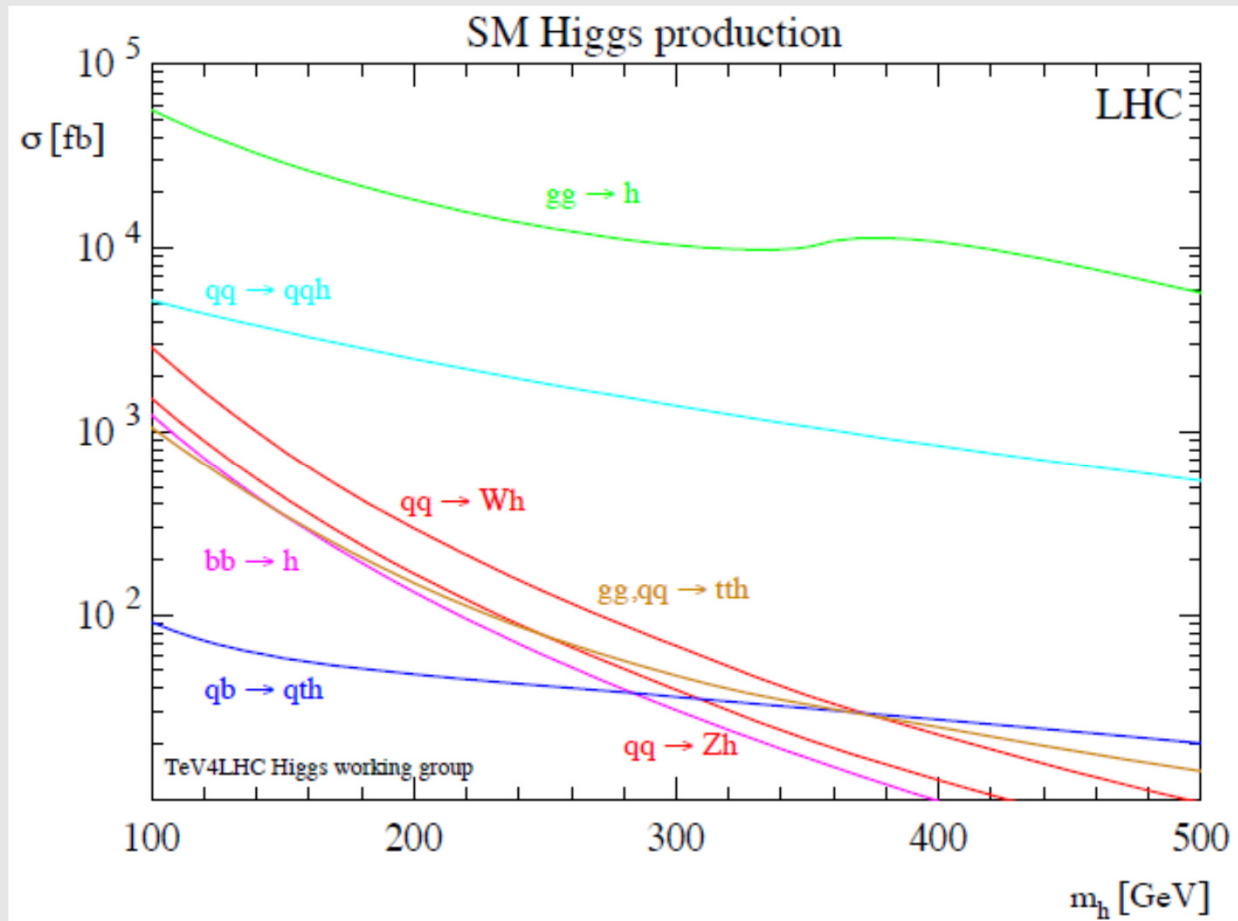
Loop diagrams, dominated by  $t$  quark

PDF somewhat dependent on  $Q^2$

# Parton Collider- III

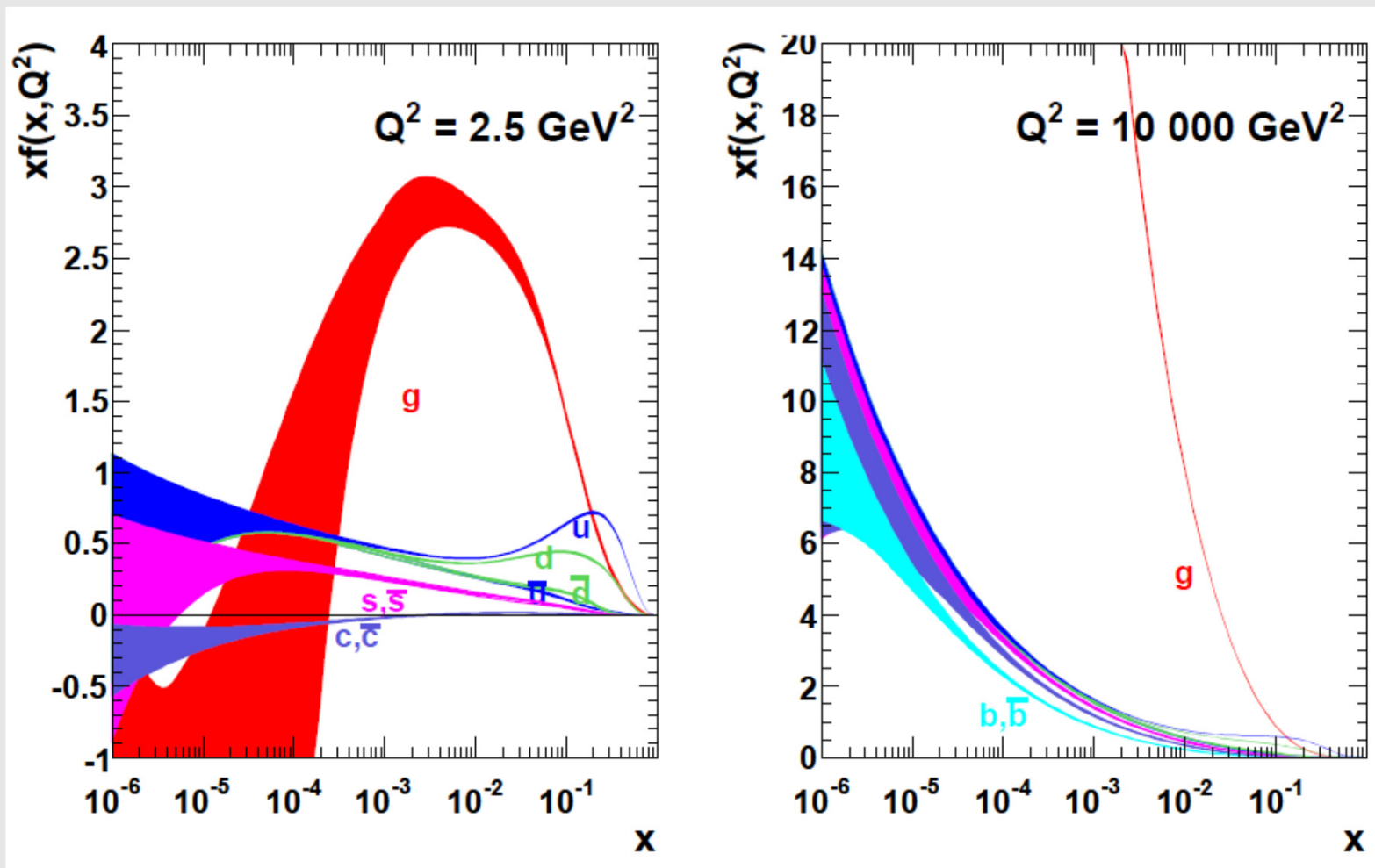


# Parton Collider- IV



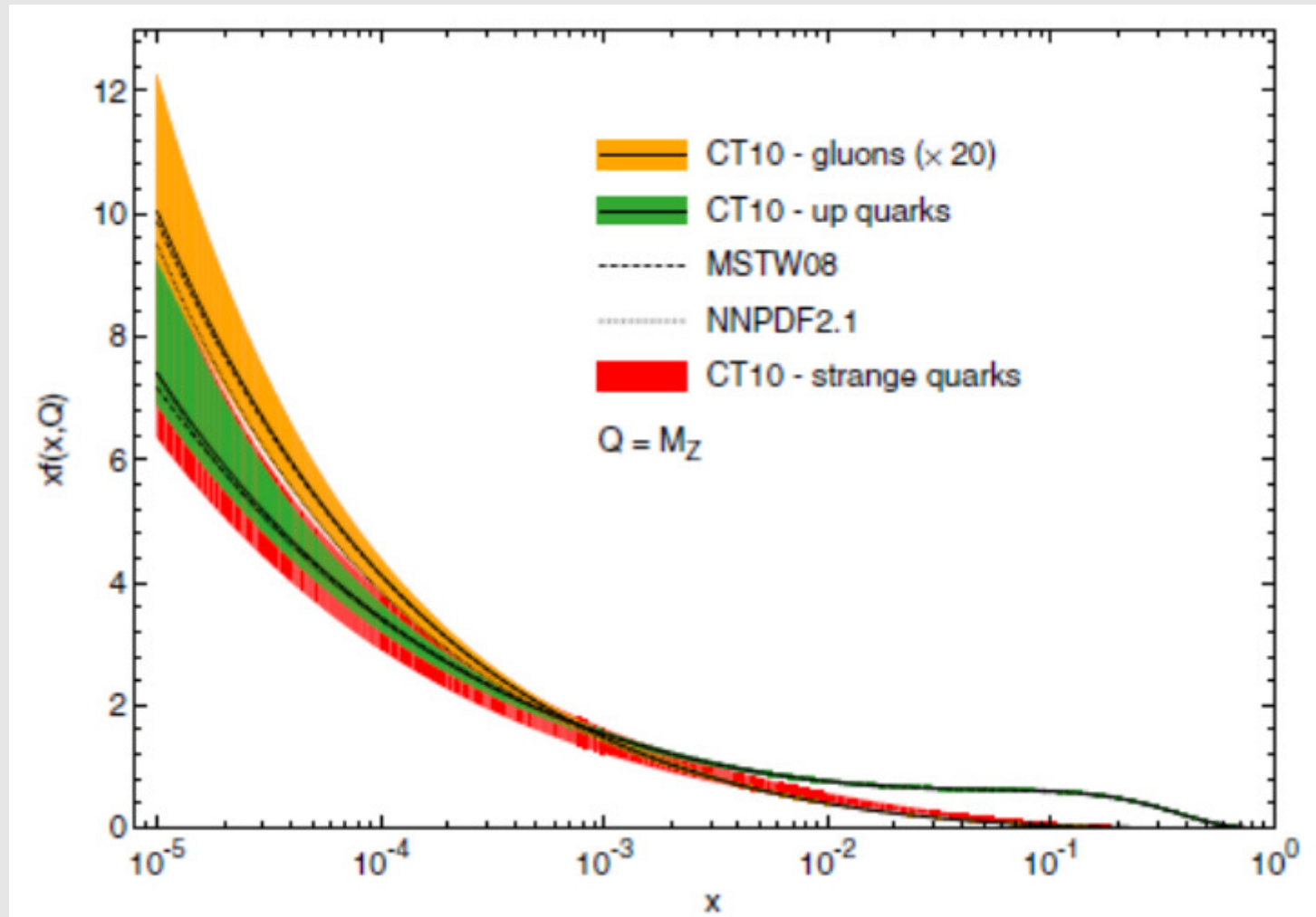
# Parton Collider - V

Parton densities:



