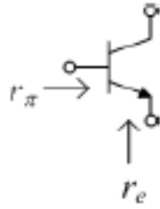


Miglioramenti del modello a T:

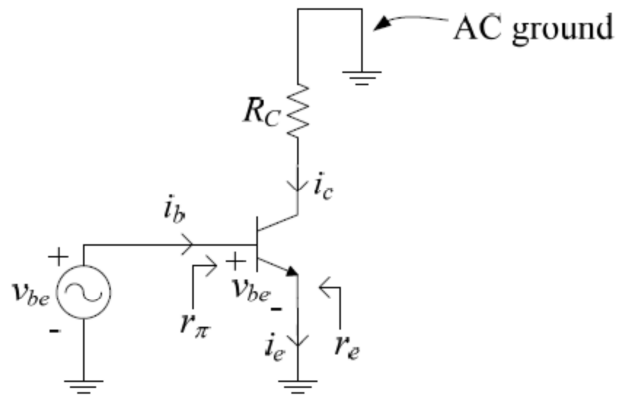
Resistenze equivalenti 'guardando' nella base e nell' emettitore



$$r_e = \frac{V_T}{I_C} \quad \text{resistenza dinamica della giunzione BE in zona attiva}$$

$$g_m = \frac{1}{r_e} = \frac{I_C}{V_T} \quad \text{transconduttanza (per piccoli segnali) del transistor}$$

$$g_m = \frac{1}{r_e} \sim \frac{dI_C}{dV_{BE}} \sim \frac{i_c}{v_{be}} \rightarrow i_c \simeq g_m v_{be} \rightarrow i_b \simeq \frac{g_m}{\beta} v_{be}$$



$$r_\pi = \frac{v_{be}}{i_b} = \frac{\beta}{g_m} = \frac{\beta V_T}{I_C}$$

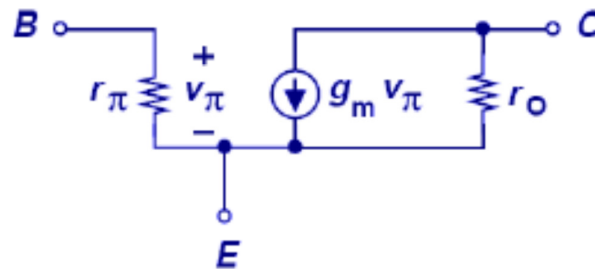
$$i_E = \frac{i_C}{\alpha} = \frac{I_C}{\alpha} + \frac{i_c}{\alpha}$$

$$i_e = \frac{i_c}{\alpha} = \frac{I_C}{\alpha} \frac{v_{be}}{V_T} = \frac{I_E v_{be}}{V_T}$$

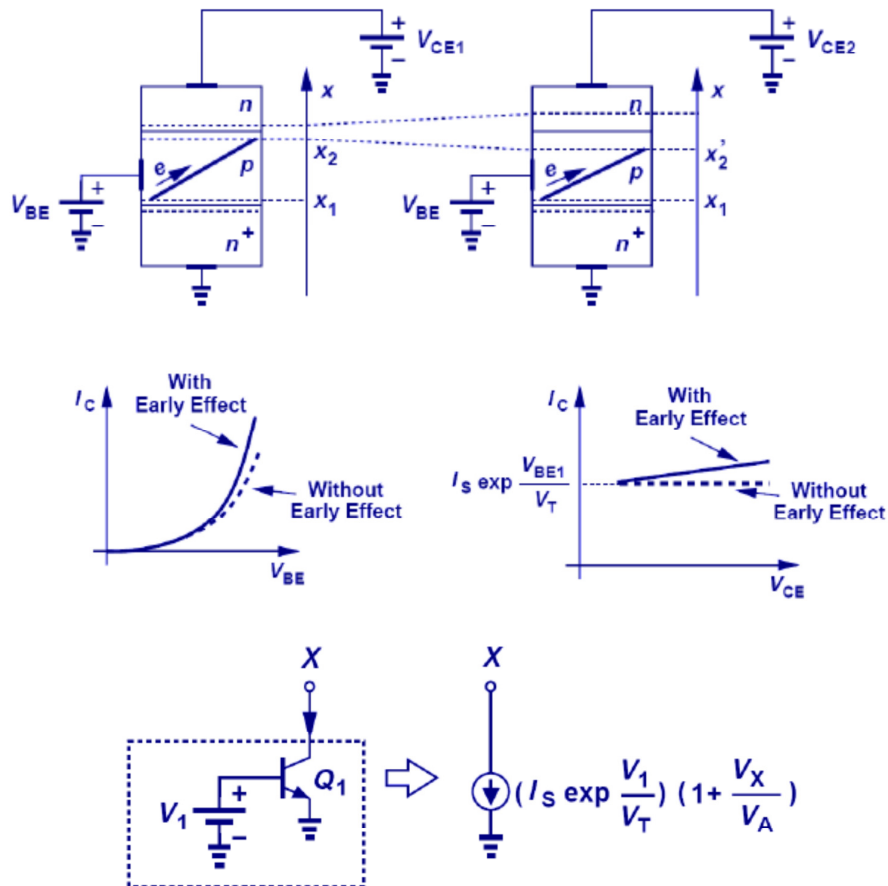
$$r_e = \frac{v_{be}}{i_e} = \frac{V_T}{I_E} = \frac{\alpha}{g_m} \left(\approx \frac{1}{g_m} \right)$$