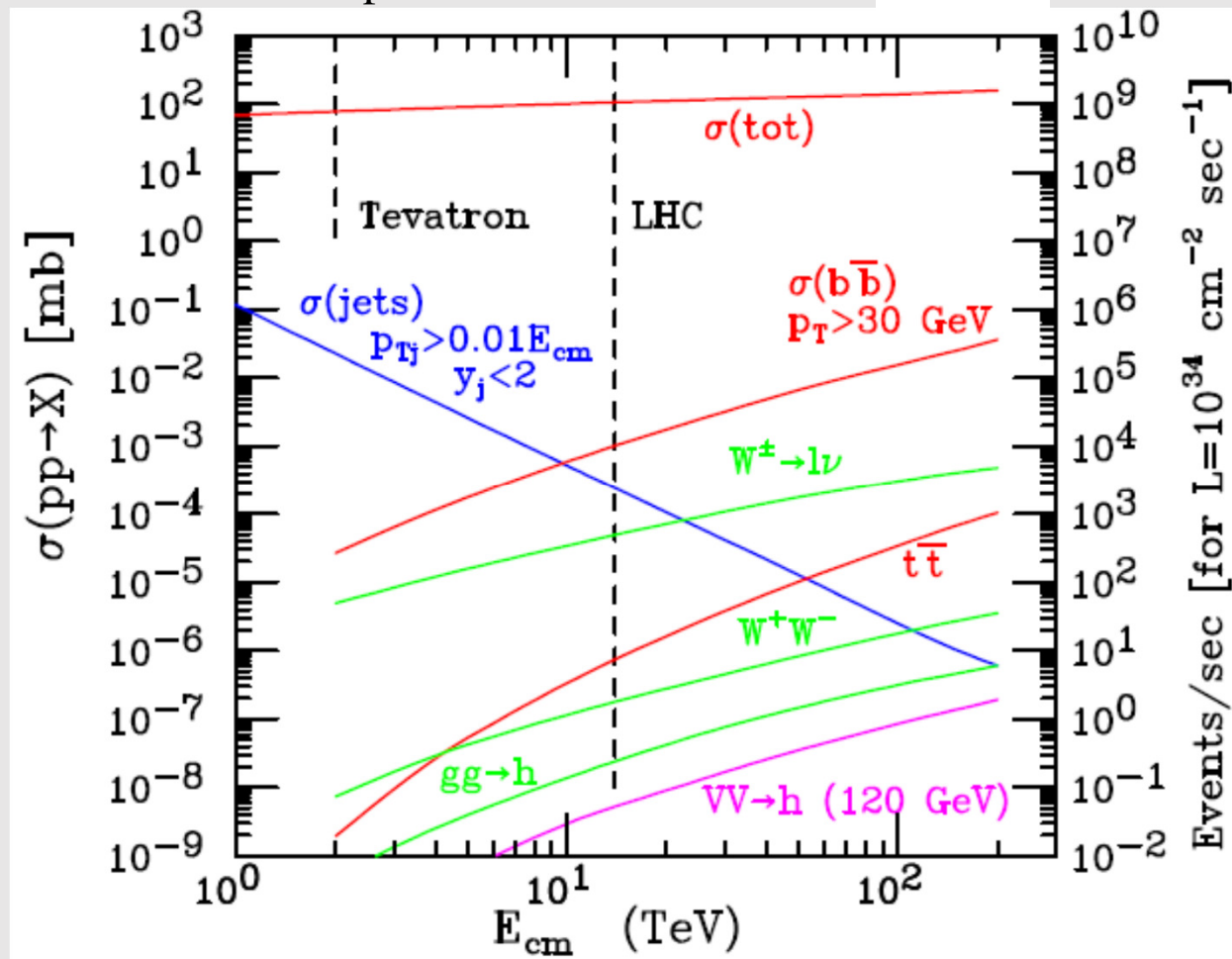


# Parton Collider - VI



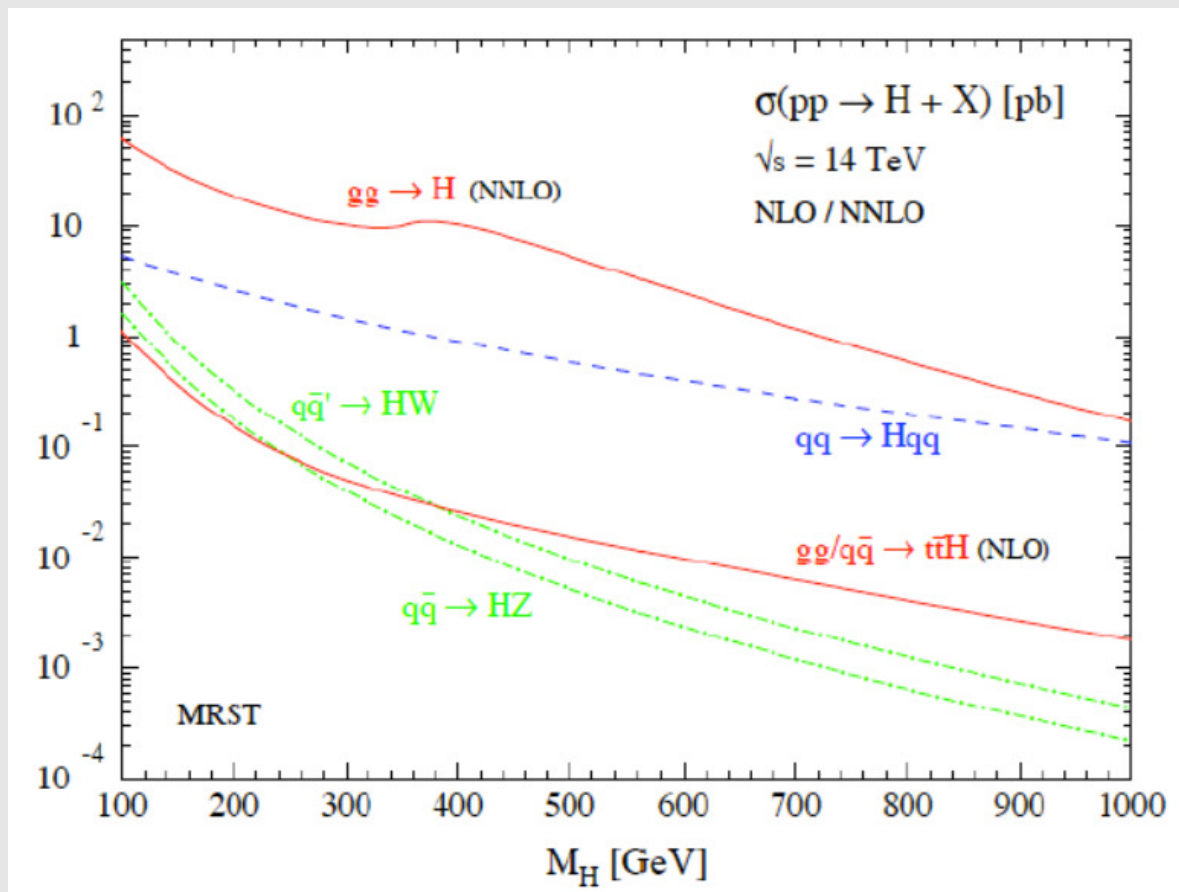
# Parton Collider - VII

Expected cross sections for parton colliders:



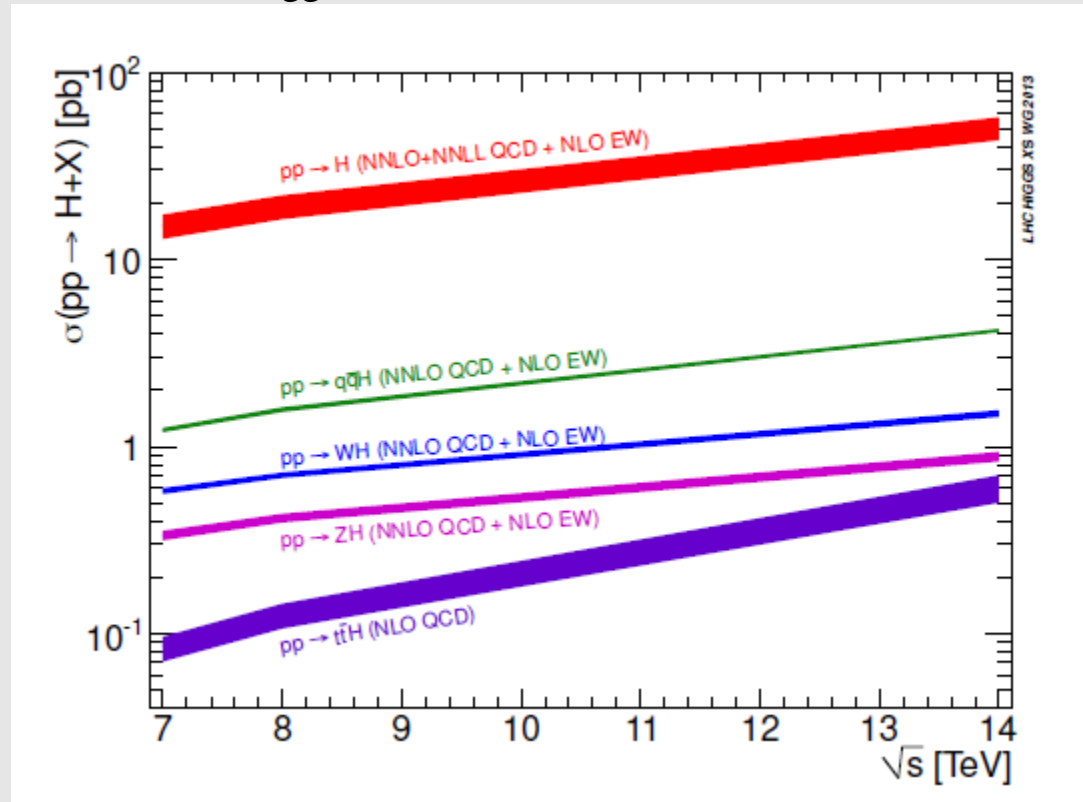
# Parton Collider - VIII

Results for LHC cross sections



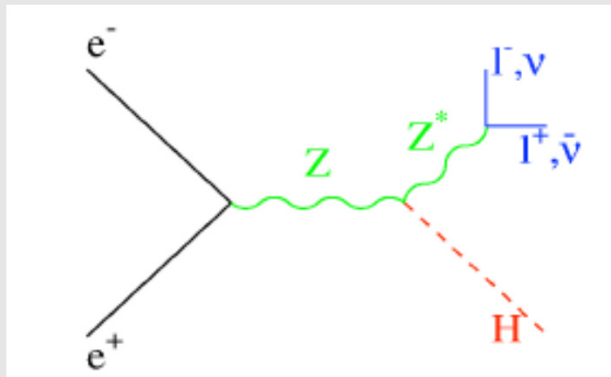
# Parton Collider - IX

Cross-sections for a 126 GeV Higgs

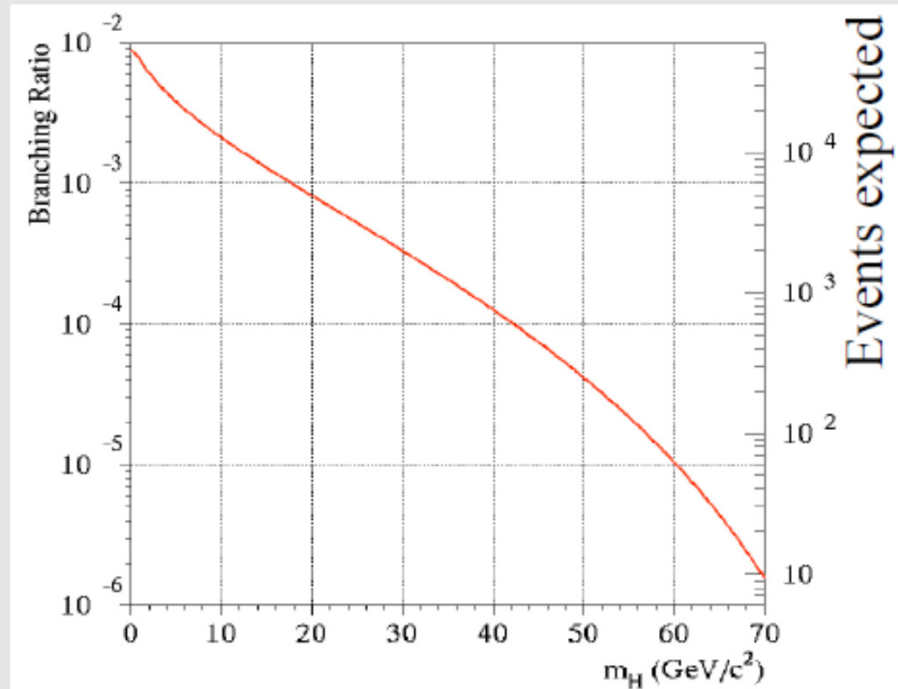


# H Searches - I

Direct searches at LEP I:  
Higgsstrahlung  
Z off-shell detected by lepton decay

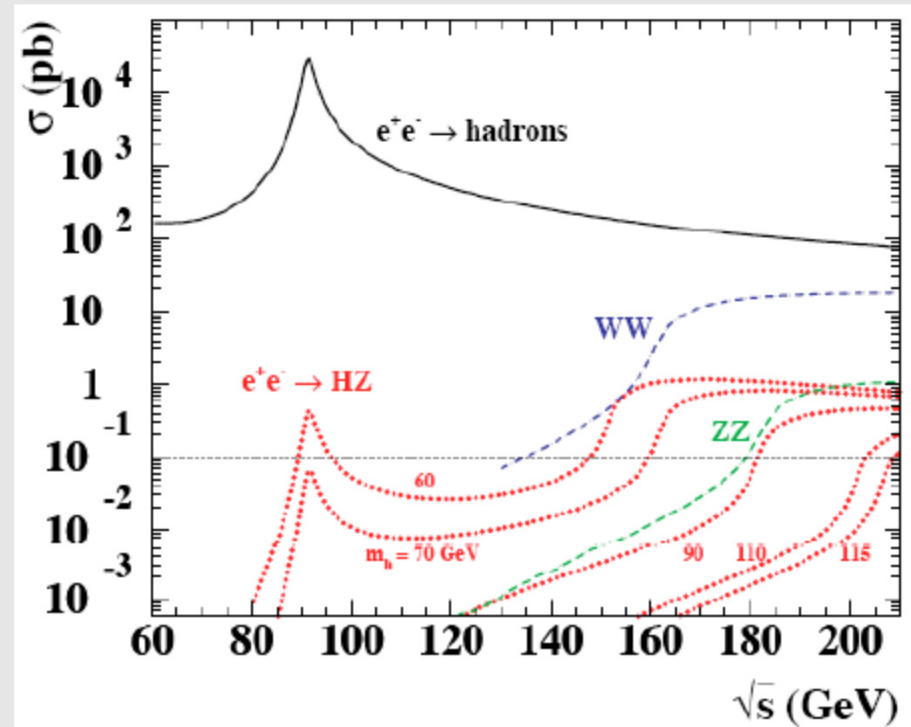
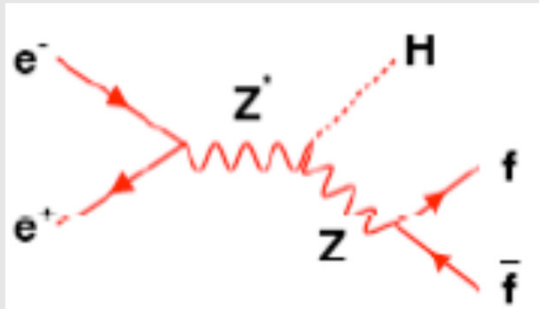


Final LEP I result:  
 $m_H < 65 \text{ GeV}$  excluded at 95% CL

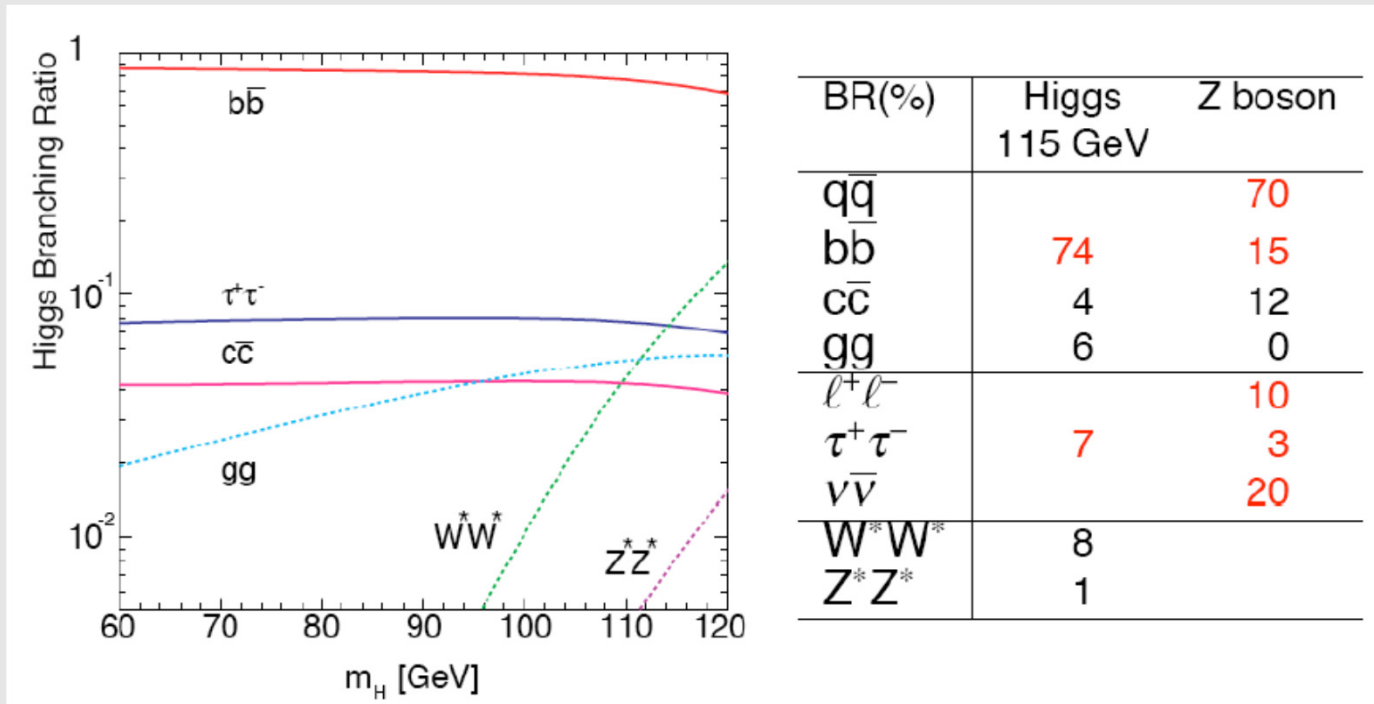


# H Searches - II

Direct searches at LEP II:  
Higgsstrahlung  
Z on-shell detected by lepton decay



# H Searches - III



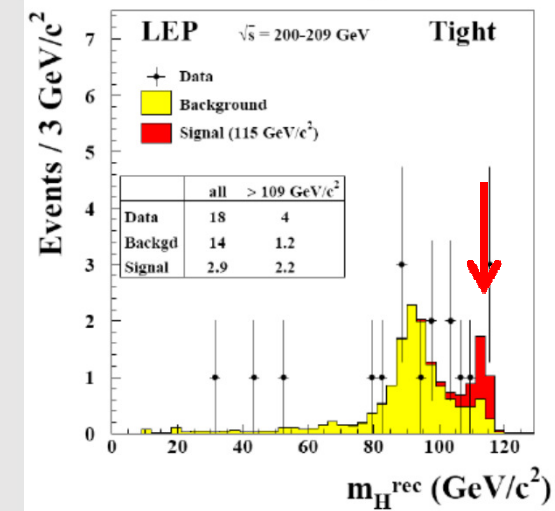
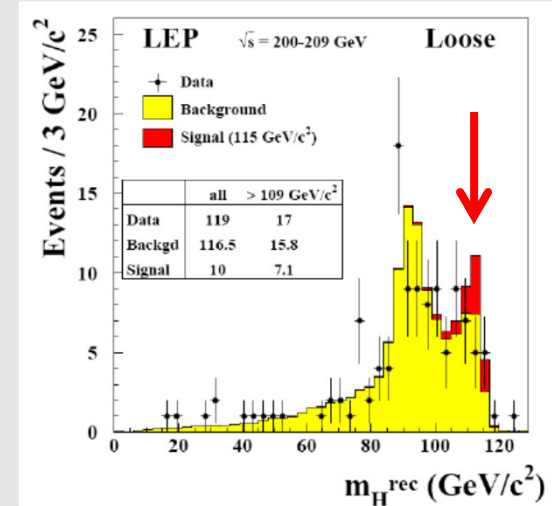
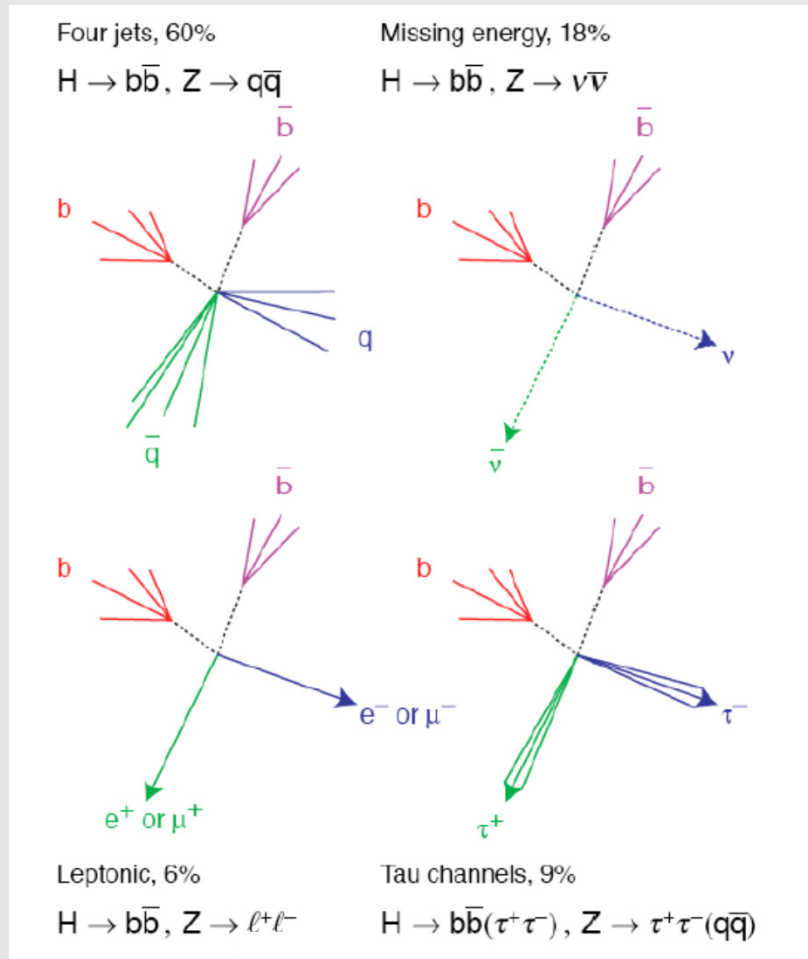
Best channel:

$$H \rightarrow b\bar{b}$$

$$Z \rightarrow q\bar{q}$$

# H Searches - IV

HZ event topologies:





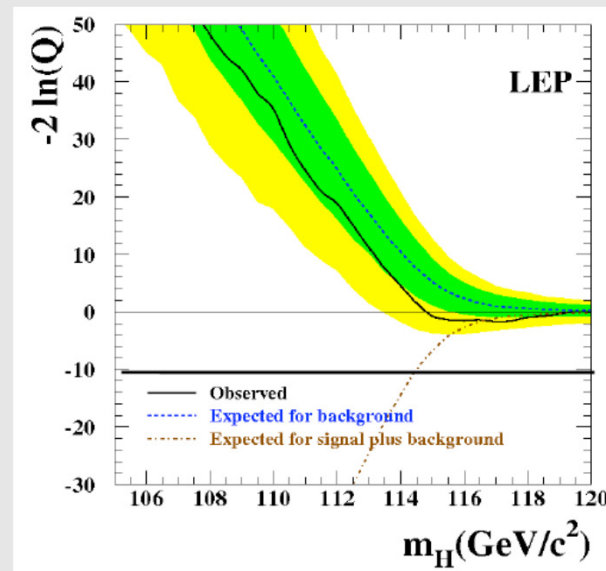
# H Searches - V

Likelihood ratio test

$$Q = \frac{L_{sign+bckg}}{L_{bckg}} \rightarrow -2 \ln Q \approx \Delta\chi^2$$

Final LEP II result:

$$m_H > 114.4 \text{ GeV at 95\% CL}$$



A false alarm:

'Signal' = Best fit

But: Excess at 115 GeV expected in 9% of cases from pure background

# *H* Searches - VI

Tevatron direct searches:

Two large experiments, CDF & D0

Among tens of channels investigated, main results from:

$$q\bar{q} \rightarrow WH \rightarrow l\nu b\bar{b}$$

$$gg \rightarrow H \rightarrow WW \rightarrow l\nu l\nu$$

Rather complex topologies, heavy use of *neural networks*  
Sophisticated, parallel logic networks capable of handling  
many parameters in order to select candidate events