$$\rightarrow r_\pi = \frac{\beta}{g_m} = \frac{\beta}{\alpha} r_e = \frac{\beta}{\beta} (\beta + 1) r_e = (\beta + 1) r_e$$

Modello a π ibrido: Versione a bassa frequenza

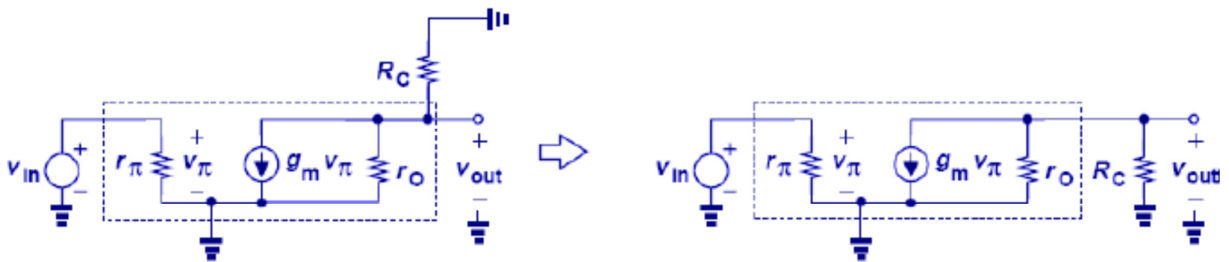
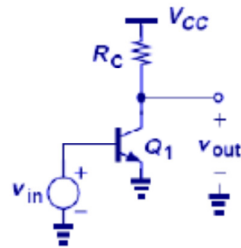


r_o legata all'effetto Early: I_C non indipendente da V_{CE}

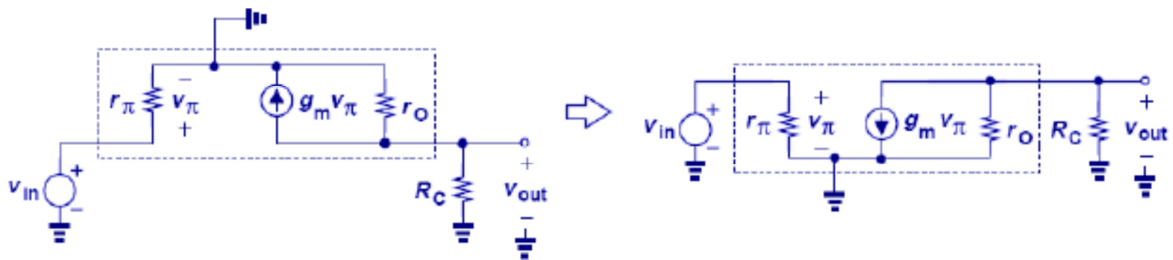
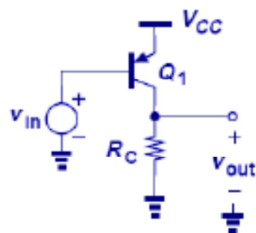


C generatore non ideale di corrente $\rightarrow r_o < \infty$ in parallelo al generatore di corrente