Can be 'trained' by tuning selection criteria across Montecarlo samples  
of signal and background

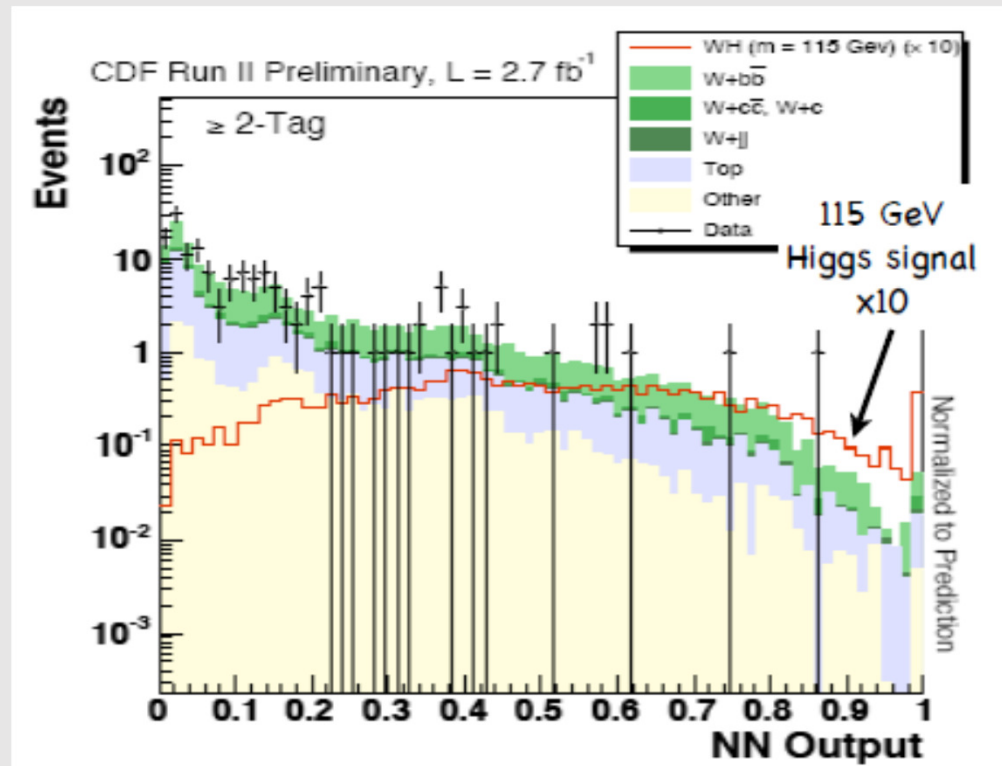
# H Searches - VII

CDF :

$$q\bar{q} \rightarrow WH \rightarrow l\nu b\bar{b}$$

Neural Network tagging

LEP 'indication' at 115 GeV: Expect 4.8 events, observe 5.6



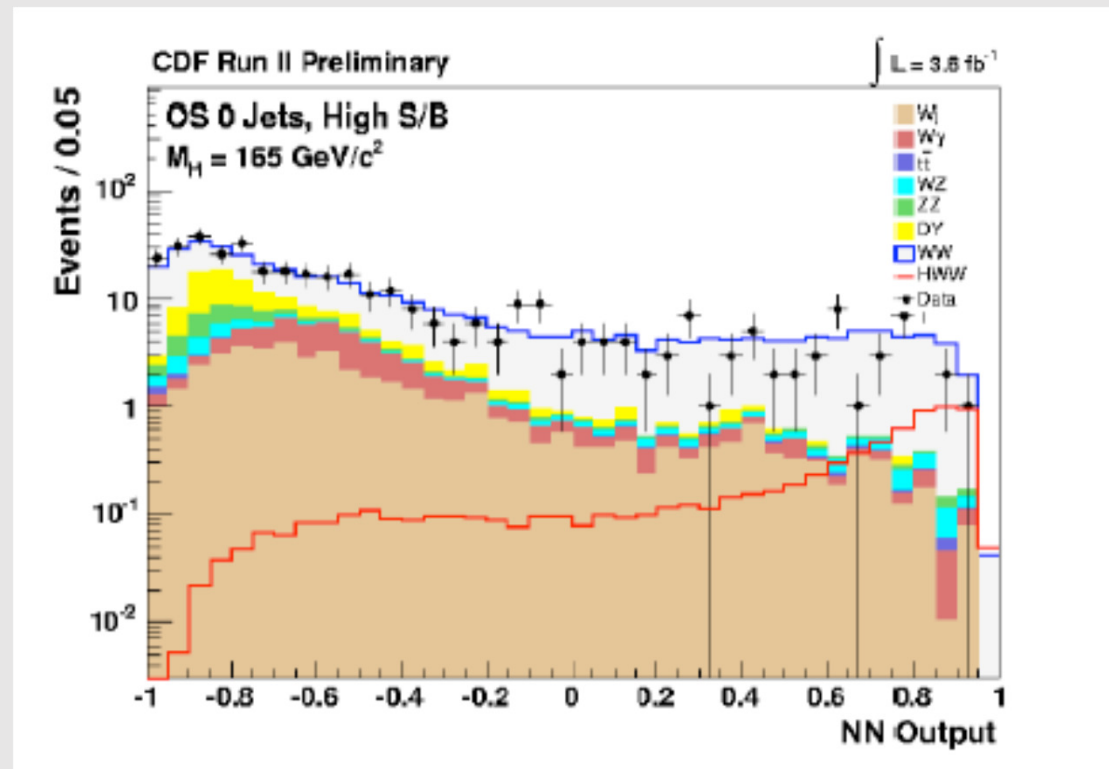
# H Searches - VIII

CDF :

$H \rightarrow WW \rightarrow l\nu l\nu$

Neural Network tagging

Consistent with  $t\bar{t}$  background

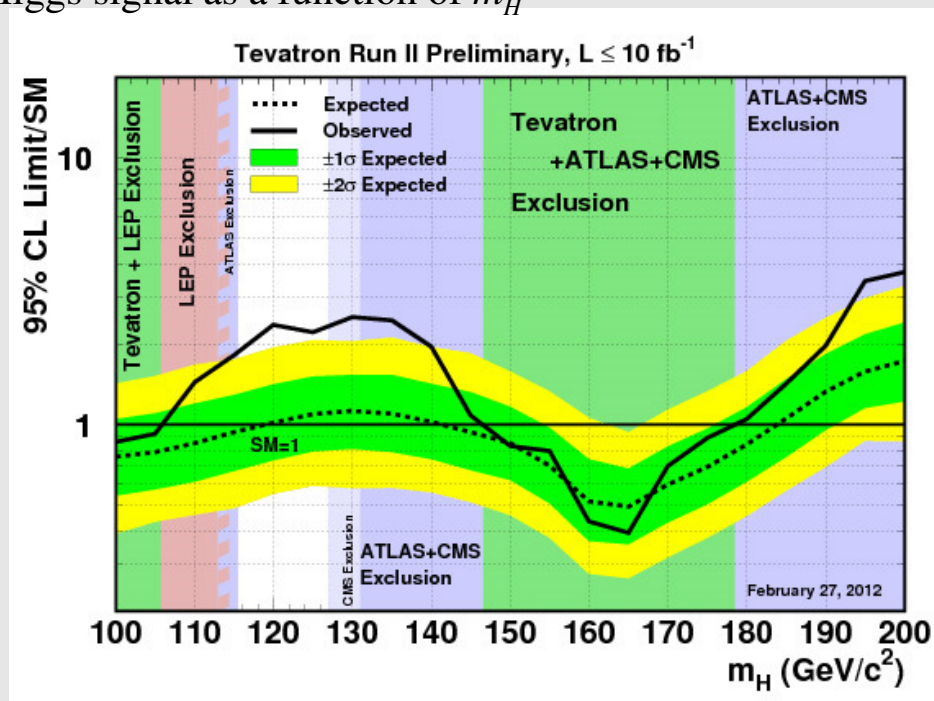


# H Searches - IX

Main Tevatron result : "Brazilian Flag" plot

Continuous line : Upper limit of (Higgs+SM Background) observed  
 Dashed line: SM Background (  $\pm 1\sigma$  ,  $\pm 2\sigma$  ) expected } vs.  $m_H$   
*Green band Yellow band*

Unit: Expected SM Higgs signal as a function of  $m_H$

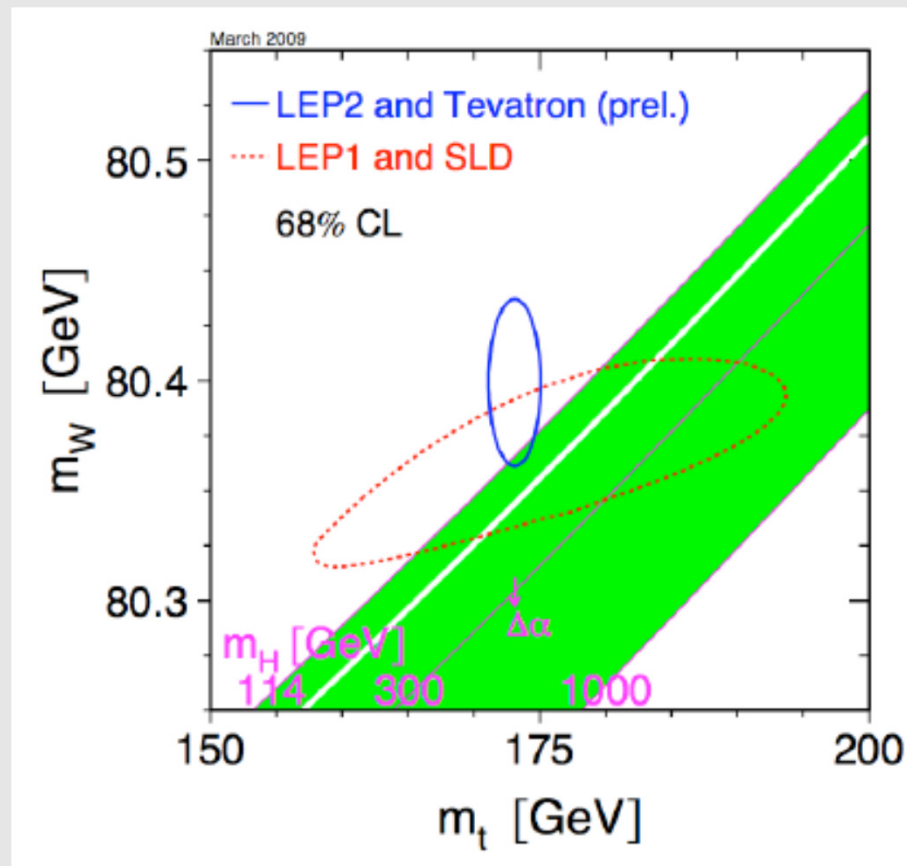


# H Searches - X

Indirect searches:

Radiative corrections to many EW observables receiving contributions  $\propto \ln m_H, m_t^2$