Esempio: Applicazione a stadio semplice CE



Identico per PNP:



Impedenze intrinseche del BJT (in zona attiva!):

Base: Si 'guarda' dentro B

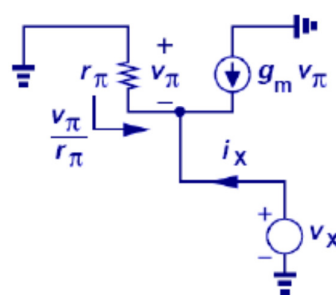
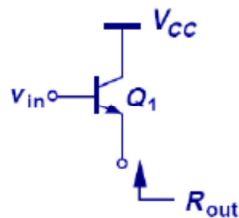
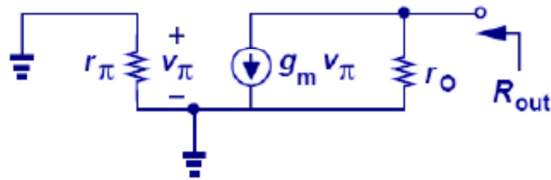
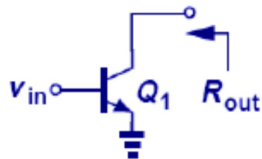
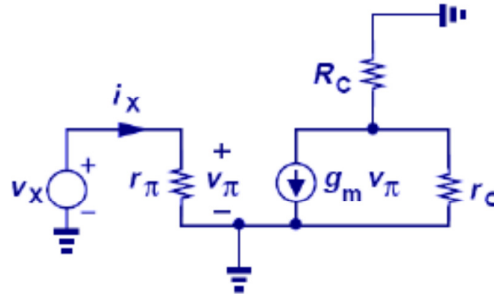
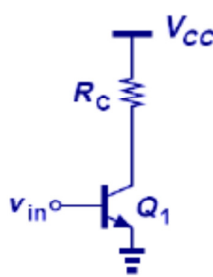
$R_b = r_\pi$; stato uscita irrilevante perche' r_o a ground

Collettore: Si 'guarda' dentro C

$R_c = r_o \approx \infty$, $r_o \rightarrow \infty$; B (ed E) a ground $\rightarrow v_\pi = 0 \rightarrow g_m v_\pi = 0$

Emettitore : Si 'guarda' dentro E

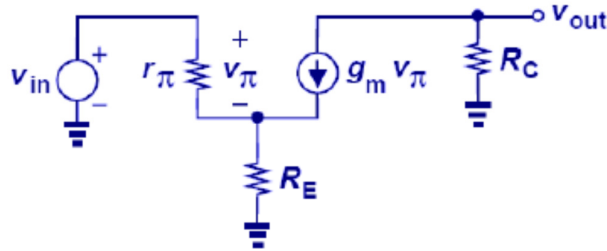
$$R_e = \frac{v_x}{i_x} = \frac{1}{g_m + \frac{1}{r_\pi}} \approx \frac{1}{g_m}, \quad r_o \rightarrow \infty; \text{ B e C a ground } \rightarrow i_x = \frac{v_\pi}{r_\pi} + g_m v_\pi$$



Applicazione: Stadio CE con resistenza su emettitore

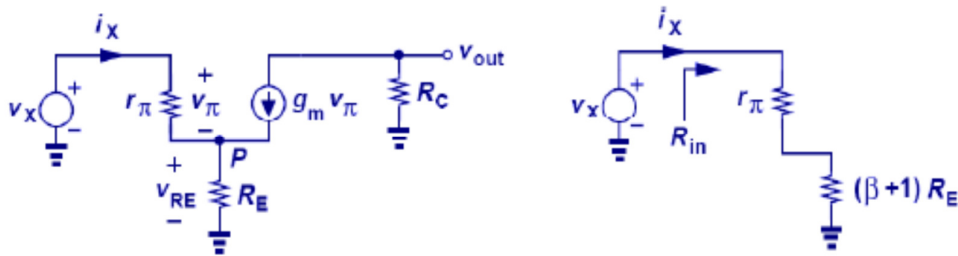
NB: Non considerate resistenze del partitore di bias