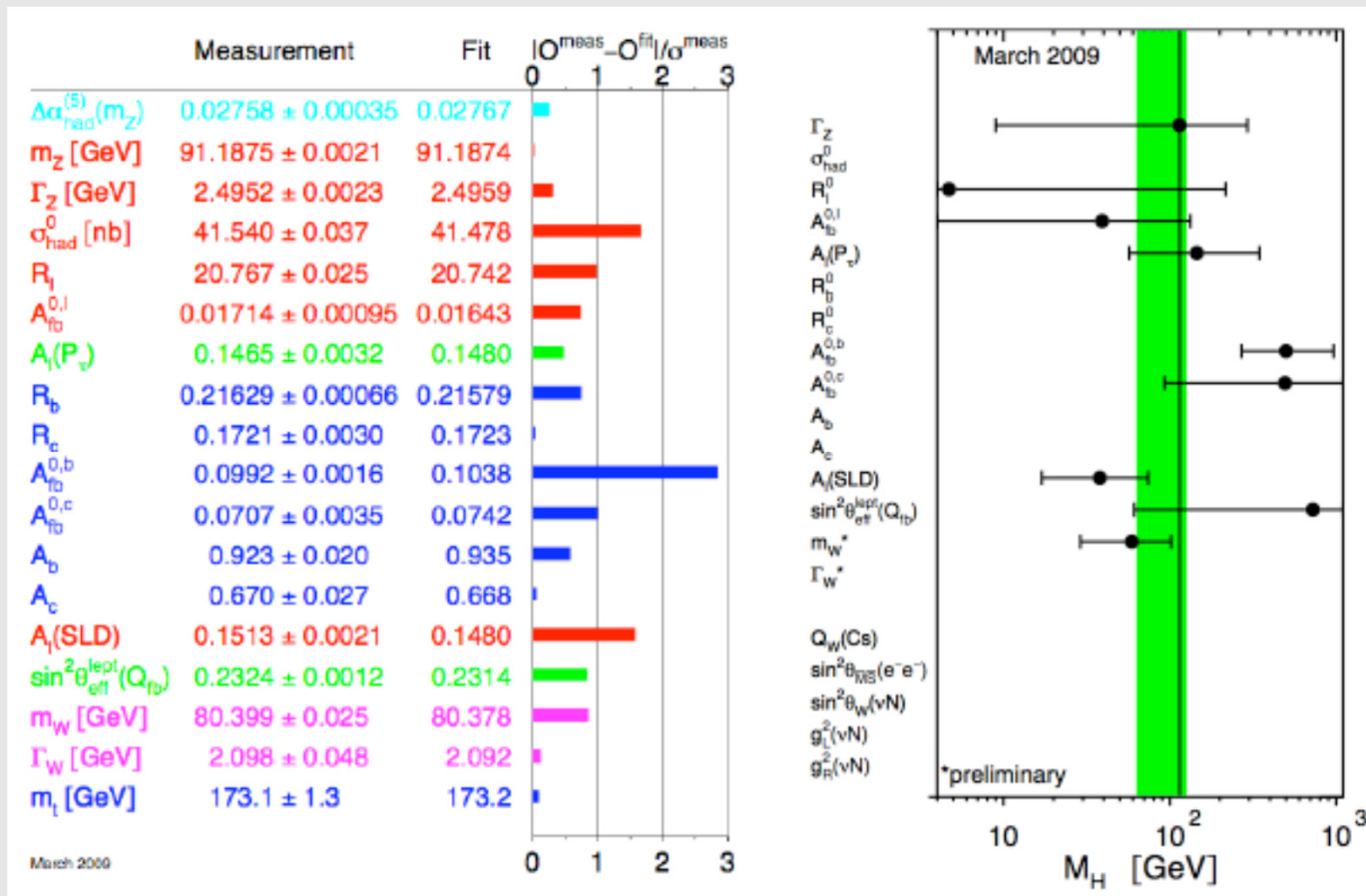
Ex:  $m_W$



# H Searches - XI

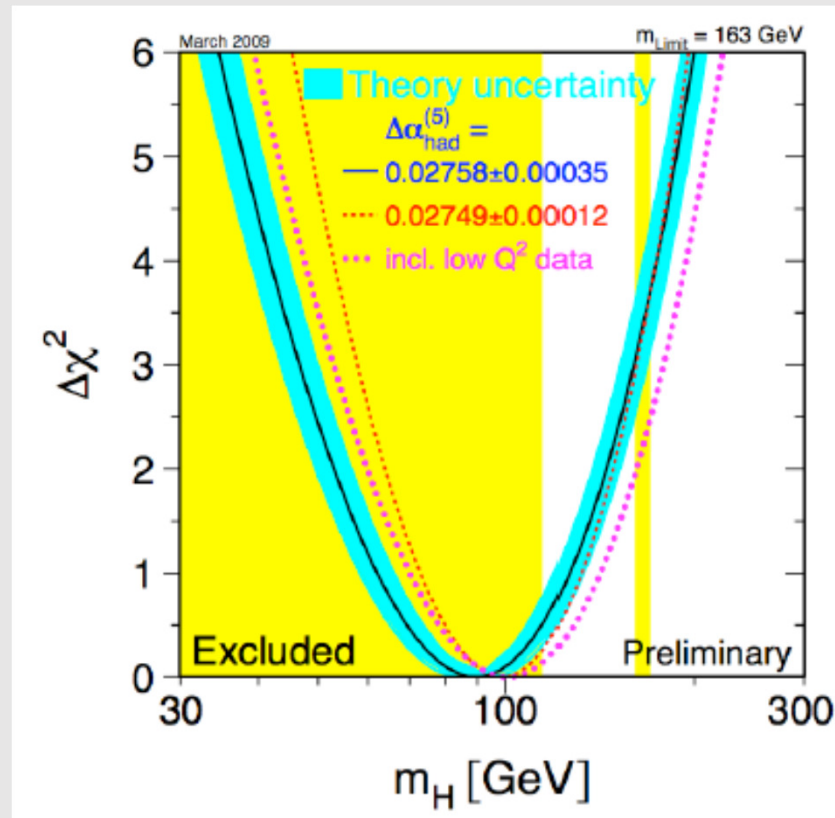
Global fit to  $\sim 20$  EW observables:

Best indirect estimate of  $m_H$



# H Searches - XII

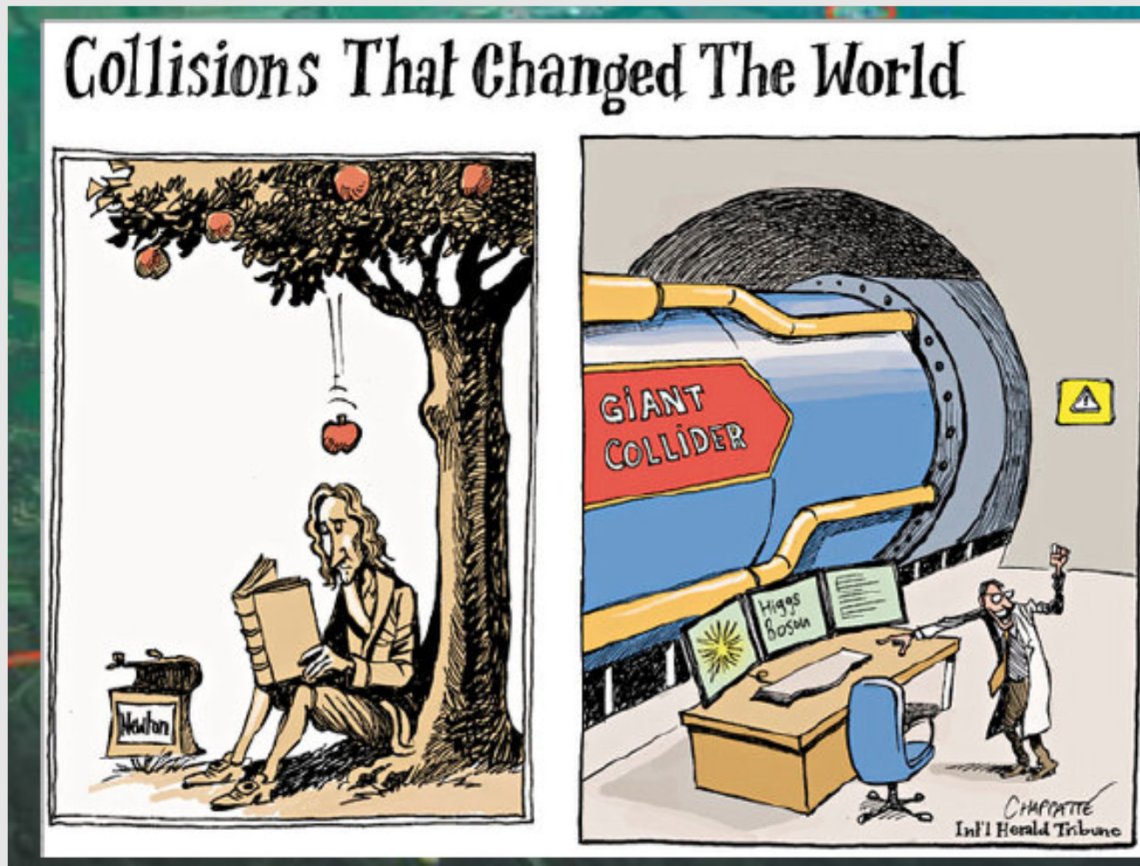
$\chi^2$  minimization:



$$m_H = 90_{-27}^{+36} \text{ GeV}, 68\% \text{ CL}$$



# LHC: Machine - I



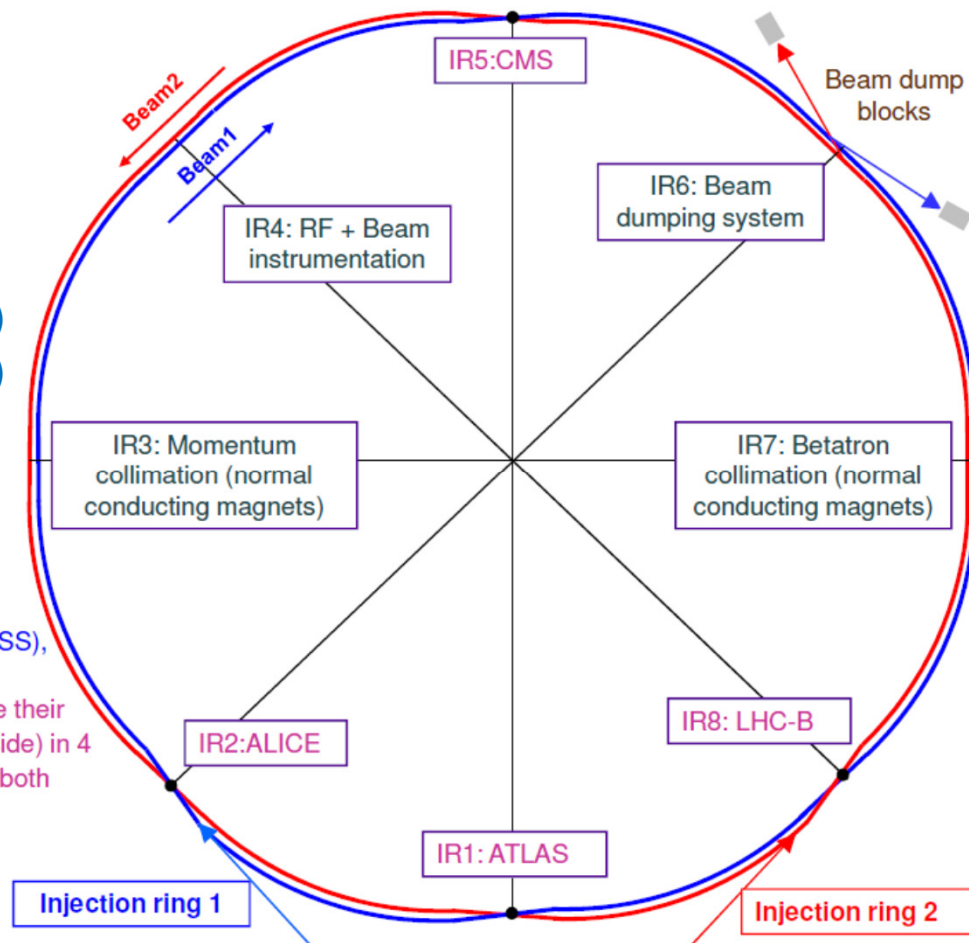
# LHC: Machine - II

LHC dipole field 8.3 T  
(HERA/Tevatron ~4 T)

LHC pp  $\sim 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$   
(Tevatron pp  $3 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ )  
(SppbarS pp  $6 \times 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$ )

### LHC Layout

- 8 arcs.
- 8 straight sections (LSS), ~ 700 m long.
- The beams exchange their positions (inside/outside) in 4 points to ensure that both rings have the same circumference !