Non considerato effetto Early



$$A_v = -\frac{g_m R_C}{1 + g_m R_E} = -\frac{R_C}{\frac{1}{g_m} + R_E}$$

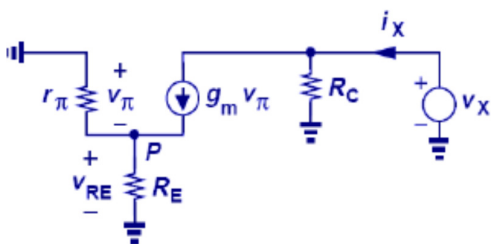
Impedenza di ingresso:



$$v_x = [r_\pi + R_E (1 + \beta)] i_x$$

$$\rightarrow R_{in} = \frac{v_x}{i_x} = r_\pi + R_E (1 + \beta)$$

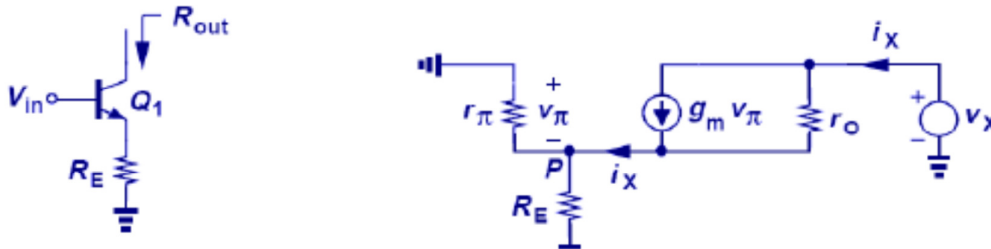
Impedenza di uscita:



$$v_{in} = v_\pi + \left(\frac{v_\pi}{r_\pi} + g_m v_\pi \right) R_E = 0 \rightarrow v_\pi = 0$$

$$\rightarrow R_{out} = \frac{v_x}{i_x} = R_C$$

Tenendo conto dell'effetto Early:



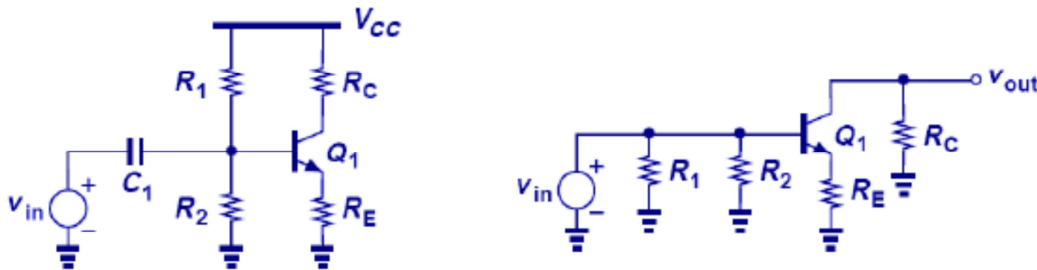
$$R_{out} = [1 + g_m (R_E \parallel r_\pi)] r_o + R_E \parallel r_\pi$$

$$R_{out} = r_o + (g_m r_o + 1)(R_E \parallel r_\pi)$$

$$R_{out} \approx r_o [1 + g_m (R_E \parallel r_\pi)]$$

R_{out} aumentata $\rightarrow$ Migliorato generatore di corrente

Tenendo conto del partitore di bias:

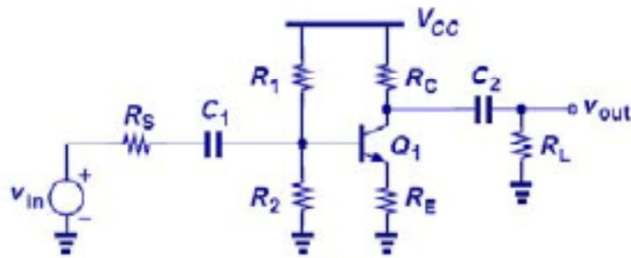


$$A_v = \frac{-R_C}{\frac{1}{g_m} + R_E}$$

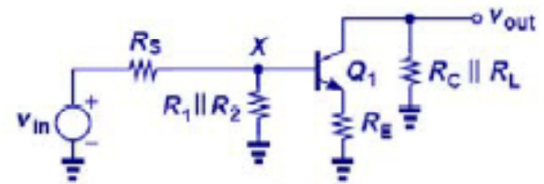
$$R_{in} = [r_\pi + (\beta + 1)R_E] \parallel R_1 \parallel R_2$$

$$R_{out} = R_C$$

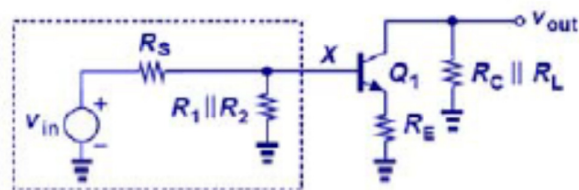
Al gran completo:



(a)



(b)



(b)

$$A_v = \frac{-R_C \parallel R_L}{\frac{1}{g_m} + R_E + \frac{R_S \parallel R_1 \parallel R_2}{\beta + 1}}$$

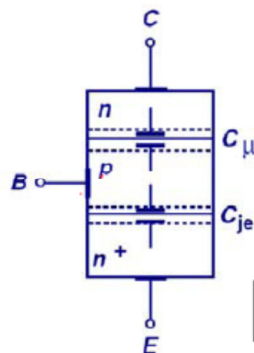
Comportamento del BJT ad alta frequenza:

Legato a caratteristiche reattive delle giunzioni

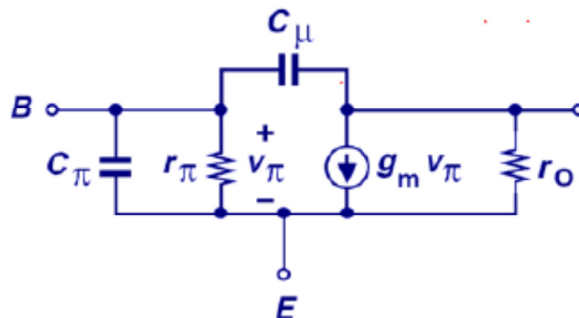
Zona attiva:

Giunzione di emettitore pol. diretta → Cap. di transizione + Cap. di diffusione

Giunzione di collettore pol. inversa → Capacita' di transizione



Modello a π ibrido esteso ad elementi reattivi:



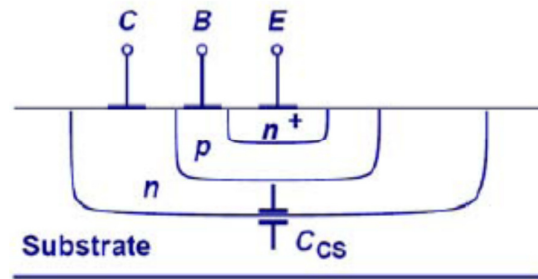
Capacita' effettive delle giunzioni:

$$C_{\pi} = C_{be} + C_{diff} \quad \text{transizione + diffusione}$$

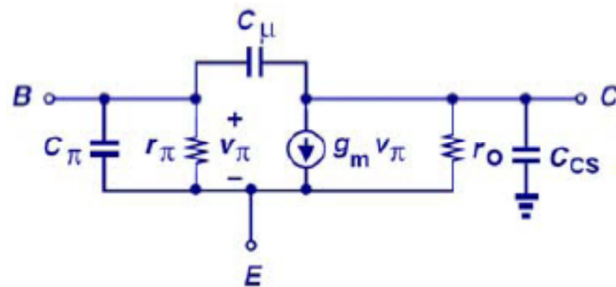
$$C_{\mu} = C_{bc} \quad \text{transizione}$$

Inoltre, nei circuiti integrati:

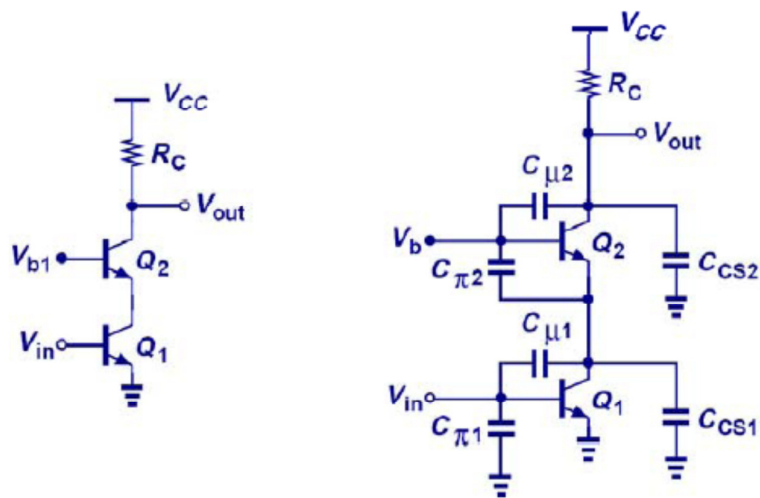
C_{cs} capacita' collettore-substrato



Modello completo per BJT in CI:



Es: Capacita' in un circuito specifico ('Cascode', v. dopo)

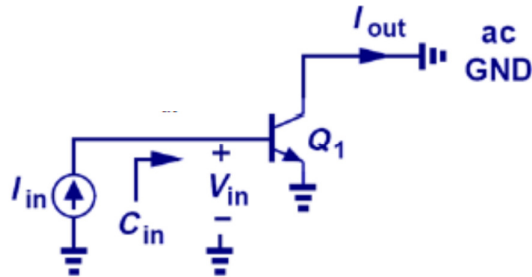


Effetto principale della capacita' C_π :

Riduzione del guadagno di corrente ad alta frequenza

Def: ω_T frequenza di guadagno unitario

Misura 'concettuale':



$$I_{out} = g_m V_{in}$$

$$V_{in} = Z_{in} I_{in}$$

$$\rightarrow I_{out} = g_m Z_{in} I_{in}$$

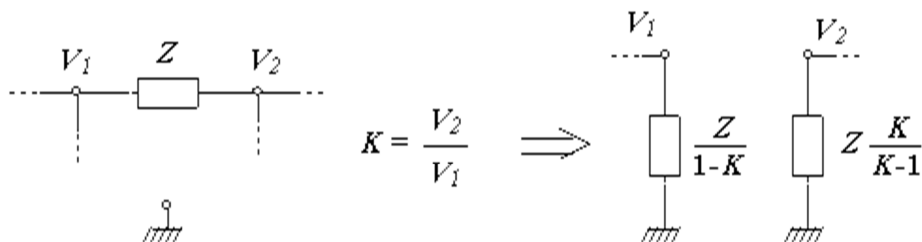
$$\rightarrow \frac{I_{out}}{I_{in}} = g_m Z_{in} = g_m \frac{1}{j\omega C_\pi}$$

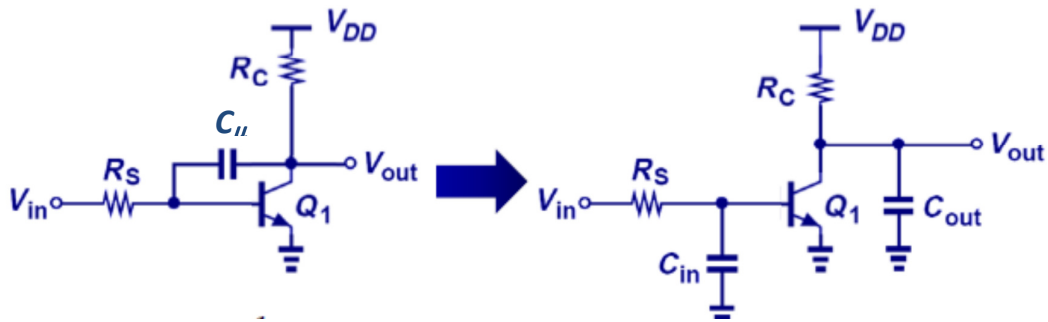
$$\left| \frac{I_{out}}{I_{in}} \right| = 1 \rightarrow \frac{g_m}{\omega_T C_\pi} = 1 \rightarrow \omega_T = \frac{g_m}{C_\pi}$$

Effetto di C_μ : ???