# LHC: Machine - III

$R = L\sigma$  Rate, Luminosity, Cross-Section

$$L = \frac{kN^2 f}{4\pi\sigma_x^* \sigma_y^*}$$

$k$  = number of bunches = 2808

$N$  = no. protons per bunch =  $1.15 \times 10^{11}$

$f$  = revolution frequency = 11.25 kHz

$\sigma_x^*, \sigma_y^*$  = beam sizes at collision point (hor./vert.) = 16 mm

High L:

Many bunches ( $k$ )

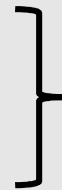
Many protons per bunch ( $N$ )

A small beam size  $\sigma_u^* = (\beta^* \varepsilon)^{1/2}$

$\beta^*$  : Beam envelope (optics)

$\varepsilon$  : Phase space volume occupied

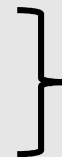
by the beam (constant along the ring)



High beam “brilliance”  $N/\varepsilon$   
(particles per phase space volume)  
→ Injector chain performance  
Small envelope  
→ Strong focusing



Optics property



Beam property

# LHC: Machine - IV

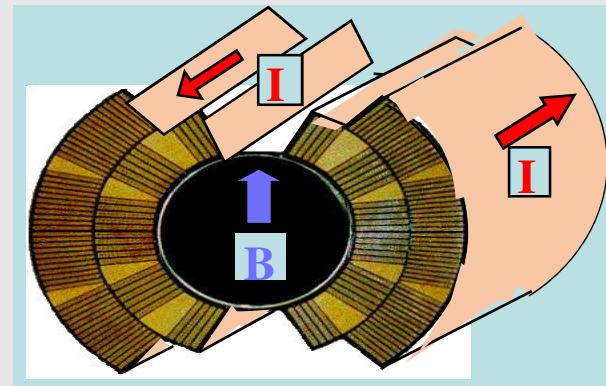
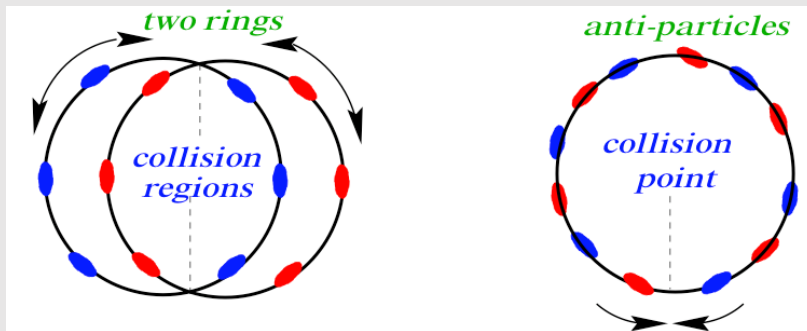
$$B\rho = \frac{mv}{e} = \frac{p}{e}$$

LHC:  $\rho = 2.8$  km given by LEP tunnel

To reach  $p = 7$  TeV/c given a bending radius of  $\rho = 2805$  m:

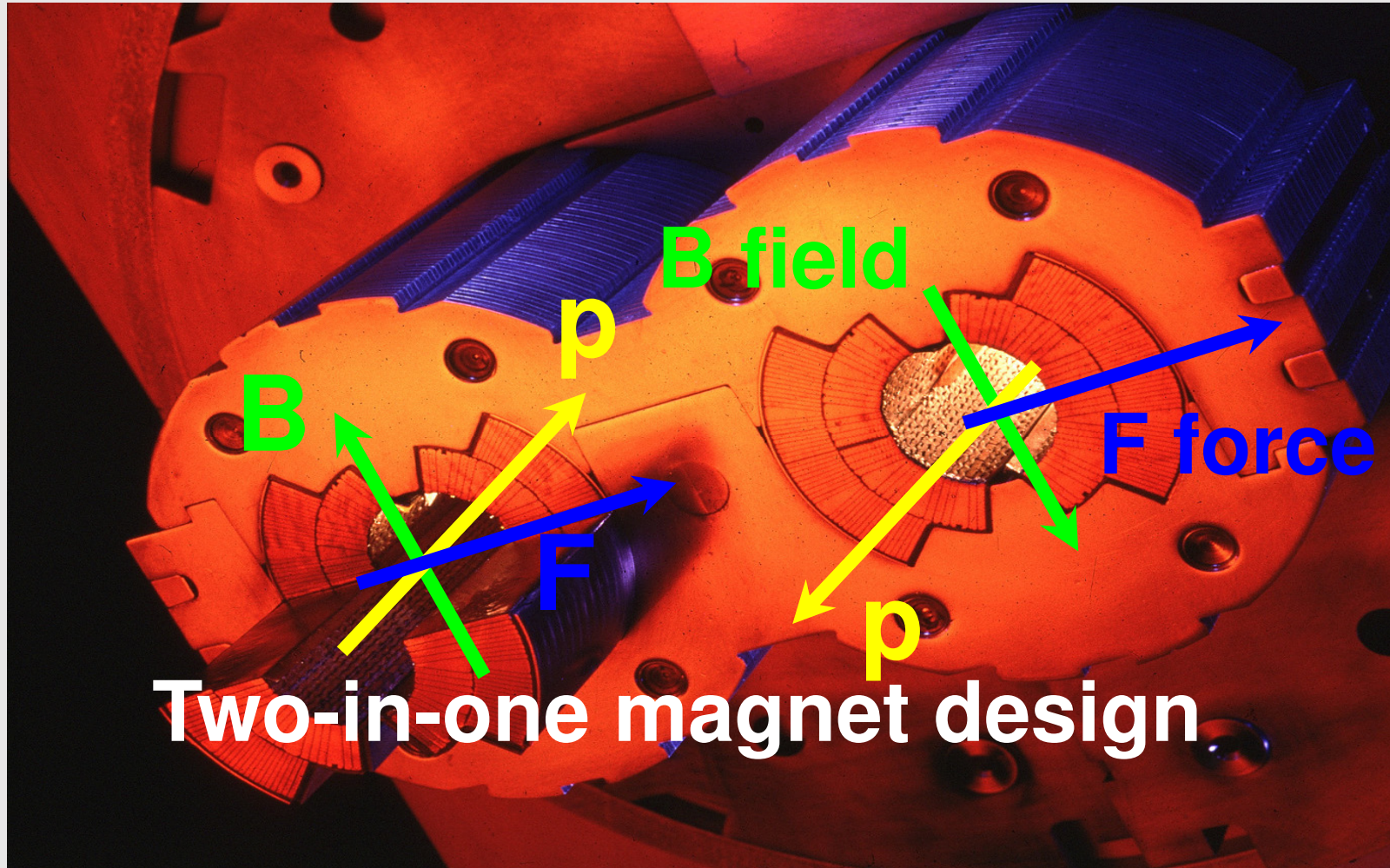
Bending field :  $B = 8.33$  T

→ Superconducting magnets



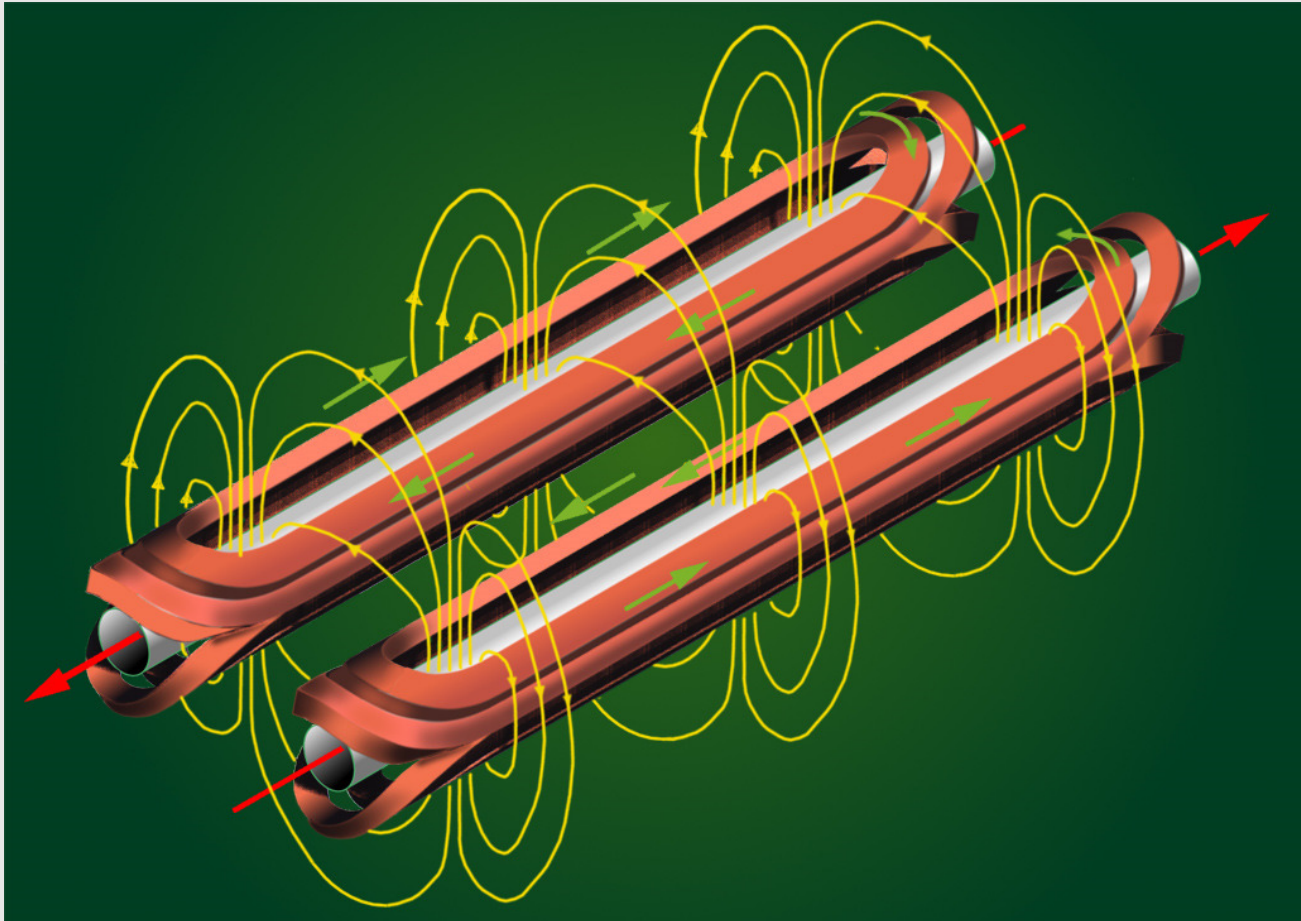


# LHC: Machine - V



# LHC: Machine - VI

Superconducting coils:

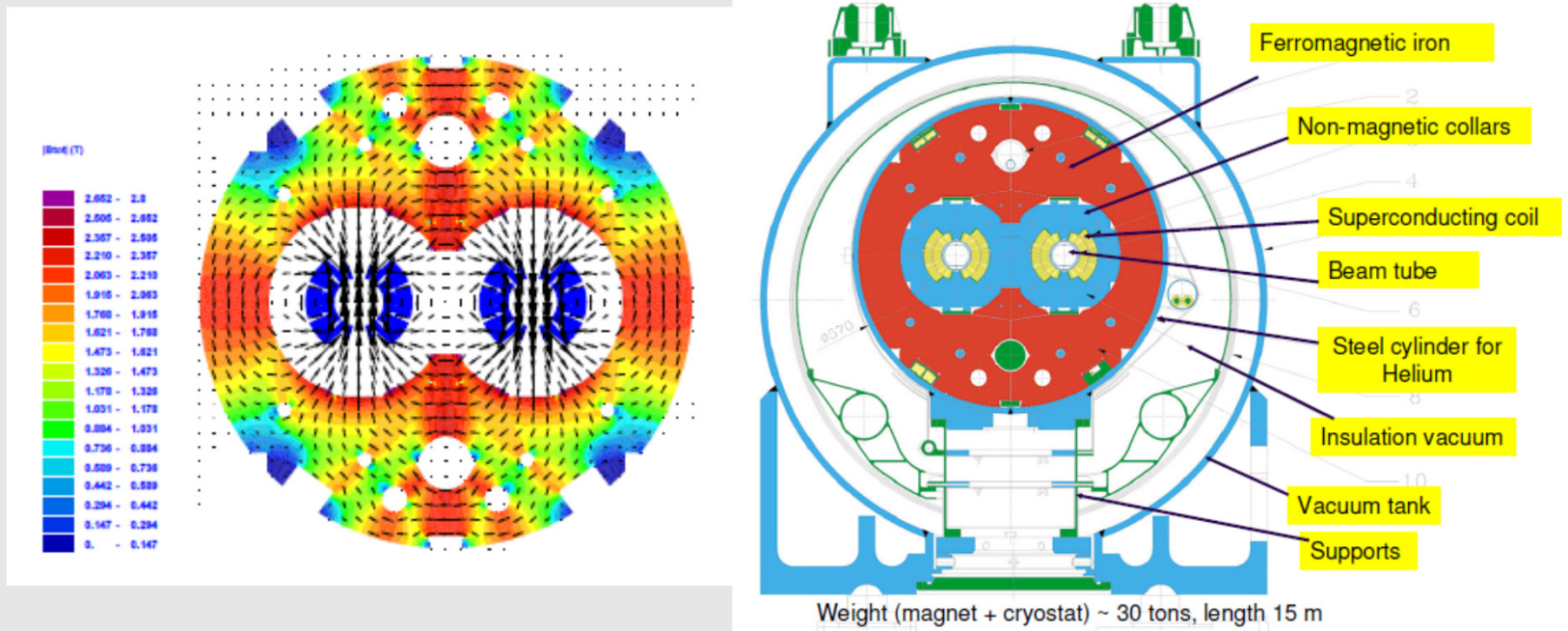




# LHC: Machine - VII

LHC main dipole:

Two magnets in a single module



# LHC: Machine - VIII

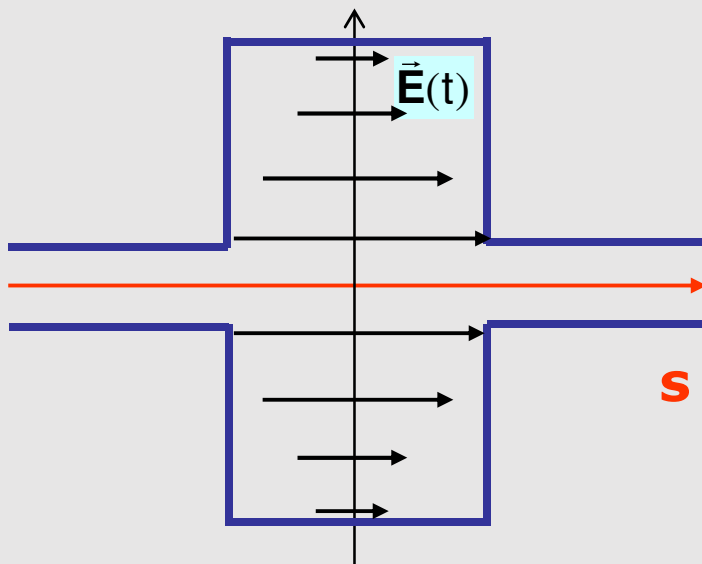
RF system:

4 + 4 Superconducting RF cavities

400 MHz

$\sim 0.5$  MeV/turn

20 minutes for 450 GeV  $\rightarrow$  7 TeV

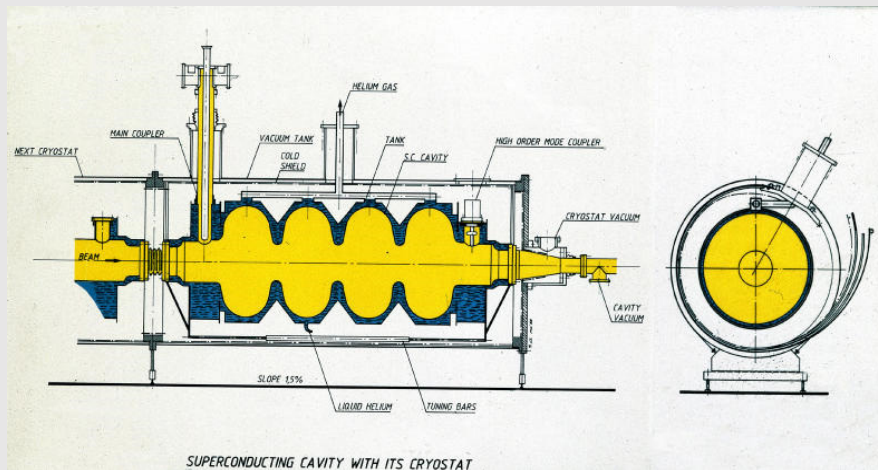


	Synchrotron radiation loss
LHC @ 3.5 TeV	0.42 keV/turn
LHC @ 7 TeV	6.7 keV /turn
LEP @ 104 GeV	$\sim 3$ GeV /turn



# LHC: Machine - IX

## Superconducting cavity



# H - I

Selecting best decay channels for detection:

Strongly dependent on (unknown)  $M_H$

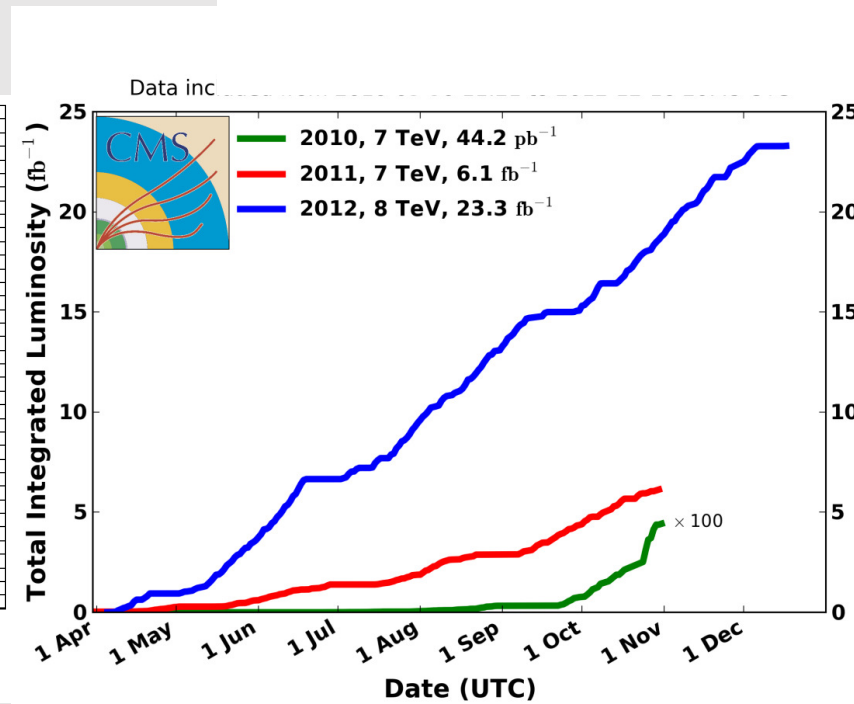
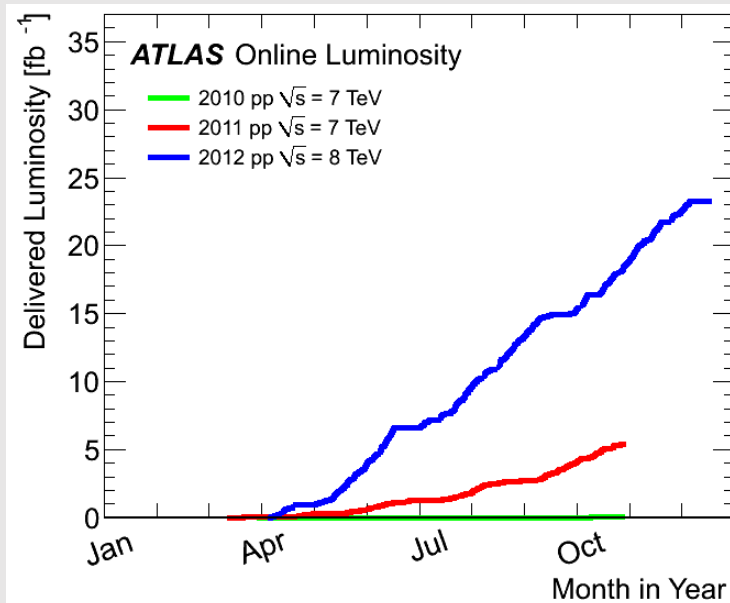
By taking  $M_H < 2M_W$

- $b\bar{b}$ : Large  $BR > 50\%$ , good signature (secondary vertexes), *lots* of QCD background
- $\tau^+\tau^-$ : Large  $BR \sim 7\%$ , somewhat harder than  $b\bar{b}$  (neutrinos)
- $\gamma\gamma$ : Tiny  $BR \sim 2 \cdot 10^{-3}$ , small background, experimentally challenging
- $gg$ : Large  $BR \sim 5\%$ , 2 jets, *lots* of QCD background
- $ZZ^*$ : Small  $BR \sim 3\%$ , small background in the 4 leptons mode
- $WW^*$ : Large  $BR \sim 20\%$ , sizeable QCD background in the 4 jets mode, harder than  $ZZ^*$  in leptonic modes (neutrinos)

# H - II

Total integrated luminosity:

$\sim 30 \text{ fb}^{-1}$  / experiment

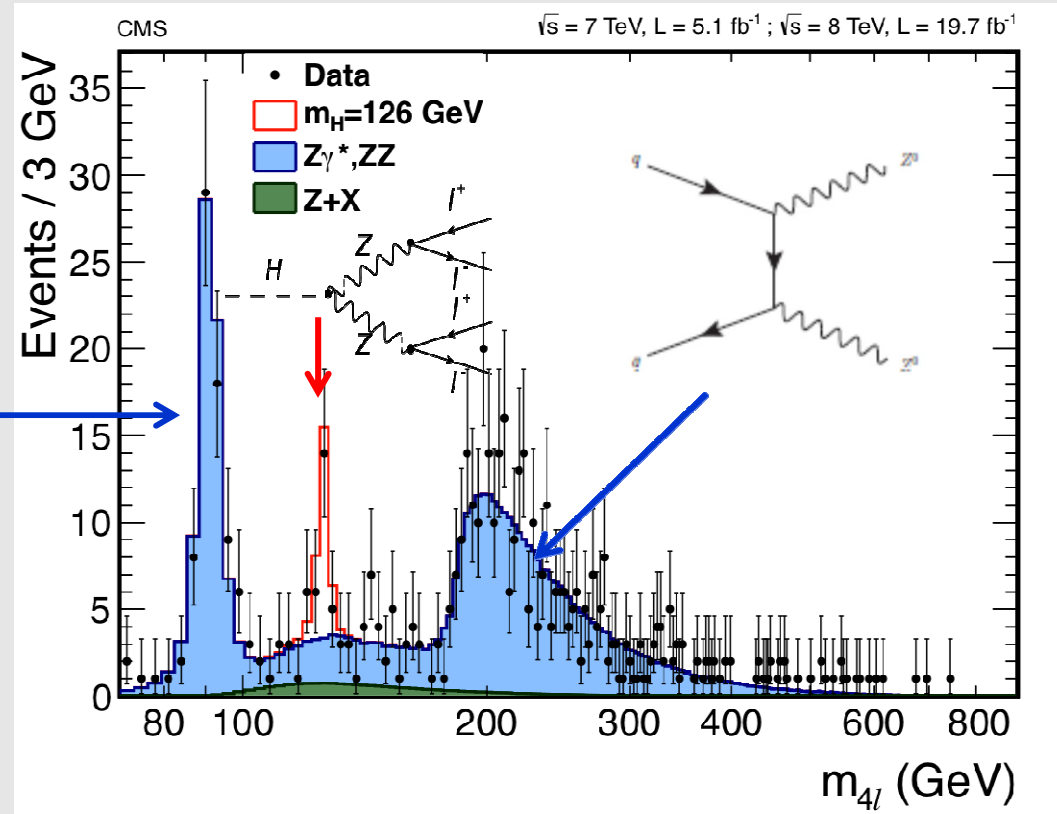
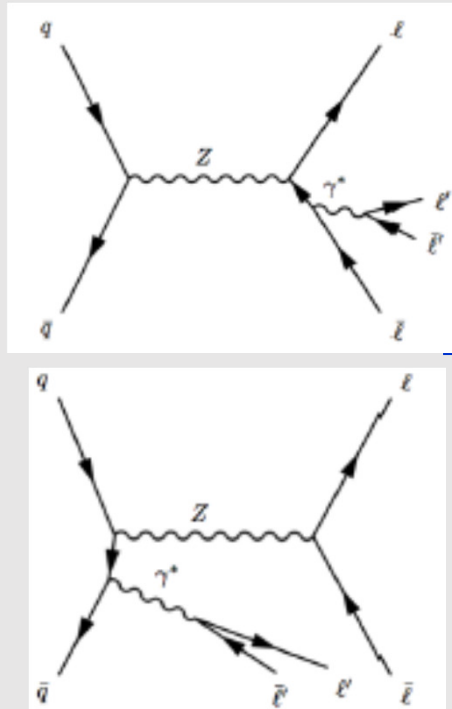


Phenomenal performance:

- Record luminosity ( $> 5 \times 10^{33}$ ) obtained soon after startup in 2012
- Sustained data collection rate of  $> 1.0 \text{ fb}^{-1} / \text{wk}$
- Delivered/recorded @ 8 TeV = [ 23.3 / 21.3 (ATLAS) , 21.8 (CMS) ]  $\text{fb}^{-1}$

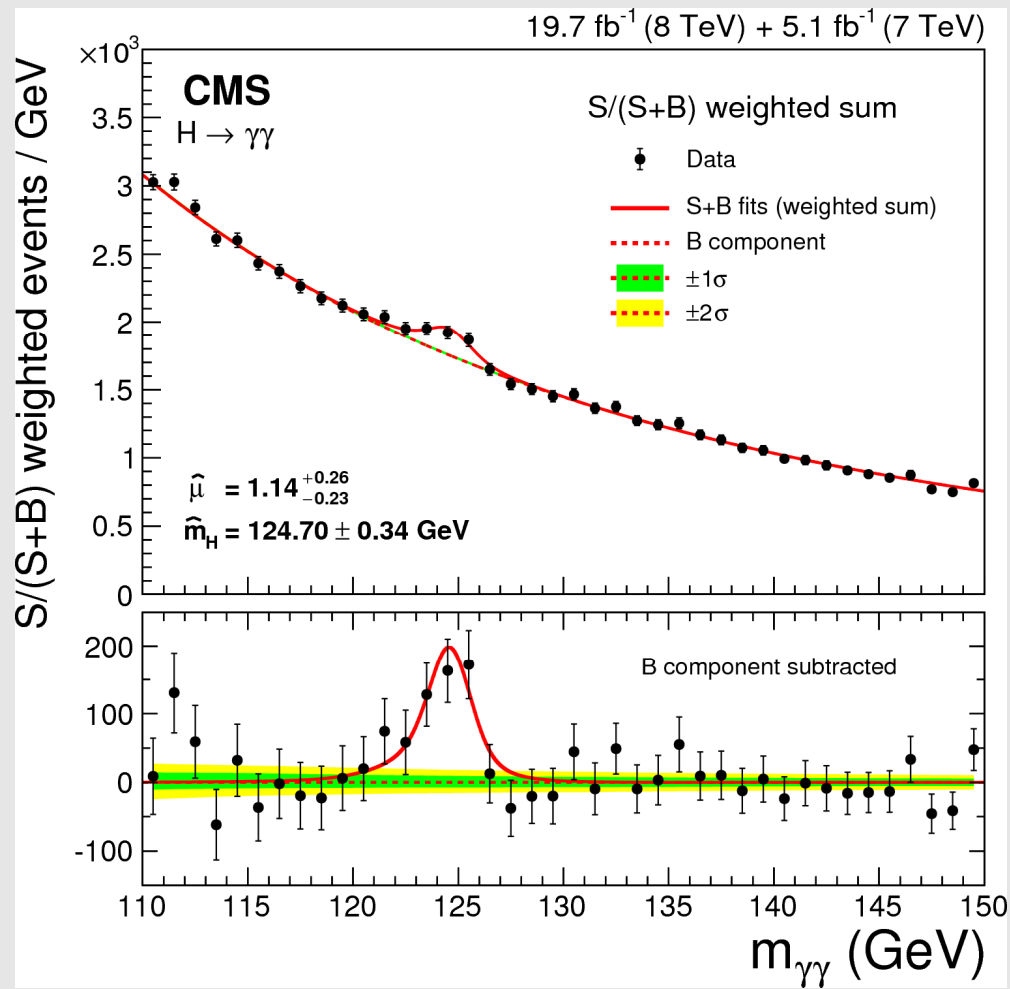
# H - III

4 leptons:  
 $\sim 7\sigma$  observation



# H - IV

2  $\gamma$ 's:  
 $\sim 6 \sigma$  observation



# $H - V$

Signal strength:

	ATLAS (expected)	ATLAS (observed)	CMS (expected)	CMS (observed)
$h \rightarrow \gamma\gamma$	4.1	7.4	5.2	5.7
$h \rightarrow ZZ$	4.4	6.6	6.7	6.8
$h \rightarrow WW$	3.7	3.8	5.8	4.3
$h \rightarrow \tau\tau$	3.2	4.1	3.6	3.4
$h \rightarrow bb$	1.6	$\sim 0$	2.1	2.1

# H - VI

Combined mass: All modes

$$m_H (\text{ATLAS}) = 125.36 \pm 0.37 (\text{stat}) \pm 0.18 (\text{syst})$$

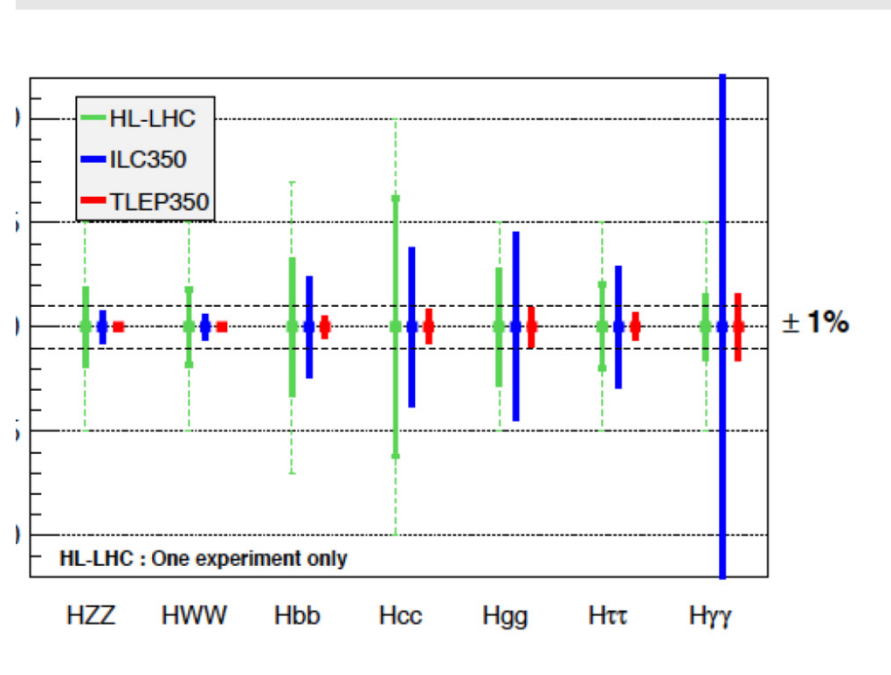
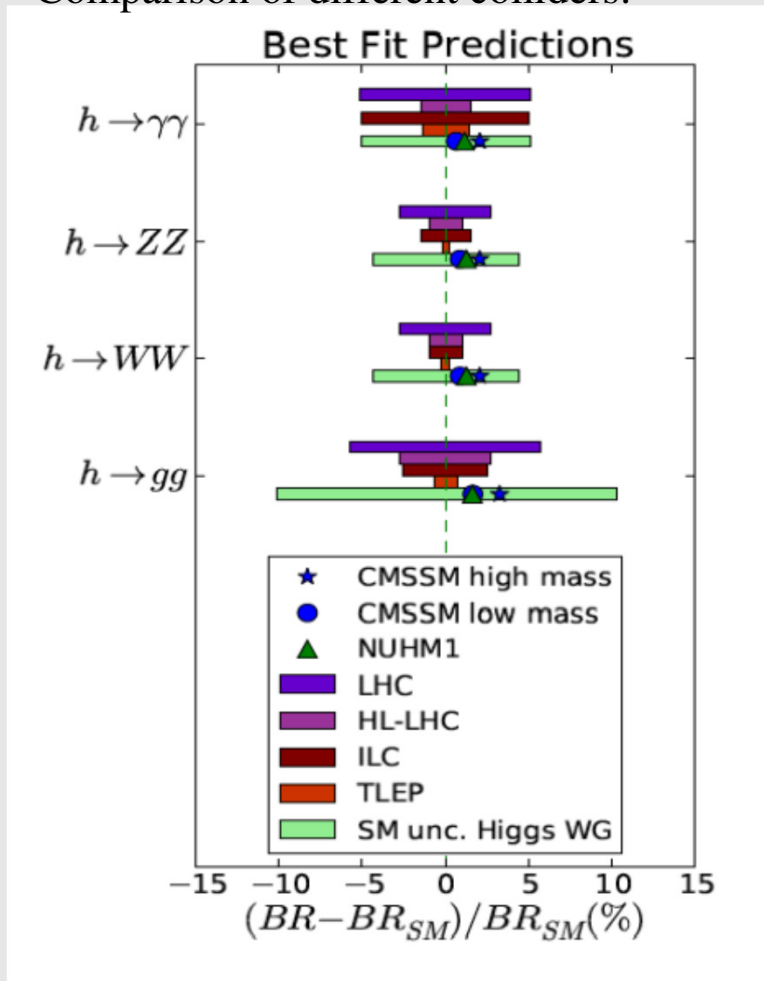
$$m_H (\text{CMS}) = 125.03^{+0.26}_{-0.27} (\text{stat})^{+0.13}_{-0.15} (\text{syst})$$

Many more results on spin/parity, couplings, width...

....Next time!

# Future Collider Comparison - I

Comparison of different colliders:





# Future Collider Comparison - II

Accelerator →  Physical Quantity ↓	LHC 300 fb <sup>-1</sup> /expt	HL-LHC 3000 fb <sup>-1</sup> /expt	ILC 250 GeV 250 fb <sup>-1</sup>  5 yrs	Full ILC 250+350+ 1000 GeV  5yrs each	CLIC 350 GeV (500 fb <sup>-1</sup> ) 1.4 TeV (1.5 ab <sup>-1</sup> )  5 yrs each	LEP3, 4 IP 240 GeV 2 ab <sup>-1</sup> (*)  5 yrs	TLEP, 4 IP 240 GeV 10 ab <sup>-1</sup> 5 yrs (*)  350 GeV 1.4 ab <sup>-1</sup> 5 yrs (*)
N <sub>H</sub>	1.7 × 10 <sup>7</sup>	1.7 × 10 <sup>8</sup>	6 × 10 <sup>4</sup> ZH	10 <sup>5</sup> ZH 1.4 × 10 <sup>5</sup> H <sub>νν</sub>	7.5 × 10 <sup>4</sup> ZH 4.7 × 10 <sup>5</sup> H <sub>νν</sub>	4 × 10 <sup>5</sup> ZH	2 × 10 <sup>6</sup> ZH 3.5 × 10 <sup>4</sup> H <sub>νν</sub>
m <sub>H</sub> (MeV)	100	50	35	35	100	26	7
ΔΓ <sub>H</sub> / Γ <sub>H</sub>	--	--	10%	3%	ongoing	4%	1.3%
ΔΓ <sub>inv</sub> / Γ <sub>H</sub>	Indirect (30%?)	Indirect (10%?)	1.5%	1.0%	ongoing	0.35%	0.15%
Δg <sub>Hγγ</sub> / g <sub>Hγγ</sub>	6.5 – 5.1%	5.4 – 1.5%	--	5%	ongoing	3.4%	1.4%
Δg <sub>HZZ</sub> / g <sub>HZZ</sub>	11 – 5.7%	7.5 – 2.7%	4.5%	2.5%	< 3%	2.2%	0.7%
Δg <sub>HWW</sub> / g <sub>HWW</sub>	5.7 – 2.7%	4.5 – 1.0%	4.3%	1%	~1%	1.5%	0.25%
Δg <sub>HZZ</sub> / g <sub>HZZ</sub>	5.7 – 2.7%	4.5 – 1.0%	1.3%	1.5%	~1%	0.65%	0.2%
Δg <sub>HHH</sub> / g <sub>HHH</sub>	--	< 30% (2 expts)	--	~30%	~22% (~11% at 3 TeV)	--	--
Δg <sub>HUU</sub> / g <sub>HUU</sub>	< 30%	< 10%	--	--	10%	14%	7%
Δg <sub>Htt</sub> / g <sub>Htt</sub>	8.5 – 5.1%	5.4 – 2.0%	3.5%	2.5%	≤ 3%	1.5%	0.4%
Δg <sub>Hcc</sub> / g <sub>Hcc</sub>	--	--	3.7%	2%	2%	2.0%	0.65%
Δg <sub>Hbb</sub> / g <sub>Hbb</sub>	15 – 6.9%	11 – 2.7%	1.4%	1%	1%	0.7%	0.22%
Δg <sub>Htt</sub> / g <sub>Htt</sub>	14 – 8.7%	8.0 – 3.9%	--	5%	3%	--	30%