Difficile da visualizzare: Capacita' 'floating', senza terminali a ground

→ Teorema di Miller (non dimostrato):





$$Z_1 = \frac{1}{\frac{j\omega C_{\mu}}{1 - A_v}} = \frac{1}{j\omega C_{\mu} (1 - A_v)}$$

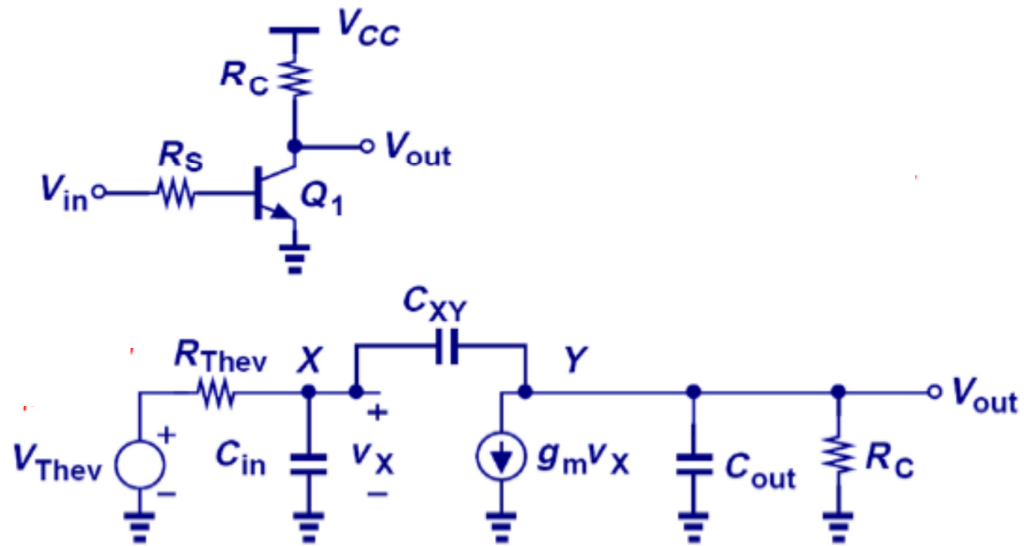
$$Z_2 = \frac{1}{1 - \frac{1}{A_v}} = \frac{1}{j\omega C_{\mu} \left(1 - \frac{1}{A_v}\right)}$$

$$A_v < 0 \rightarrow C_{\mu} \nearrow :$$

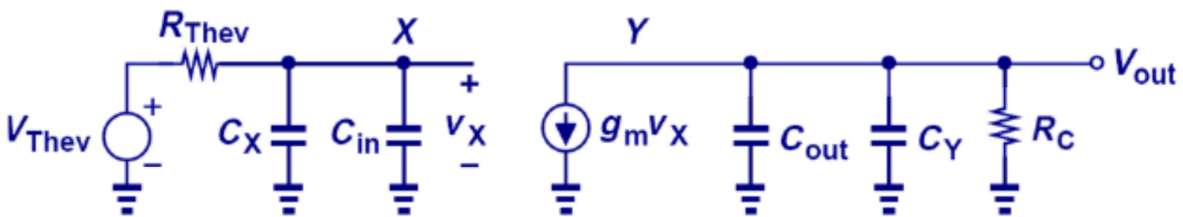
Effetto Miller = Aumento della capacita' floating

$|A_v| \gg 1 \rightarrow$ Effetto dominante quello di C_{in}

Applicazione a stadio *CE*:



Teorema di Miller:



$$V_{\text{Thev}} = V_{\text{in}} \frac{r_{\pi}}{r_{\pi} + R_S}$$

$$R_{\text{Thev}} = R_S \parallel r_{\pi}$$

$$C_X = C_{\mu} (1 + g_m R_C)$$

$$C_Y = C_{\mu} \left(1 + \frac{1}{g_m R_C} \right)$$

Frequenze di taglio, ingresso e uscita, per guadagno:

$$\omega_{p,in} = \frac{1}{R_{Thev} (C_{in} + (1 + g_m R_C) C_\mu)}$$

$$\omega_{p,out} = \frac{1}{R_C \left(C_{out} + \left(1 + \frac{1}{g_m R_C} \right) C_\mu \right)}$$

Impedenze di ingresso e uscita:

$$Z_{in} \approx \frac{1}{j\omega [C_\pi + (1 + g_m (R_C \parallel r_o)) C_\mu]} \parallel r_\pi$$

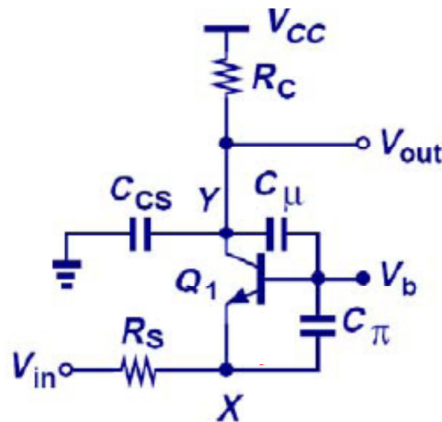
$$Z_{out} = \frac{1}{j\omega [C_\mu + C_{CS}]} \parallel R_C \parallel r_o$$

Applicazione a stadio a *CB*:

Vantaggi notevoli nella risposta in frequenza

Nessuna capacita' floating

→ No effetto Miller (← V_b sta a valore fisso!)



$$\omega_{p,Y} = \frac{1}{R_C C_Y}$$

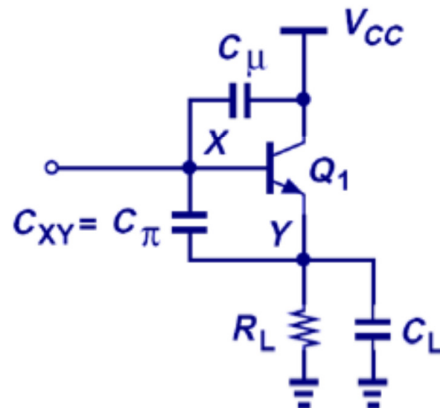
$$C_Y = C_\mu + C_{CS}$$

$$\omega_{p,X} = \frac{1}{\left(R_S \parallel \frac{1}{g_m} \right) C_X} > \omega_T$$

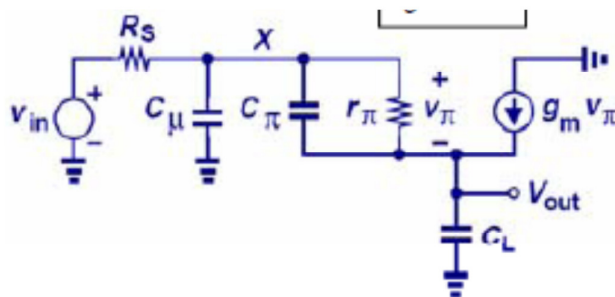
$$C_X = C_\pi$$

→ Frequenze di taglio $\sim$ Essenzialmente indipendenti dal guadagno

Applicazione a stadio a CC (Emitter follower):



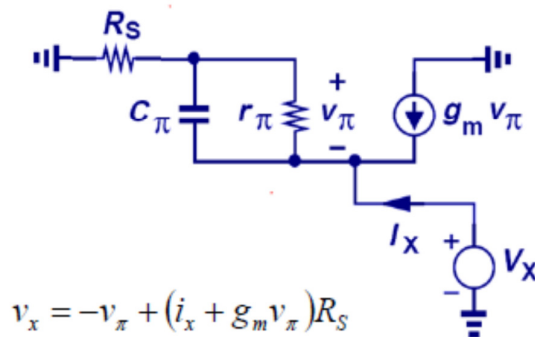
Modello a π ibrido (trascurando r_0):



$$C_X = (1 - A_v) C_\pi = \frac{C_\pi}{1 + g_m R_L}$$

$$C_Y = \left(1 - \frac{1}{A_v}\right) C_\pi = \frac{-C_\pi}{g_m R_L}$$

$$C_{in} = C_\mu + \frac{C_\pi}{1 + g_m R_L}$$



$$v_X = -v_\pi + (i_X + g_m v_\pi) R_S$$

$$v_\pi = -(i_X + g_m v_\pi) \left(r_\pi \parallel \frac{1}{j\omega C_\pi} \right) \quad v_X = -v_\pi + (i_X + g_m v_\pi) R_S$$

$$Z_{out} \equiv \frac{v_X}{i_X} = \frac{R_S r_\pi C_\pi (j\omega) + r_\pi + R_S}{r_\pi C_\pi (j\omega) + \beta + 1} = \frac{r_\pi + R_S}{\beta + 1} \cdot \frac{1 + \frac{j\omega}{(r_\pi + R_S)/R_S r_\pi C_\pi}}{1 + \frac{j\omega}{(\beta + 1)/r_\pi C_\pi}} = \begin{cases} \frac{r_\pi + R_S}{1 + \beta} & \text{for low } \omega \\ R_S & \text{for high } \omega \end{cases}$$